

Article

# Dark Supernova Remnants revealed by CO-line Bubbles in the W43 Molecular Complex along the 4-kpc Galactic Arm

Yoshiaki SOFUE

Institute of Astronomy, The University of Tokyo, 2-21-1 Mitaka, Tokyo 181-8588, Japan ;  
sofue@ioa.s.u-tokyo.ac.jp

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**Abstract:** Fine structure of the density distribution in giant molecular clouds (GMC) around W43 (G31+00+90 km s<sup>-1</sup> at ~ 5.5 kpc) was analyzed using the FUGIN\* CO-line survey at high-angular (20'' ~ 0.5 pc) and velocity (1.3 km s<sup>-1</sup>) resolutions (\*Four-receiver-system Unbiased Galactic Imaging survey with the Nobeyama 45-m telescope). The GMCs show highly turbulent structures, and the eddies are found to exhibit spherical bubble morphology appearing in narrow ranges of velocity channels. The bubbles are dark in radio continuum emission, unlike usual supernova remnants (SNR) or HII regions, and in infrared dust emission, unlike molecular bubbles around young stellar objects. The CO bubbles are interpreted as due to fully evolved buried SNRs in molecular clouds after rapid exhaustion of the released energy in dense molecular clouds. Then, the CO bubbles may be a direct evidence for exciting and maintaining the turbulence in GMCs by SN origin. Search for CO bubbles as "dark SNRs" (dSNR) will have implication to estimate the supernova rate more accurately, and hence the star formation activity in the Milky Way.

**Keywords:** galaxies: individual (Milky Way) ; ISM: CO line; ISM: molecular clouds; ISM: supernova remnant

## 1. Introduction

Galactic supernova remnants (SNRs) are observed as extended objects bright in radio, X-ray, and/or optical emissions, often exhibiting shell structures expanding at high velocities [1–3]. About 300 Galactic SNRs are currently catalogued in the Milky Way [4,5]. Their feedback to the ISM via interaction with the ambient molecular clouds has crucial implication to the interstellar physics such as the origin of interstellar turbulence, star formation, and cosmic ray acceleration [6–10].

Although most of radio SNRs are supposed to be catalogued for the transparency of the Galactic disc in radio, a larger number of SNRs is predicted from the estimated supernova rate of  $0.02 \pm 0.01$  SNe y<sup>-1</sup> [11–16], suggesting 200 to 2000 SNRs in the Galaxy for supposed life time of a SNR of 10<sup>4–5</sup> y. Since remnants of core collapse SNe are expected to be located near to their birth places because of the short lifetime of high-mass progenitors, it is expected that their distribution is tightly correlated with that of HII regions. However, only a weak concentration has been found in the spiral arms for the known SNRs [17]. In order to uncover missing SNRs, an extensive survey has been obtained by radio continuum observations, and a large number of candidate SNRs have been detected [18]. However, their longitudinal distribution does not indicate a clear correlation with that of HII regions.

From these statistics we may expect that there exist a larger number of uncovered SNRs that are not detected in the current observations in radio or in other wave lengths. A possible way of existence of such uncovered SNRs would be buried SNRs in molecular clouds (MC). Supernovae (SNe) exploded in dense gas of MCs evolve in a quite different way from that exploded in the low-density inter cloud

space. They evolve rapidly in a short lifetime of  $\sim 10^2$  y reaching a small radius of a few pc after peaky infrared flash [3,19–21]. Hence, their direct detection is difficult for the short time scale and compactness, so that no observational evidence has been obtained yet of the buried SNRs.

In spite of the short flashing phase, the molecular cavity left after the buried SNR can survive for much longer time, which would be detectable as a cavity or a bubble of molecular gas. We recently reported the discovery of an almost perfect round-shaped cavity with a clear-cut boundary in a medium sized molecular cloud at G35.75-0.25+28 in the  $^{12}\text{CO}$  ( $J = 1 - 0$ ) line emission  $\text{km s}^{-1}$  [22]. The cavity is quiet in radio emission, unlike usual SNRs or HII regions. It is also quiet in infrared emissions, unlike Spitzer bubbles associated with molecular shells around young stellar objects (YSO) [23,24]. The peculiar property of the molecular cavity G35.75 was understood as due to a relic of a fully evolved supernova remnant (SNR) in the cloud, which may be the first evidence for the existence of a buried SNR in the Galactic disc. We called the molecular cavity a "dark SNR" (dSNR).

In this paper, we extend the search for dSNRs in the form of molecular bubbles and/or cavities in the giant molecular clouds (GMC) surrounding the active star-forming region, W43 Main (G31+00+90  $\text{km s}^{-1}$ ), in the tangential direction of the 4-kpc molecular arm. The molecular gas properties and star formation in the W43 region have recently been extensively studied using the FUGIN CO line data [25,26]. We adopt a distance of 5.5 kpc according to the literature, which is close to the near-side kinematical distance of  $5.56 \pm 0.46$  kpc at  $v_{\text{lsr}} = 93$   $\text{km s}^{-1}$  (center velocity of W43) for the most recent rotation curve of the Galaxy [27].

We make use of the FUGIN (Four-receiver Unbiased Galactic Imaging survey with the Nobeyama 45-m telescope) survey data in the  $^{12}\text{CO}$ ,  $^{13}\text{CO}$ , and  $\text{C}^{18}\text{O}$  line emissions [28]. The data are available at the URL of FUGIN, <http://nro-fugin.github.io>. The full beam width at half maximum of the 45-m telescope was  $15''$  at the  $^{12}\text{CO}$  ( $J = 1 - 0$ ) frequency and the velocity resolution was  $1.2$   $\text{km s}^{-1}$ . The effective beam size in the used 3D FITS cube is  $20''$ , rms noise level  $\sim 1$  K, and the pixel size  $(\Delta l, \Delta b, \Delta v_{\text{lsr}}) = (8''.5, 8''.5, 0.65$   $\text{km s}^{-1})$ .

