

The CO-to-H₂ Conversion Factor of the Galactic Giant Molecular Clouds using CO isotopologues: the high-resolution X_{CO} maps

Mikito Kohno^{1,2}[★], and Yoshiaki Sofue³

¹*Astronomy Section, Nagoya City Science Museum, 2-17-1 Sakae, Naka-ku, Nagoya, Aichi 460-0008, Japan*

²*Department of Physics, Graduate School of Science, Nagoya University, Furo-cho, Chikusa-ku, Nagoya, Aichi 464-8602, Japan*

³*Institute of Astronomy, The University of Tokyo, Mitaka, Tokyo 181-0015, Japan*

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ABSTRACT

We investigated the correlation between intensities of the ¹²CO and ¹³CO ($J = 1-0$) lines toward the Galactic giant molecular clouds (GMCs) W51A, W33, N35-N36 complex, W49, M17SW, G12.02-00.03, W43, and M16 using the FUGIN (FOREST Unbiased Galactic plane Imaging survey with the Nobeyama 45-m telescope) CO line data. All the GMCs showed intensity saturation in the ¹²CO line when the brightness temperature of ¹³CO is higher than a threshold temperature of about ~ 5 K. We obtained high-resolution ($\sim 20''$) distribution maps of the X_{CO} factor in individual GMCs using the correlation diagrams of the CO isotopologues. It was shown that X_{CO} is variable in each GMC within the range of $X_{\text{CO}} \sim (0.9-5) \times 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$. Despite the variability in the GMCs, the averaged value among the GMCs was found to be nearly constant at $X_{\text{CO}} = (2.16 \pm 0.30) \times 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$, which is consistent with that from the previous studies in the Milky Way.

Key words: ISM: clouds – ISM: general – ISM: molecules – radio lines: ISM

1 INTRODUCTION

Molecular clouds mainly consist of hydrogen molecules (H₂) and are the sites of star formation in galaxies (Blitz et al. 2007; Dobbs et al. 2014; Chevance et al. 2022). The hydrogen molecule is difficult to observe directly because it does not have an electric dipole moment for its homonuclear diatomic nature (Heyer & Dame 2015). Therefore, we often observe carbon monoxide (CO) with the rotational transitions at millimeter wavelengths and convert the intensity to the H₂ column density using the CO-to-H₂ conversion factor (hereafter X_{CO}), which is given by

$$X_{\text{CO}} = N_{\text{H}_2} / W_{12\text{CO}} [\text{cm}^{-2} (\text{K km s}^{-1})^{-1}], \quad (1)$$

where $W_{12\text{CO}}$ and N_{H_2} are the ¹²CO $J=1-0$ integrated intensity and column density of hydrogen molecule, respectively (Bolatto et al. 2013).

The conversion factor has been obtained in various ways by comparisons of CO luminosity with virial mass (e.g., Solomon et al. 1987; Scoville et al. 1987), visual or infrared extinction (e.g., Frerking et al. 1982; Lombardi et al. 2006; Pineda et al. 2008; Lee et al. 2018), X-ray absorption (e.g., Sofue & Kataoka 2016), the brightness of gamma-ray (e.g., Strong et al. 1988; Abdo et al. 2010; Planck Collaboration et al. 2015; Hayashi et al. 2019), and dust emission (e.g., Planck Collaboration et al. 2011; Fukui et al. 2014; Okamoto et al. 2017; Hayashi et al. 2019). The values have been discussed in the Milky Way and Local Group galaxies, and

the dependence on the metallicity has been suggested (e.g., Wilson 1995; Arimoto et al. 1996; Sakamoto 1996; Dame et al. 2001; Mizuno et al. 2001; Rosolowsky et al. 2003; Fukui & Kawamura 2010; Liszt et al. 2010; Leroy et al. 2011; Lee et al. 2014; Lin et al. 2016; Muraoka et al. 2017; Pitts & Barnes 2021; Ohno et al. 2023). The often used value currently in the Milky Way is $X_{\text{CO}} = 2.0 \times 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$, having uncertainty of $\pm 30\%$ (Bolatto et al. 2013).

Recently, Sofue & Kohno (2020) (hereafter paper I) proposed a new method to estimate the molecular cloud mass considering the variability of the X_{CO} factor from the correlation between ¹²CO and ¹³CO. Paper I analyzed only two Galactic GMCs of M16 (Sofue 2020b; Nishimura et al. 2021) and W43 (Sofue et al. 2019; Sofue 2021; Kohno et al. 2021), and the spatial distributions of X_{CO} inside the GMCs have not been discussed yet.

In this paper, we extend the analysis of Paper I, aiming at revealing the variability of X_{CO} within the molecular cloud of scales ($\sim 10-50$ pc) at sub-pc resolutions ($\sim 20''$). The target GMCs are W51A (Fujita et al. 2021), W33 (Kohno et al. 2018), W49 (Miyawaki et al. 2022), N35-N36 complex (Torii et al. 2018; Sofue 2019a,b), M17SW (Nishimura et al. 2018; Sofue 2020a, 2022), G012.02-00.03 (Sanna et al. 2014), W43 (Sofue et al. 2019; Kohno et al. 2021), and M16 (Sofue 2020b; Nishimura et al. 2021). These GMCs are also known as the massive star-forming regions in the Milky Way. The basic parameters of these GMCs were summarized in Table 1.