## 2. CO Bubbles

### 2.1. Positions, Sizes and Distribution

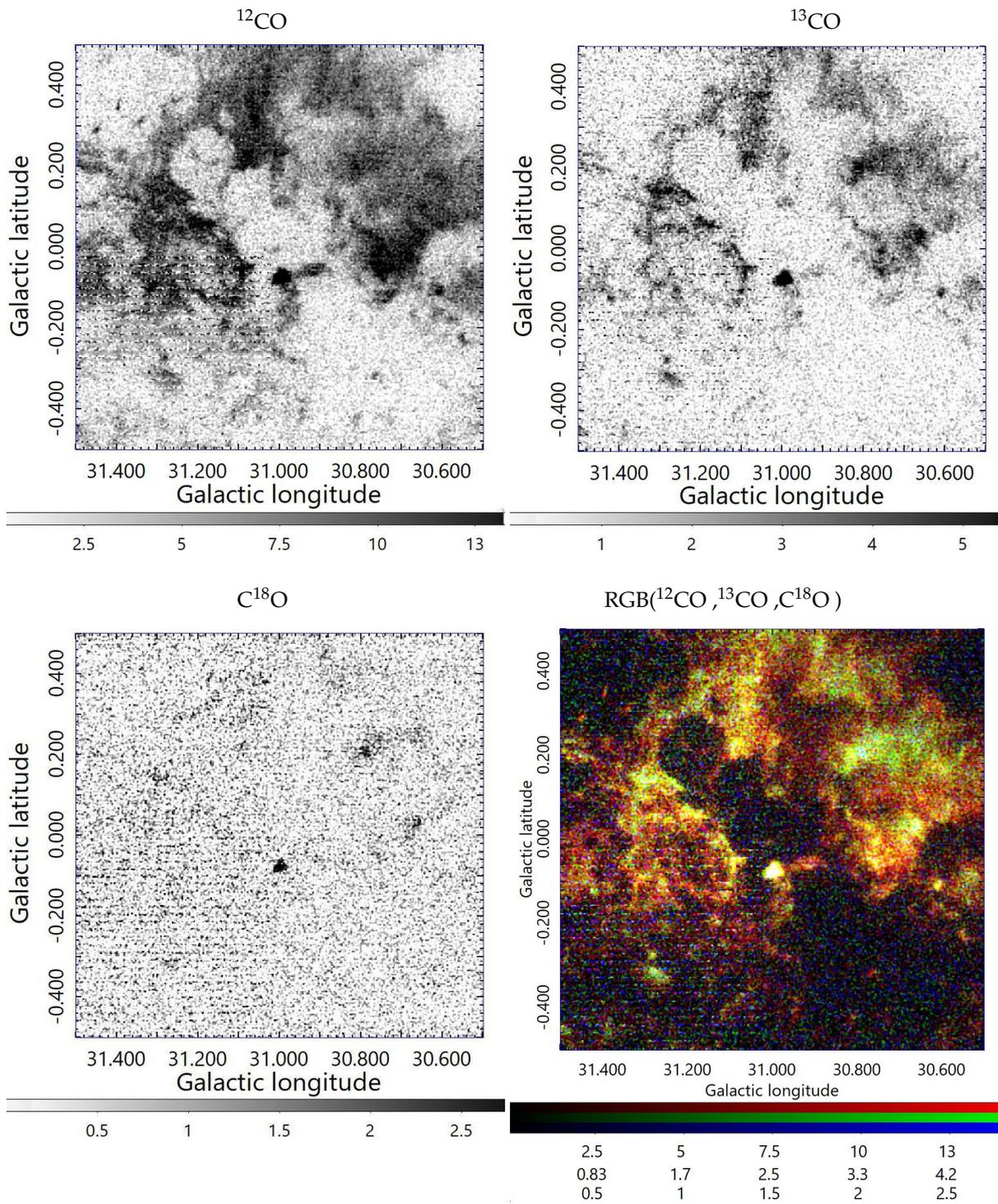
In figure A1 of the Appendix, we show channel maps of the  $^{12}\text{CO}$  -line brightness temperature in the  $2^\circ \times 2^\circ$  region around W43. Figure A2 shows the same, but extended emissions with scale sizes greater than  $3'$  ( $\sim 5$  pc) are subtracted in order to enhance shells, arcs, and/or filaments. All the channel maps exhibit numerous bubbly features (hereafter, bubbles), arcs and filaments. Bubbles and arcs show up in the channel maps more pronounced than in the integrated intensity map of the same region [26]. Each of the bubbles appears in a narrow range of velocity of a few  $\text{km s}^{-1}$ , and the diameter is typically  $\sim 0''.1$  (10 pc), ranging from  $\sim 2'$  to  $\sim 15'$  (3 to 24 pc). Arcs and filaments are generally fainter than complete bubbles, and are more extended.

Figure 1 shows typical cases from a channel map, where CO bubbles at G31.2+0.2+81 at  $v_{\text{lsr}} = 81.465$   $\text{km s}^{-1}$  are shown by a composite color-coded map of  $^{12}\text{CO}$  brightness in red ( $T_{\text{B}}$  from 0 to 15 K),  $^{13}\text{CO}$  in green (0 to 4 K), and  $\text{C}^{18}\text{O}$  in blue (0 to 2 K). Several almost empty cavities, each about  $0''.1$  in diameter, are aligned from G30.8-0.2 to G31.2+0.2, apparently in touch with each other. The surrounding molecular gas makes shell structures with enhanced density. Since there is no signature of excess in green intensity ( $^{13}\text{CO}$  line), the molecular gas is mildly compressed at the bubble edges.

Using the original channel maps of a  $2^\circ \times 2^\circ$  region around W43 taken from the FUGIN FITS cube data (<http://nro-fugin.github.io>), we identified many bubbles and arcs as shown in figure A3. Their positions, approximate radii, center velocities, and approximate velocity widths are listed in table A1.

### 2.2. Quiet in radio and far infrared

In figure A3 we plot positions and extents of extended radio continuum sources at 5.8 GHz taken from the VLA survey (GLOSTAR) [29] with a similar angular resolution ( $18''$ ) as the present CO maps.



**Figure 1.** Brightness temperature maps of the G31+00 region at 81.675 km s<sup>-1</sup> in the <sup>12</sup>CO, <sup>13</sup>CO, and C<sup>18</sup>O ( $J = 1 - 0$ ) lines, and a color-coded (RGB) map of <sup>12</sup>CO (red, 0 - 15 K), <sup>13</sup>CO (green, 0 - 5 K), and C<sup>18</sup>O (blue, 0 - 3 K).

81 Except for W43 Main associated with comparable sized shells in CO and radio continuum, there appear  
82 no clear corresponding pairs.

83 In figure 2 we enlarge the bubbles around G31.0+0.1, and compare with the radio continuum  
84 emission at 20 cm [31,32] (MAGPIS) and dust emission at  $8\ \mu\text{m}$  (GLIMPSE<sup>1</sup>). We emphasize that the  
85 bubbles are not associated with radio continuum emission, unlike usual SNRs or HII regions. Also,  
86 unlike molecular bubbles around young stellar objects (YSO), they are dark in thermal radio and  
87 infrared emissions.

88 Panel (c) of the figure shows the positions of YSOs by crosses (SIMBAD) and Spitzer bubbles  
89 by circles (showing approximate extents) [24], which are not coincident with the CO bubbles. These  
90 facts indicate that the CO bubbles are empty not only in the molecular gas, but also in warm dust,  
91 ionized thermal gas and non-thermal emitters (cosmic rays and magnetic fields). These CO bubbles  
92 are recognized only in the subsequent several channels ( $0.65\ \text{km s}^{-1}$  increment), indicating that the  
93 velocity width of each bubble is several  $\text{km s}^{-1}$ .

### 94 2.3. Kinematics

95 Figure 3 shows a close up of the bubble at  $G31.2+0.2+81.675\ \text{km s}^{-1}$ , and an averaged LV diagram  
96 across the center made from four subsequent LV diagrams. The bubble is clearly visible as an elliptical  
97 ridge in the LV diagram as marked by an ellipse of radius of  $\sim 0^\circ.075$  and half velocity width of  $\sim 7$   
98  $\text{km s}^{-1}$ . Such an elliptical LV feature can be naturally understood as due to an expanding shell of  
99 radius  $7.2\ \text{pc}$  at velocity  $7\ \text{km s}^{-1}$ . It is stressed that the thus estimated expanding velocity, which is  
100 ubiquitous in other bubbles, is greater than the velocity dispersion of a few  $\text{km s}^{-1}$  in the surrounding  
101 MC. If the bubbles are dark SNRs, or the relics of buried SNRs, such increased velocity would be a  
102 direct evidence for the acceleration of interstellar turbulence by the feedback kinetic energy of an SN  
103 explosion.

104 In the third panel of figure 3, we present a cross section of  $T_{\text{B}}$  across the bubble center. It reveals a  
105 clear-cut inner wall with the intensity maximum at the edge followed by an extended outskirts. This  
106 indicates that the bubble is a vacant cavity, and suggests that the interior gas, which had filled the  
107 cavity, is accumulated near the edge of the cavity, composing a shell structure observed as a CO bubble.  
108 Alternatively or additionally, the inner gas may have escaped from the bubble through a smaller hole  
109 or a crack in the wall. In fact, the bubble is not perfectly surrounded by the wall, but some parts are  
110 missing, being merged with the neighbouring bubbles.

### 111 2.4. Are CO bubbles ubiquitous?

112 In order to examine a wider area for the CO bubbles, we show channel maps of the  $2^\circ \times 2^\circ$  region  
113 around W43 in the Appendix, along with background-filtered images of each channel map to enhance  
114 bubbly and filamentary features. Thereby, we detected many possible bubbles as indicated in the  
115 Appendix.