This paper is structured as follows: section 2 introduces the FUGIN (FOREST Unbiased Galactic plane Imaging survey with

* E-mail: mikito.kohno@gmail.com, kohno@nagoya-p.jp

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the Nobeyama 45-m telescope) data; section 3 presents the methods of analysis; in section 4, we demonstrate the results; in section 5, we discuss the variability of the X_{CO} factor, and in section 6, we summarize the results.

2 DATA

We utilized the ^{12}CO , ^{13}CO $J = 1-0$ line data obtained with the Nobeyama 45 m telescope (FUGIN: Umemoto et al. 2017; Torii et al. 2019; Fujita et al. 2023). The front end was the FOOr beam REceiver System on the 45-m Telescope (FOREST: Minamidani et al. 2016; Nakajima et al. 2019), which is the four-beam, side-band separating (2SB), and dual-polarization superconductor–insulator–superconductor (SIS) receiver. The observations were carried out in the on-the-fly mapping mode (Sawada et al. 2008). The back-end system used an FX-type spectrometer named SAM 45 (Kuno et al. 2011; Kamazaki et al. 2012). The data were calibrated to the main-beam temperature by measuring the main-beam efficiency of 0.43 for ^{12}CO , 0.45 for ^{13}CO , and C^{18}O using the standard calibration sources. The detailed information on the FUGIN project was summarized in the project overview paper by Umemoto et al. (2017). The cube data calibrated to the main-beam temperature is opened at the Japanese Virtual Observatory (JVO). The root-mean-square noise level of each GMC was presented in Table 1.

3 METHODS

We derive the H_2 column density per velocity channel by the local thermal equilibrium (LTE) method using the X_{CO} factor as based in Paper I and Pineda et al. (2008). The brightness temperature (T_B) of CO line intensity with the excitation temperature (T_{ex}) and optical depth (τ) is given by

$$T_B = T_0 \left(\frac{1}{e^{T_0/T_{\text{ex}}} - 1} - \frac{1}{e^{T_0/T_{\text{bg}}} - 1} \right) (1 - e^{-\tau}) \quad [\text{K}], \quad (2)$$

where $T_{\text{bg}} = 2.725$ K is the temperature of the cosmic-microwave background radiation. $T_0 = h\nu/k$ is the Planck temperature with h , ν , and k being the Planck constant, rest frequency, and Boltzman constant, respectively. If we assume the ^{12}CO line is optically thick, the excitation temperature is given by

$$T_{\text{ex}} = T_0^{115} \left/ \ln \left(1 + \frac{T_0^{115}}{T_B(\text{^{12}CO})_{\text{max}} + 0.83632} \right) \right. \quad [\text{K}], \quad (3)$$

where $T_B(\text{^{12}CO})_{\text{max}}$ and $T_0^{115} = 5.53194$ correspond to the ^{12}CO peak intensity and the Planck temperature at the rest frequency of ^{12}CO $J = 1-0$, respectively. We assume that T_{ex} is equal in the ^{12}CO and ^{13}CO line emissions, and express the optical depth as

$$\tau(\text{^{13}CO}) = -\ln \left(1 - \frac{T_B(\text{^{13}CO})_{\text{max}}/T_0^{110}}{(e^{T_0^{110}/T_{\text{ex}}} - 1)^{-1} - 0.167667} \right), \quad (4)$$

where $T_B(\text{^{13}CO})_{\text{max}}$ and $T_0^{110} = 5.28864$ represent the ^{13}CO peak intensity and the Planck temperature at the rest frequency of ^{13}CO $J = 1-0$, respectively. The ^{13}CO column density is given by

$$N_{\text{^{13}CO}} = 3.0 \times 10^{14} \frac{\tau}{1 - e^{-\tau}} \frac{1}{1 - e^{-T_0^{110}/T_{\text{ex}}}} I_{\text{^{13}CO}} \quad [\text{cm}^{-2}], \quad (5)$$

where $I_{\text{^{13}CO}}$ is the ^{13}CO integrated intensity. Then, we convert $N_{\text{^{13}CO}}$ to the H_2 column density using the abundance ratio of H_2 to ^{13}CO molecules given by

$$N_{\text{H}_2}(\text{^{13}CO}) = Y_{\text{^{13}CO}} N_{\text{^{13}CO}} \quad [\text{cm}^{-2}]. \quad (6)$$

Here, $Y_{\text{^{13}CO}}$ is adopted as $(5.0 \pm 2.5) \times 10^5$ (Dickman 1978) following Paper I.