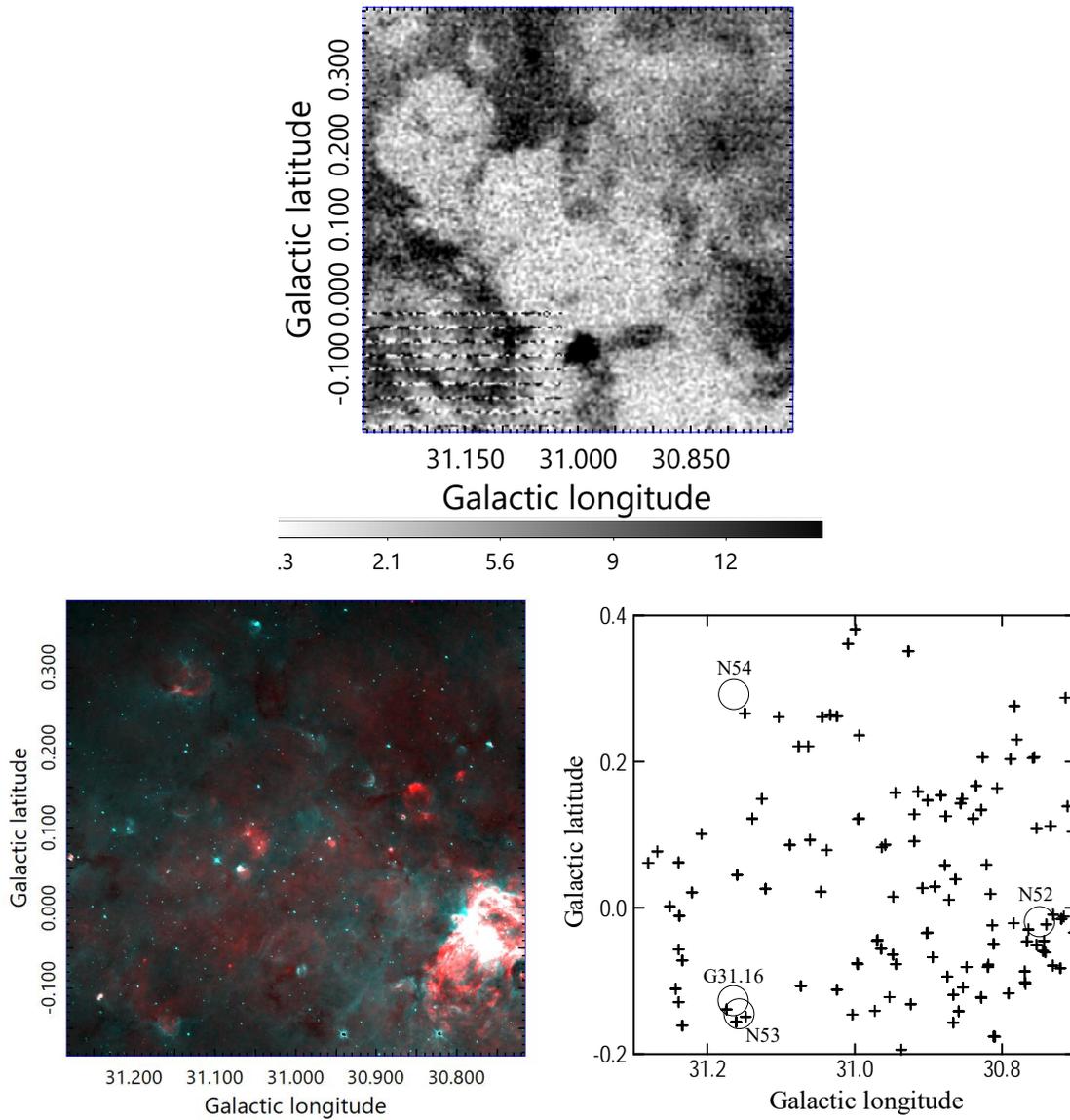
116 Although the purpose of this paper is to search for CO bubbles in the molecular complex around  
117 W43 between  $80$  and  $100\ \text{km s}^{-1}$ , it may be worthwhile to look for similar objects in different regions  
118 and velocity ranges. Figure 4 shows examples of such bubbles found at different velocities, and hence  
119 in different arms, at  $G30.4+0.4+70\ \text{km s}^{-1}$  and  $G30.45+0.36+46\ \text{km s}^{-1}$  in the same sky area as for W43.

120  $G30.4+0.4+70$  is located on the lower-velocity branch of the Scutum arm, and bubble diameters  
121 are about  $0^\circ.12$ , corresponding to  $D \sim 8.5$  or  $19.6\ \text{pc}$  for near or far distances of  $4.2 \pm 0.3$  and  $9.6 \pm 0.3$   
122 kpc, respectively. The LV behavior is not straightforward due to superposition of multiple bubbles,  
123 showing some vertical (velocity) elongations suggesting expansion at several  $\text{km s}^{-1}$ .

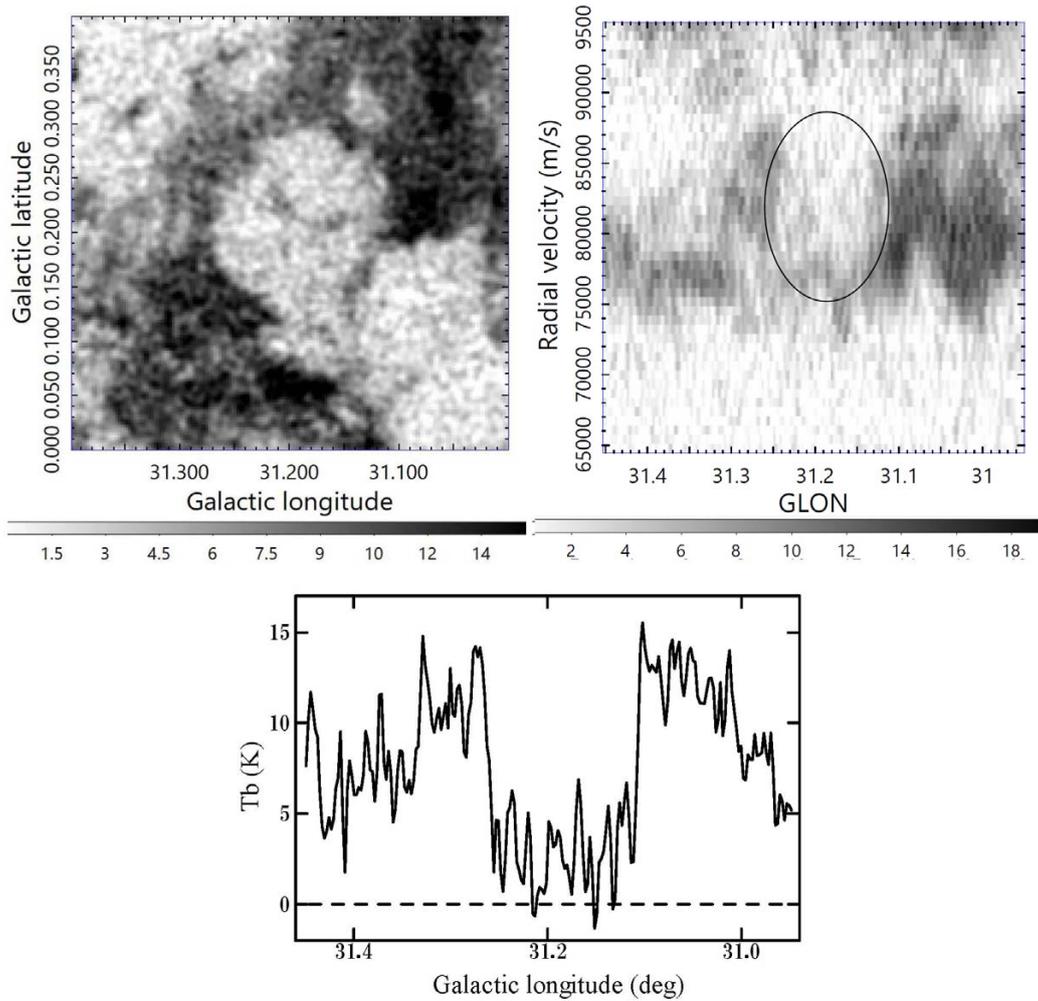
124  $G30.45+0.36+46\ \text{km s}^{-1}$  is located on the higher-velocity branch of the Sagittarius arm. The radius  
125 of  $0^\circ.12 \times 0^\circ.1$  corresponds to  $6.1$  or  $22.4\ \text{pc}$  for near and far distances of  $2.9 \pm 0.3$  and  $10.9 \pm 0.3$  kpc,

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<sup>1</sup> <http://www.spitzer.caltech.edu/glimpse360/aladin>



**Figure 2.** (Top) CO bubbles around G31+0.1 in  $^{12}\text{CO } T_{\text{B}}$  (K) at  $81.465 \text{ km s}^{-1}$ , (bottom left) 20 cm brightness in red (from 0 to 10 mJy/beam; MAGPIS) and  $8 \mu\text{m}$  brightness in blue/green (from 50 to 500 mJy/str; GLIMPSE), and (bottom right) YSO positions by crosses (SIMBAD: AGAL, 2MASS; <http://simbad.u-strasbg.fr/simbad/>) and Spitzer bubbles by circles with names.



**Figure 3.** (Top left) Molecular bubble S31.2+0.2 at  $81.465 \text{ km s}^{-1}$ . (Top right) Longitude-velocity diagram around  $b = 0^\circ.23$  across the bubble G31.2+0.2 (average of 4 channels in the latitude direction near the bubble center). The ellipse represents bubble radius  $0^\circ.074$  (7.1 pc at 5.5 kpc distance) and half velocity width  $6.7 \text{ km s}^{-1}$  centered on  $l = 31^\circ.19$ ,  $v_{\text{lsr}} = 81.9 \text{ km s}^{-1}$ . (Bottom)  $T_B$  cross section at  $81.0 \text{ km s}^{-1}$  across the bubble center at position angle of  $120^\circ$ .

126 respectively. The LV diagram shows an elliptical feature, indicating an expanding motion at several  
127  $\text{km s}^{-1}$ . If we adopt the near distances, the sizes are comparable to those obtained for W43 bubbles.

128 The present search for CO bubbles was obtained only for the limited area on the sky around  
129 G31+00. However, it is expected that similar CO bubbles would be found generally in many other  
130 molecular clouds, particularly in giant molecular clouds adjacent to star forming regions. We may,  
131 therefore, reasonably argue that the CO bubbles of the same property as found here are rather  
132 ubiquitous in the Galactic disc, particularly in molecular complexes near active star forming regions in  
133 dense spiral arms.

### 134 2.5. Mass and energy

135 It is not easy to estimate the mass of a bubble, not only because it is vacant of the gas, but  
136 also because the outer boundary of the molecular cloud is not definite for the extended outskirt.  
137 Instead, we may calculate the mass of supposed exhausted molecular gas that had filled the bubble  
138 in the past, assuming that the density was same as the ambient cloud density. The mean  $T_B$  of  
139 the surrounding gas cloud around the bubble G31.1+0.2+81 is about  $T_B \sim 10$  K, velocity width is  
140  $\delta v \sim 5 \text{ km s}^{-1}$ . The mean molecular density can be estimated to be  $n_{\text{H}_2} \sim X_{\text{CO}} T_B \delta v / r \sim 230 \text{ cm}^{-3}$ ,  
141 where  $r = 7 \text{ pc}$  is the bubble radius and  $X_{\text{CO}} \sim 2 \times 10^{20} \text{ H}_2 \text{ cm}^{-3} (\text{K km s}^{-1})^{-1}$  is the conversion  
142 factor for extended molecular clouds [32]. The total lost mass inside the bubble is then estimated as  
143  $M \sim 4\pi/3 \mu n_{\text{H}_2} m_{\text{H}} r^3 \sim 2.3 \times 10^4 M_{\odot}$ , where  $\mu = 2.8$  is the mean molecular weight and  $m_{\text{H}}$  is the  
144 hydrogen mass. If the mass had escaped from the bubble at a velocity of  $v_{\text{esc}} \sim 7 \text{ km s}^{-1}$ , the total  
145 kinetic energy of the thus lost mass is  $E_{\text{esc}} \sim 1/2 M v_{\text{esc}}^2 \sim 10^{49} \text{ erg}$ , safely supplied by the input energy  
146 by an SN explosion.

## 147 3. Discussion

### 148 3.1. More Bubbly GMCs than Filaments

149 We showed that the giant molecular clouds (GMCs) composing the W43 molecular complex are  
150 filled with CO bubbles. Such bubbly structures are particularly evident in the channel maps after  
151 subtracting the extended emission (figure A2). Thus, in so far as the W43 complex is concerned, the  
152 GMCs are generally bubbly rather than exhibiting filament structures. This makes contrast to the  
153 filamentary interstellar turbulence in the local Orion clouds [33] or to that expected from simulations  
154 [34]. Hence, as will be concluded in the next subsection, the bubbly behavior may be due to a more  
155 efficient feedback by the current SF activities in W43 associated with a larger number of SNe compared  
156 to that in the local ISM in the solar vicinity.