We, then, calculate the H_2 column density per velocity channel, which is defined as the spectral column density, using the LTE method for X_{CO} from the intensity of ^{12}CO and ^{13}CO as in Paper I. The spectral column densities (SCD) of ^{12}CO and ^{13}CO are expressed as

$$\text{SCD}_{12X} = \frac{dN_{\text{H}_2}(\text{^{12}CO})}{dv} = X_{\text{CO}} T_B(\text{^{12}CO}) \quad [\text{cm}^{-2}(\text{km s}^{-1})^{-1}], \quad (7)$$

and

$$\begin{aligned} \text{SCD}_{13L} &= \frac{dN_{\text{H}_2}(\text{^{13}CO})}{dv} \\ &= 3.0 \times 10^{14} \frac{\tau}{1 - e^{-\tau}} \frac{Y_{\text{^{13}CO}} T_B(\text{^{13}CO})}{1 - e^{-T_0^{110}/T_{\text{ex}}}} \quad [\text{cm}^{-2}(\text{km s}^{-1})^{-1}]. \end{aligned} \quad (8)$$

Here, SCD_{12X} and SCD_{13L} are spectral column densities of H_2 at the peak velocity channels, derived from the X_{CO} factor and the LTE assumption, respectively.

4 RESULTS

Figure 1(a-h) shows thus obtained ^{12}CO $J = 1-0$ peak intensity maps of W51A, W33, N35-N36 complex, W49, M17SW, G012.02-00.03, W43 and M16 GMC. W49 and G012.02-00.03 GMC show compact CO distribution of ~ 20 pc, while W33, N35-N36 complex, W43, and M16 have more diffuse distribution of molecular gas at 15-20 K, 10-15 K, 15-18 K, and 10-20 K of the brightness temperature, respectively.

Figure 2(a-h) presents scatter plots between SCD_{12X} and SCD_{13L} of GMCs presented in Figure 1(a-h). Black dotted lines show the linear relation of $\text{SCD}_{12X} = \text{SCD}_{13L}$. SCD_{12X} shows saturation at high SCD_{13L} , and the nonlinear relation of each GMC has different saturation levels. The nonlinear relation between the ^{12}CO and ^{13}CO intensity are consistent with the previous studies on the Perseus molecular clouds (Pineda et al. 2008) and the CO $J = 2-1$ Galactic plane survey (Yoda et al. 2010). Then, we performed curve fitting to the scatter plots between SCD_{12X} and SCD_{13L} using the free parameters of α and SCD_c (spectral column density coefficient), as in Paper I. SCD_{12X} is given by

$$\text{SCD}_{12X} = \text{SCD}_c \left(\frac{\text{SCD}_{13L}}{\text{SCD}_c} \right)^\alpha. \quad (9)$$

The blue curves show the fitting results of individual GMCs. The fitting parameters have the range of $\alpha = 0.29-0.60$ and $\text{SCD}_c = (1.2-4.8) \times 10^{21} \text{ cm}^{-2} (\text{km s}^{-1})^{-1}$.

5 DISCUSSION

5.1 Spatial distributions of X_{CO} in the Galactic GMCs

We obtained the X_{CO} factor of each GMC from the correlation between SCD_{12X} and SCD_{13L} . The X_{CO} factor at each pixel of