### 157 3.2. Origin of CO Bubbles

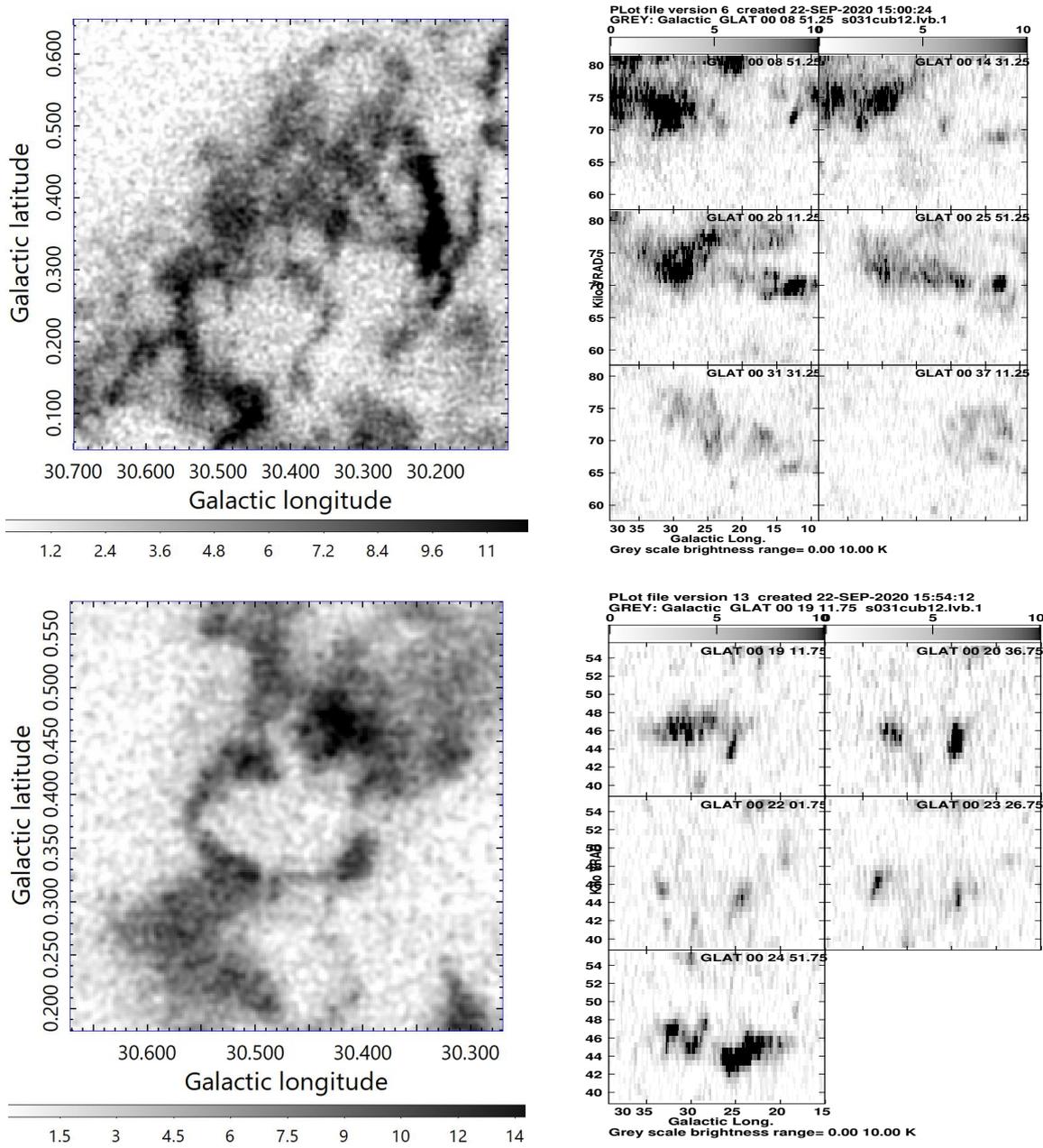
158 As to the origin of the CO bubbles, we may consider several possible mechanisms.

159 (i) The first idea is that they are fully evolved relics of buried SNRs, simply argued from the required  
160 total energy. Thereby, the shell structure is maintained by its own expanding motion, as described  
161 later.

162 (ii) The second idea is that they are evolved Spitzer bubbles. This idea encounters the difficulties, as  
163 raised in the previous section, that the bubbles are quiet in thermal radio and infrared emissions.

164 (iii) Stellar winds from young stars may also be excluded, because there is no signature of star formation  
165 inside the bubbles, as for the reasons against (ii), except for the core area of the W43 Main.

166 (iv) Outflows from old population stars such as planetary nebulae would be another possibility  
167 [37]. The responsible mass-loss stars are distributed in the population II disc at a number density  
168 approximately equal to that of AGB stars  $n_{\text{PN}} \sim t_{\text{AGB}} / t_* (M_{\text{disc}} / M_*) / (\pi r_{\text{disc}}^2 z_{\text{disc}}) \sim 10^{-6} \text{ pc}^{-3}$ , where  
169  $t_{\text{AGB}} \sim 10^3 \text{ y}$ ,  $t_* \sim 10^{10} \text{ y}$ ,  $M_{\text{disc}} \sim 10^{11} M_{\odot}$  is the Galactic disc mass,  $M_* \sim 1 M_{\odot}$ ,  $r_{\text{disc}} \sim 5 \text{ kpc}$   
170 and  $z_{\text{disc}} \sim 200 \text{ pc}$  is the disc radius and full thickness, respectively. We thus expect only one such  
171 star within  $\sim 100 \text{ pc}$  volume around W43. Moreover, the supplied energy would be too small,



**Figure 4.**  $T_B$  maps and LV diagrams of CO bubbles at different velocities in different arms : (Top) G30.4+0.4+70 km s<sup>-1</sup> and (bottom) G30.45+0.36+46 km s<sup>-1</sup>.

172  $E_{\text{PN}} \sim (1/2)v^2\dot{M}_{\text{AGB}} \sim 10^{45}$  ergs from the wind, where  $\dot{M} \sim 10^{-8}M_{\odot}\text{y}^{-1}$  is the mass-loss rate and  
 173  $v \sim 2500 \text{ km s}^{-1}$  is outflow velocity.

174 (v) Thermal instability produces a cavity, if the heating rate by cosmic rays per molecule is constant  
 175 and the cooling rate is proportional to the square of gas density [38]. A lower-density perturbation  
 176 results in a growing cavity. However, it cannot explain the observed expanding velocity of the shell at  
 177 several  $\text{km s}^{-1}$ , because the perturbation grows at the sound speed of molecular gas,  $\sim 1 \text{ km s}^{-1}$ .

178 (vi) Magnetic filaments will produce perpendicular molecular filaments [39,40]. However, in order to  
 179 make CO bubbles, the magnetic fields must be radial about the bubble centre.

180 (vii) Finally, one may attribute the bubbles to interstellar turbulence. However, this argument does not  
 181 answer the question about the origin of the CO bubbles. In fact, ideas (i) to (vi) are almost equivalent  
 182 to that about the origin of turbulence in molecular clouds.

### 183 3.3. Dark SNRs

184 From the above consideration, we here conclude that idea (i) is most plausible as the origin of  
 185 the observed CO bubbles. We here try to explain the CO bubbles by well evolved and radio quiet  
 186 SNRs, which exploded inside molecular clouds and had evolved as buried SNRs. We assume that the  
 187 responsible energy sources are mostly core-collapsed (type II) SNe, because most of the catalogued  
 188 SNRs, mainly from radio observations by their shell structures, are of type II SN origin. Type Ia SNe  
 189 would make SNRs of filled center morphology, while rarely produce shell structures. Also, kinetic  
 190 energy released by this type is not sufficient to explain the expanding kinetic energy of the CO bubbles.

191 Massive stars produce cavities in the ambient gas by the stellar winds for some My. The  
 192 wind-driven shells evolves into shocked SNRs soon after SN explosions [20,21]. By scaling the  
 193 current SNR models for ambient density of  $\sim 1 \text{ H cm}^{-3}$  to a case of  $\sim 10^3 \text{ H cm}^{-3}$  in a MC, both the  
 194 radius and velocity can be scaled down by a factor of  $100^{-2/5} = 0.16$  for the same time scale unit.  
 195 When the shock wave reaches the wind's boundary, the molecular gas is compressed and evolves as a  
 196 buried SNR. Here, we consider a case that massive stars are distributed over the GMC, and they end  
 197 their lives as individual SNe.

198 If high-mass stars compose a dense cluster ending by multiple SNe, they will disrupt the ambient  
 199 clouds [21]. In this case, the SNe may not leave such a bubbly GMC as observed around W43, but will  
 200 blow off the surrounding MCs, from which they formed, leaving a naked stellar cluster.

201 The expansion velocity  $v$  and radius  $r$  of a spherical adiabatic shock wave in a uniform-density  
 202 gas are related to the input kinetic energy  $E_0$  and gas density  $\rho_0$  as  $E_0 \sim (1/2)(4\pi/3)r^3\rho_0v^2$ , where  
 203  $\rho_0 = \mu n_{\text{H}_2,0}m_{\text{H}}$  is the ambient gas density. Most of the released energy by core-collapse SN explosion,  
 204  $\sim 10^{51}$  erg, in a dense gas cloud is exhausted by the initial infrared flash within  $\sim 10^2$  years [3,19,20].  
 205 After the initial radiation phase, the kinetic energy given to the gas expansion may be assumed to be  
 206 on the order of  $E_0 \sim 10^{50}$  erg, an order of magnitude smaller than the total released energy.

207 We here introduce a parameter,  $ED$ , defined by  $ED = \log(E_0/n_{\text{H}})$ , where  $E_0$  is the input energy  
 208 by the explosion in ergs, and  $n_{\text{H}}$  is the number density of hydrogen atoms in  $\text{cm}^{-3}$ . The hydrogen  
 209 number density in a molecular cloud is related to the  $\text{H}_2$  density through  $n_{\text{H}} = \mu n_{\text{H}_2}$  with  $\mu = 2.8$ .  
 210 The observed radius and velocity for the CO bubble G31.2+0.2 of  $\sim 7 \text{ pc}$  and  $\sim 7 \text{ km s}^{-1}$  is realized,  
 211 when  $ED = 46.3$ , and the age is determined to be  $t \sim 0.4 \text{ My}$ . If we adopt  $E_0 = 10^{50}$  erg, the density is  
 212 required to be  $n_{\text{H}} = 5 \times 10^3 \text{ H cm}^{-3}$ , or  $n_{\text{H}_2} \sim 2 \times 10^3 \text{ H}_2 \text{ cm}^{-3}$ . If the cooling is significant so that the  
 213 input energy is equivalently decreased to  $E_0 = 10^{49}$  erg, the density may be an order of magnitude  
 214 lower, consistent with the measured density of  $\sim 230 \text{ H}_2 \text{ cm}^{-3}$  in the GMC around W43.

### 215 3.4. Evolution

216 The presently identified molecular bubbles exhibit close resemblance to that reported in our  
 217 earlier paper on G34.75-0.2 [22]. We here try to explain the molecular bubbles as due to dark SNRs,  
 218 which had evolved in the molecular clouds as buried SNR in W43 molecular clouds, ceased their  
 219 expansion, and faded out of the thermal and high-energy radiation phase.

220 The evolutionary time scale in the radiation phase of buried SNRs is two orders of magnitude  
 221 shorter than the usual SNRs exploded in inter-cloud low-density regions because of the extremely  
 222 higher ambient density, so that the luminous phase ends in  $\sim 10 - 100$  y [3,19–21]. For the short  
 223 lifetime, they have little chance to be observed and catalogued as radio or optical SNRs, but can be  
 224 recognized by molecular bubbles as dark SNRs in their latest phases.