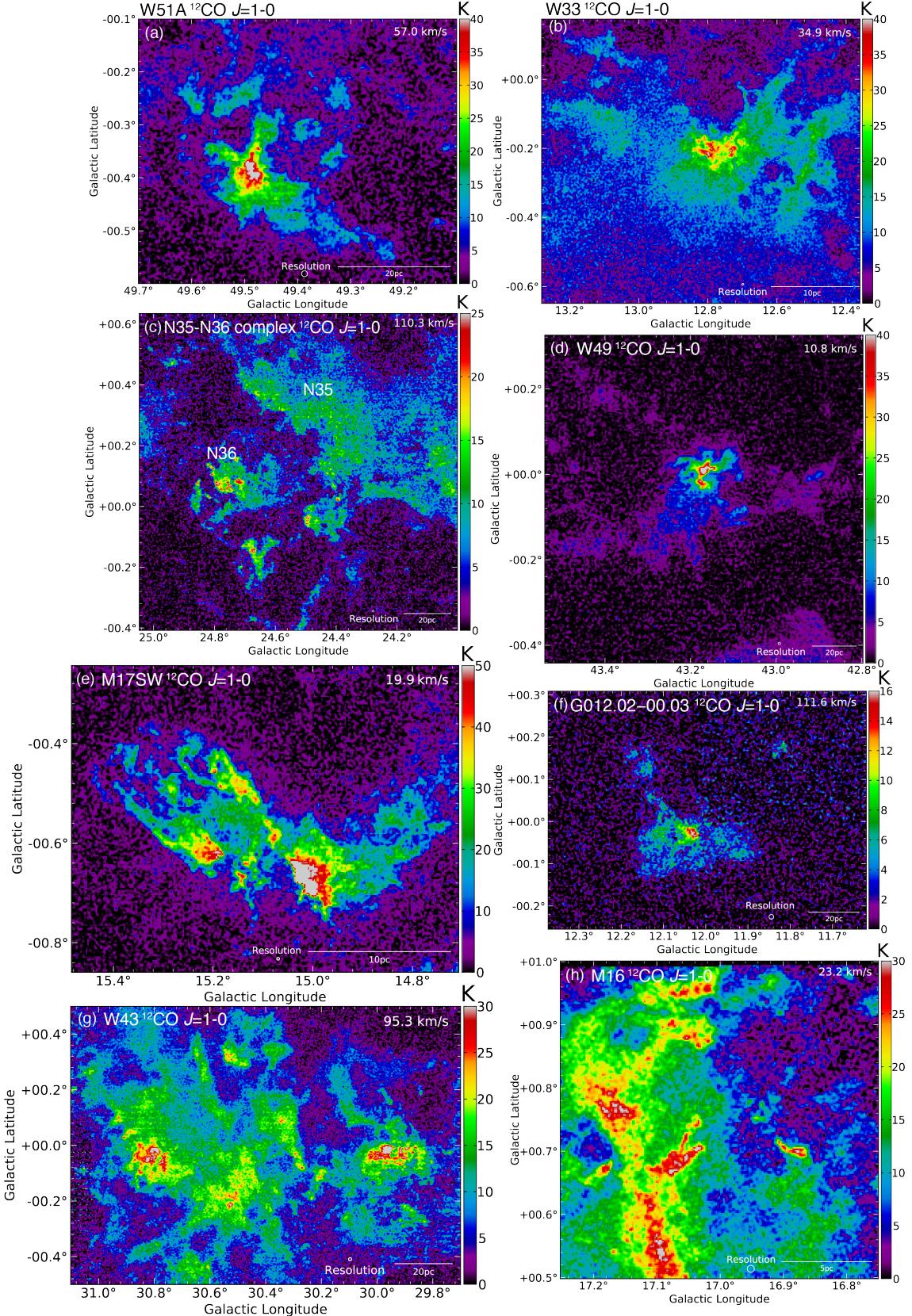


Figure 1. The ^{12}CO peak intensity map of (a) W51A at the radial velocity of 57.0 km s^{-1} , (b) W33 at 34.9 km s^{-1} , (c) N35-N36 complex at 110.3 km s^{-1} , (d) W49 at 10.8 km s^{-1} , (e) M17SW at 19.9 km s^{-1} , (f) G012.02-00.03 at 111.6 km s^{-1} , (g) W43 at 95.3 km s^{-1} , and (h) M16 at 23.2 km s^{-1} .

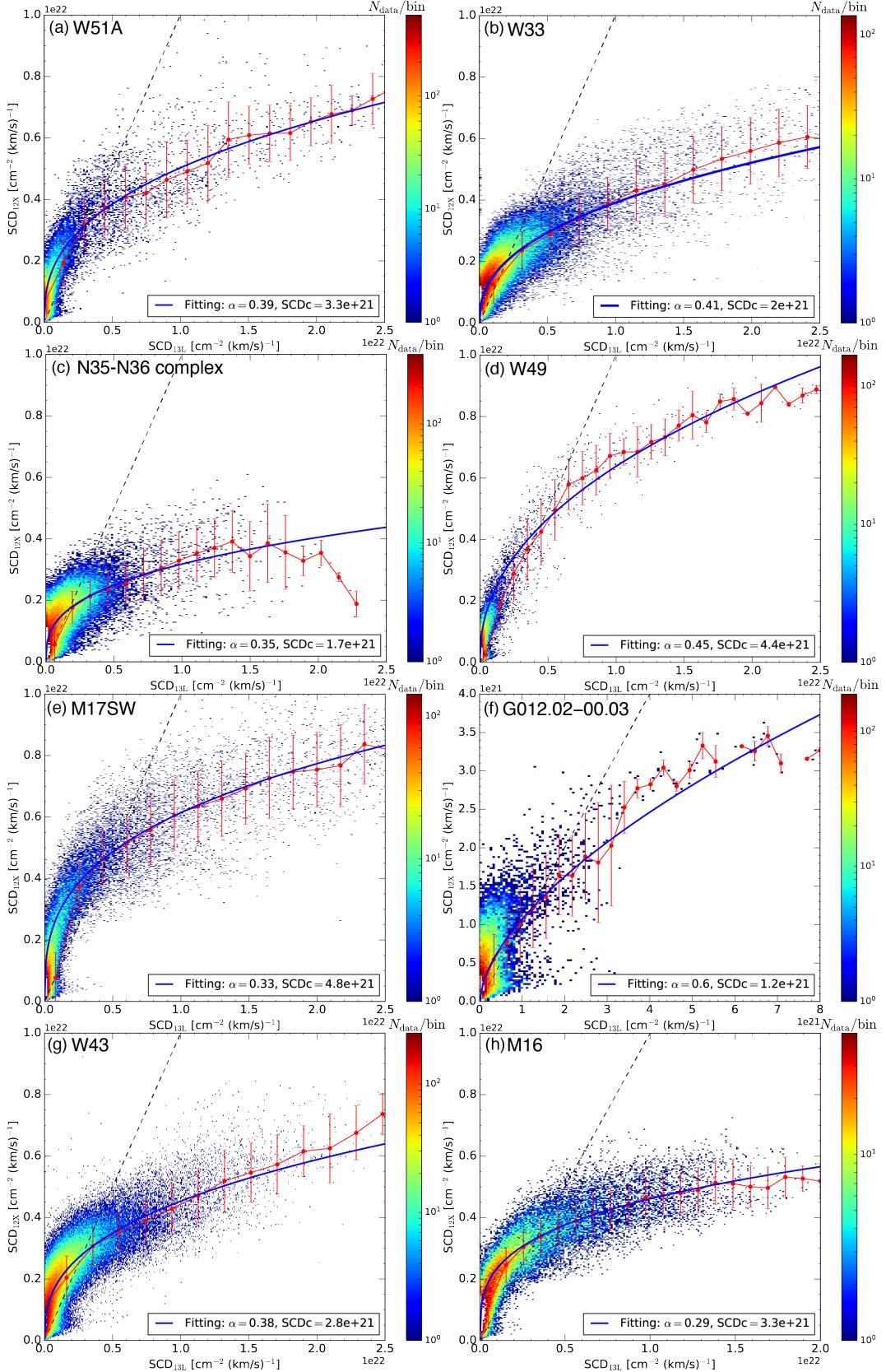


Figure 2. Scatter plot between SCD_{13L} and SCD_{12X} of (a) W51A, (b) W33, (c) the N35-N36 complex, (d) W49, (e) M17SW, (f) G012.02-00.03, (g) W43, and (h) M16. Red points show the averaged values of each bin, and the error bars are standard deviations of SCD_{12X} . Blue curves indicate the fitting results of scatter plots. The black dashed lines indicate the linear relation of $\text{SCD}_{12X} = \text{SCD}_{13L}$.

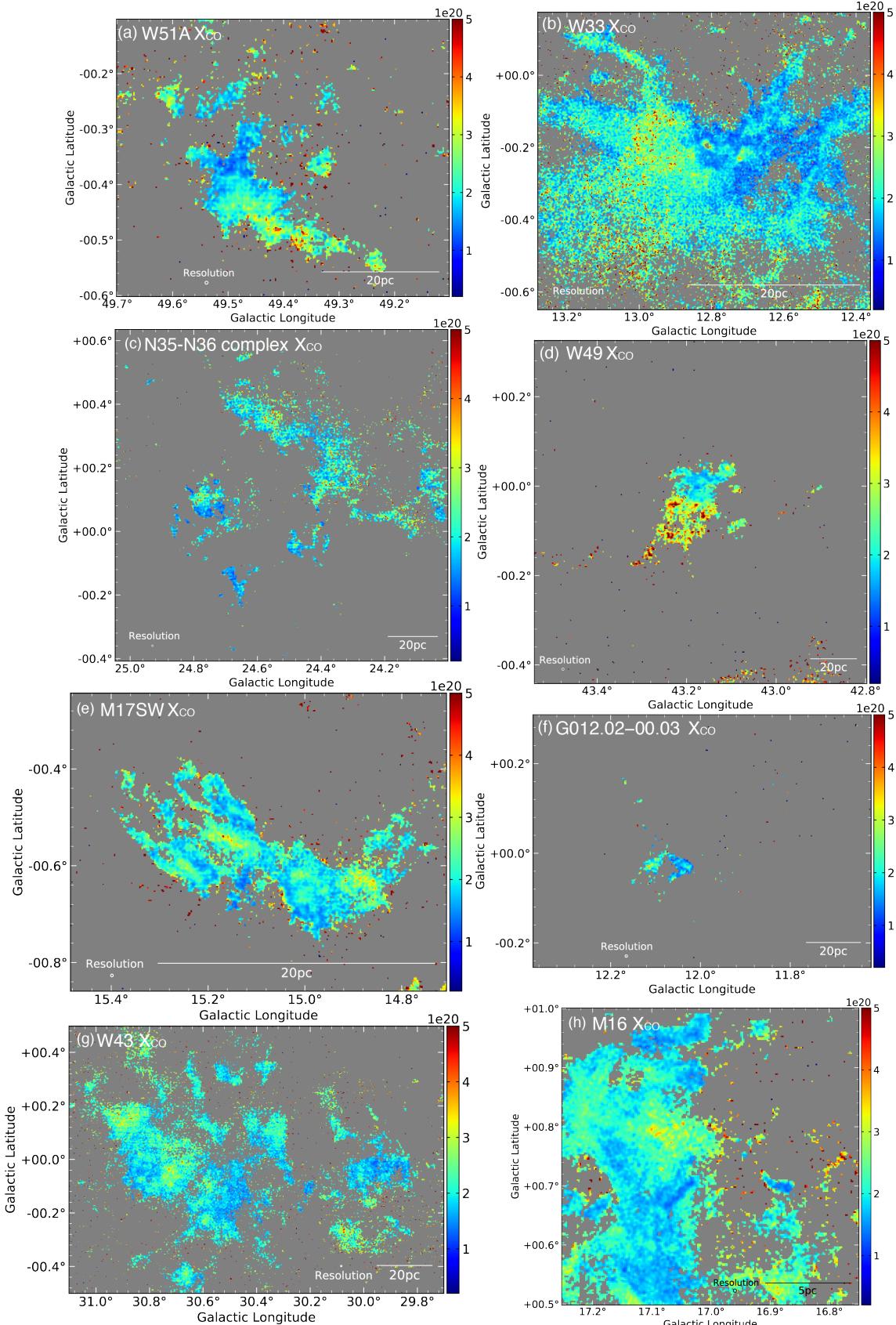


Figure 3. Spatial distributions of the X_{CO} factor in (a) W51A, (b) W33, (c) the N35-N36 complex, (d) W49, (e) M17SW, (f) G012.02-00.03, (g) W43, and (h) M16. The points are plotted of T_B (^{13}CO) $> 3\sigma$. The 1σ noise level of each GMC is presented in Table 1.

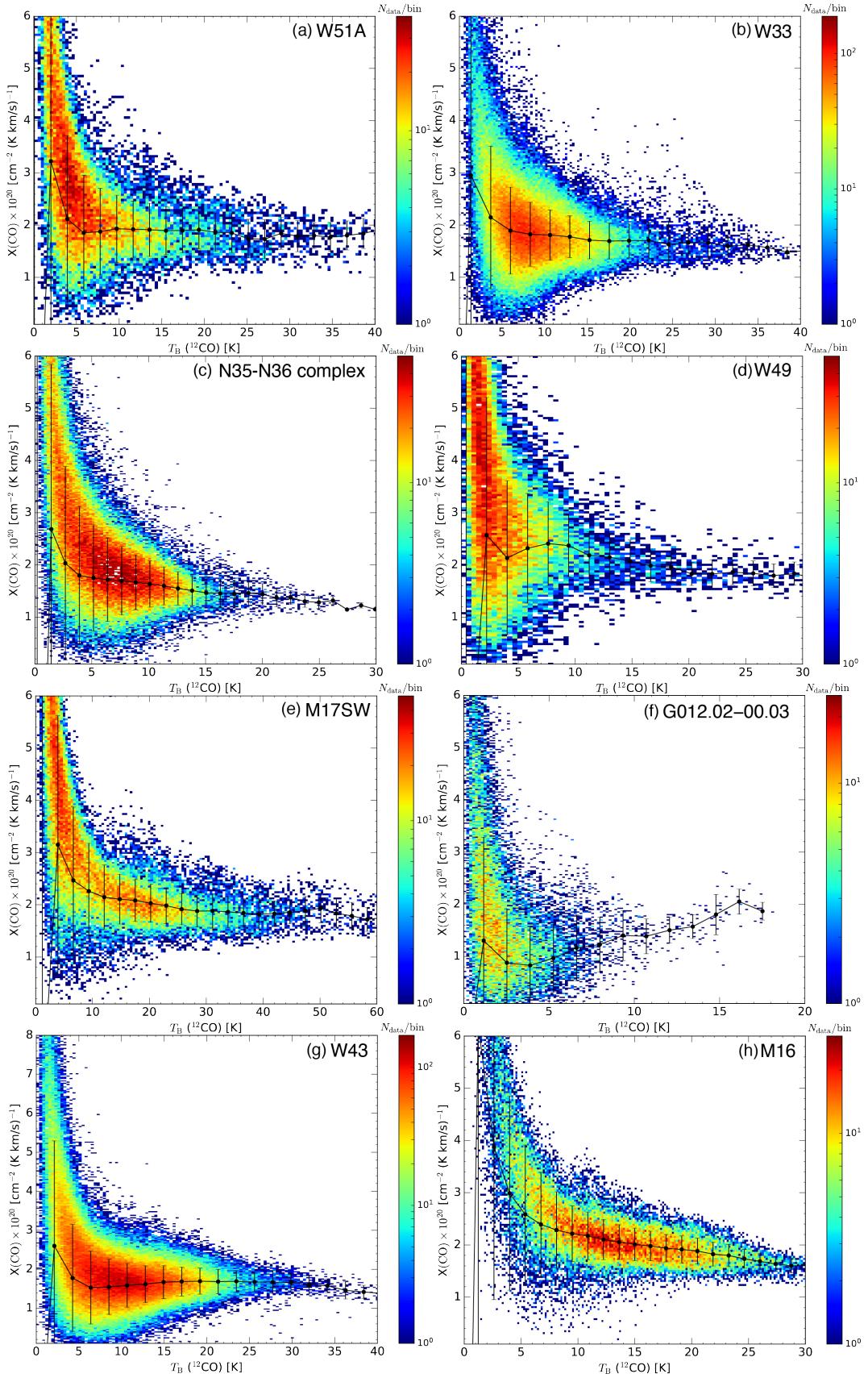


Figure 4. Scatter plot between the X_{CO} factor and T_B (^{12}CO) in (a) W51A, (b) W33, (c) the N35-N36 complex, (d) W49, (e) M17SW, (f) G012.02-00.03, (g) W43, and (h) M16. Black points show the averaged values of each bin, and the error bars are standard deviations of the X_{CO} factor.

Table 1. Properties of the Galactic massive star forming regions

Name (1)	<i>l</i> [deg] (2)	<i>b</i> [deg] (3)	<i>V</i> _{LSR} [km s ⁻¹] (4)	<i>D</i> [kpc] (5)	<i>R</i> _G [kpc] (6)	<i>T</i> _{rms} (¹³ CO) [K] (7)	Reference (8)
W51A	49.5	-0.4	57	5.4	6.1	~ 0.6	[1]
W33	12.8	-0.2	35	2.4	5.7	~ 0.6	[2]
N35-N36 complex	24.5	0.1	110	7.3	3.3	~ 1.1	[3,4]
W49A	43.16	0.0	11	11	7.5	~ 0.5	[5]
M17SW	15.0	-0.7	20	2.0	6.1	~ 0.7	[6,7,8]
G012.02-00.03	12.02	-0.03	112	9.4	2.3	~ 0.7	[9]
W43	30.8	0.0	95	5.5	4.3	~ 0.9	[10,11]
M16	17.1	0.7	23	2.0	6.1	~ 0.7	[12,13]

Columns: (1) Name. (2) Galactic longitude (3) Galactic latitude (4) Radial velocity (5) Distance from the solar system (6) Distance from the Galactic center. The Galactic distance from the Sun is assumed to be $R_0 = 8.0$ kpc obtained by the mean value of the very long baseline interferometry astrometry results (VERA Collaboration et al. 2020; Reid et al. 2019). (7) r.m.s noise reveals of the ¹³CO data (8) References [1] Fujita et al. (2021) [2] Kohno et al. (2018) [3] Torii et al. (2018) [4] Sofue (2019a) [5] Miyawaki et al. (2022) [6] Nishimura et al. (2018) [7] Sofue (2020a) [8] Yamagishi et al. (2016) [9] Sanna et al. (2014) [10] Sofue et al. (2019) [11] Kohno et al. (2021) [12] Sofue (2020b) [13] Nishimura et al. (2021)

molecular clouds is expressed as

$$X_{\text{CO}} = \text{SCD}_c \left(\frac{\text{SCD}_{13L}}{\text{SCD}_c} \right)^\alpha / T_B(^{12}\text{CO}) [\text{cm}^{-2}(\text{K km s}^{-1})^{-1}]. \quad (10)$$

where α and SCD_c are the fitting parameters obtained in Figure 2.

Figure 3(a-h) shows the X_{CO} maps of each GMC. X_{CO} has a variability with the range of $(0.9\text{--}5.0) \times 10^{20} [\text{cm}^{-2}(\text{K km s}^{-1})^{-1}]$ in a GMC. Comparing Figure 1 and Figure 3, we find an anti-correlation between the ¹²CO peak intensity and X_{CO} . Figure 4 shows the scatter plot between the X_{CO} factor and $T_B(^{12}\text{CO})$ in each GMC. The X_{CO} factor monotonically decreases with increasing brightness temperature except for G012.02-00.03. It also shows a lower limit around $X_{\text{CO}} \sim 2 \times 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$ above $T(^{12}\text{CO}) > 20$ K. These results may correspond to the saturation of ¹²CO intensity in dense cores of the GMC. It is consistent with previous studies of the Perseus molecular clouds obtained by the correlation between the ¹²CO integrated intensity and H_I column number density derived from the optical depth of 353 GHz dust emission (τ_{353}) by the Planck satellite observations (see Figure 12 and 15 in Okamoto et al. 2017).

Table 2 lists the results of parameter fitting for α , SCD_c , X_{CO} , and correlation coefficient. The mean value of X_{CO} of all GMCs in this paper is $(2.16 \pm 0.30) \times 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$. In our study, X_{CO} shows the local variability in the Galactic GMCs (Figure 3), while the mean value is consistent within errors previous works reported $2 \times 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$ (Bolatto et al. 2013), $(1.8 \pm 0.3) \times 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$ (Dame et al. 2001), and $(2.54 \pm 0.13) \times 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$ (Planck Collaboration et al. 2011).

5.2 Radial gradient of the X_{CO} factor

Finally, we investigated the radial gradient of the X_{CO} factor in the Galactic disc. The averaged X_{CO} factor has a high value in W49 at Galactocentric distance $R = 7.5$ kpc, while G012.02-00.03 has a low value at $R = 2.3$ kpc. According to Arimoto et al. (1996), the X_{CO} factor increases with the Galactocentric radius by an exponential function given by

$$\log_{10} \left(\frac{X_{\text{CO}}}{X_0} \right) = 0.41 \frac{(R - R_0)}{r_e}, \quad (11)$$

Table 2. Fitting results and $\langle X_{\text{CO}} \rangle$ taken from the correlation of SCD_{12X} and SCD_{13L} .

Name (1)	α (2)	SCD_c [$\times 10^{21}$] (3)	$\langle X(\text{CO}) \rangle$ [$\times 10^{20}$] (4)	C.C. (5)
W51A	0.39	3.3	2.23	0.76
W33	0.41	2.0	2.14	0.74
N35-N36	0.35	1.7	2.13	0.71
W49	0.45	4.4	2.68	0.78
M17 SW	0.33	4.8	2.23	0.74
G012.02-00.03	0.60	1.2	1.59	0.62
W43	0.38	2.8	2.10	0.76
M16	0.29	3.3	2.15	0.81
Average	0.40 ± 0.09	2.94 ± 1.27	2.16 ± 0.30	0.74 ± 0.06

Columns: (1) GMC names (2) The fitting parameter of the non-linear relation. (3) The coefficient of the spectrum column density (SCD_c). (4) The mean value of the X_{CO} factor in a GMC. (5) Correlation coefficient. The errors of averaged value are adopted as the standard variation in all GMCs.

where $r_e = 6.2$ kpc is the scale radius of Galactic disc and X_0 is X_{CO} at $R = R_0 = 8.0$ kpc (VERA Collaboration et al. 2020; Reid et al. 2019). This equation can be deformed as follows.

$$X_{\text{CO}} = 0.59 \times 10^{20} \exp \left(\frac{R}{6.567 \text{ [kpc]}} \right) [\text{cm}^{-2}(\text{K km s}^{-1})^{-1}] \quad (12)$$

Figure 5 shows a plot of the X_{CO} factor obtained in this paper as a function of the Galactocentric distance. It is found that X_{CO} increases with the distance from the Galactic Centre, and the plot may be fitted by an exponential function by

$$X_{\text{CO}} = 1.48 \times 10^{20} \exp \left(\frac{R}{14.07 \text{ [kpc]}} \right) [\text{cm}^{-2}(\text{K km s}^{-1})^{-1}]. \quad (13)$$

Our fitting result yields a significantly larger X_{CO} at the Galactic Centre by a factor of 3 compared to that by Arimoto et al. (1996) indicated by the green dotted line. This discrepancy may be caused by no data point within $R < 2$ kpc in our study as well as by the normalization of the local value to $2 \times 10^{20} [\text{H}_2 \text{ cm}^{-2}(\text{K km s}^{-1})^{-1}]$

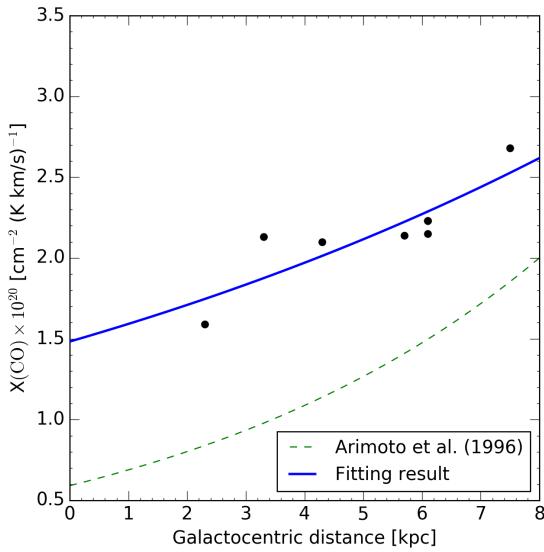


Figure 5. The X_{CO} gradient from the distance of the Galactic Center. The blue line shows the fitting result adopted by the exponential function.

The green dashed line indicates the relation from Arimoto et al. (1996).

at 8 kpc in the previous study. Sodroski et al. (1995) reported that the X_{CO} factor within 400 pc in the Galactic Centre region is by a factor 3–10 lower than the Galactic disk. Therefore, the value of X_{CO} in the Galactic Centre is still controversial. The present method applied to the ^{12}CO and ^{13}CO $J = 1-0$ line data in the Galactic Centre region would provide with a more precise determination of X_{CO} in the innermost Milky Way. A detailed analysis of this point will be presented in a separate paper using the CO survey data of the Galactic Centre (e.g., Oka et al. 1998; Torii et al. 2010; Tokuyama et al. 2019).

6 SUMMARY

The conclusions of this paper are summarized as follows:

- (i) We studied the correlation between ^{12}CO and ^{13}CO intensities toward the Galactic GMCs W51A, W33, N35-N36 complex, W49, M17SW, G12.02-00.03, W43, and M16 using the FUGIN CO survey data taken with the Nobeyama 45 m telescope.
- (ii) All the GMCs show intensity saturation of the ^{12}CO line in regions with high brightness of ^{13}CO .
- (iii) We also presented high-resolution X_{CO} factor maps made from the correlations of the CO isotopologues, which revealed local variability of the factor in each GMC. We also showed that the X_{CO} factor monotonically decreases with increasing ^{12}CO brightness temperature.
- (iv) The averaged value of all GMCs is calculated to be $X_{\text{CO}} = (2.16 \pm 0.30) \times 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$, which is consistent within the error with the reported values in the previous review.
- (v) We showed that the X_{CO} increases with the Galactocentric distance in accordance with the previous works, while suggesting a smaller value in the GC by a factor of 3.

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Data availability The data underlying this article are available in <http://nro-fugin.github.io>. The FUGIN CO data were retrieved from the JVO portal <http://jvo.nao.ac.jp/portal> operated by ADC/NAOJ.

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