225 Figures 5 illustrates the evolutionary scenario along a flow line of the Galactic rotation. It  
 226 schematically explains the spiral arm structures of molecular clouds, HII regions and of SNRs,  
 227 according to the evolutionary scenario under the galactic shock wave theory. We may summarize the  
 228 evolution from core collapse SNe to dSNR as follows.

#### 229 3.4.1. Galactic shock wave, cloud collision, and star formation ( $t \sim -1$ My)

230 Diffuse ISM as well as molecular clouds are strongly compressed by the galactic shock wave along  
 231 the 4-kpc molecular arm [25]. Due to both the galactic shock and orbital condensation in the bar-end,  
 232 cloud collisions are strongly enhanced [26]. Accordingly, intense star formation is activated at cloud  
 233 interaction fronts, and OB stars are formed and HII regions are produced, emitting thermal radio and  
 234 far infrared dust emissions. A significant fraction of the formed OB stars and clusters develop inside  
 235 the giant molecular cloud. Frequent cloud collisions cause not only star formation, but also growth of  
 236 molecular clouds by merger, resulting in formation of larger scale molecular complex.

#### 237 3.4.2. SN explosion ( $t = 0$ y), buried, and cool SNR ( $\sim 10^{1-2}$ y)

238 The OB stars explode as supernovae, and their significant fraction are still embedded inside  
 239 the molecular complex along the molecular arm. Most of the released energy of SNe is exhausted  
 240 by radiation of neutrinos,  $\gamma$  rays, and hard-X rays. The ejecta of SNe and snow-plowed gas in the  
 241 molecular cloud form expanding buried SNRs, which evolve rapidly due to strong cooling by the dust  
 242 and thermal emissions in infrared and mm waves. The buried SNRs end their shining phase in a life  
 243 time as short as  $\sim 10^2$  y, leaving cool SNRs.

#### 244 3.4.3. Dark SNR as molecular bubbles ( $\sim 10^3 - 10^5$ y)

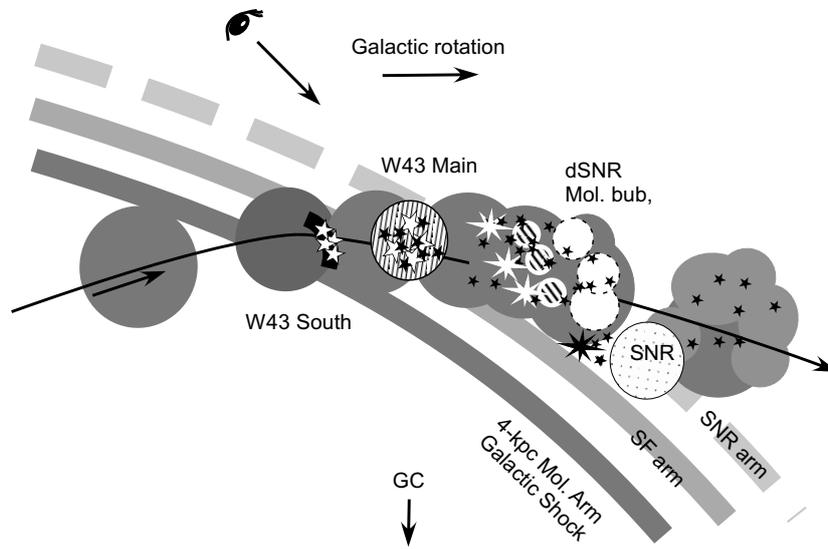
245 The evolved buried SNRs remain as dark SNRs, which expand as an almost adiabatic shock wave  
 246 in the dense molecular gas. They are observed as the molecular cavities and bubbles in their expanded  
 247 phase, as reported in this paper.

### 248 3.5. Bubble properties

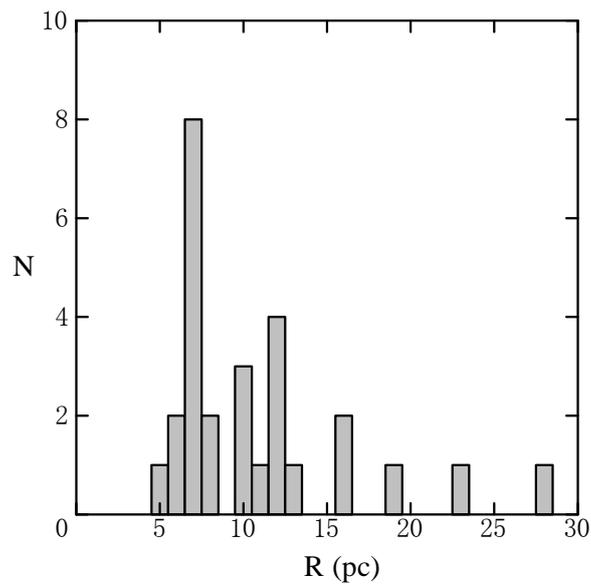
249 As readily shown in figures 1, A1 and A2, the analyzed region is full of molecular bubbles. The  
 250 bubbles have a typical radius of  $r \sim 7$  pc, spreading from 5 to 15 pc. Some arc shaped filaments with  
 251 larger radii or length of 15 pc are also found in the maps, which are supposed to be segments and/or  
 252 remnants of CO bubbles. Besides those counted here, there appear a larger number of fainter shells  
 253 and arcs that cannot be measured on the maps. So, the here listed bubbles may be a minimal set of  
 254 dark SNRs in the analyzed region.

255 It may be stressed that the here found bubbles exhibit round shapes. If they are rings or loops,  
 256 such generally round shapes are not expected, but they must exhibit elongated ellipses on the sky  
 257 because of the higher probability of viewing a ring obliquely. It is, therefore, natural to consider that  
 258 they are spherical bubbles.

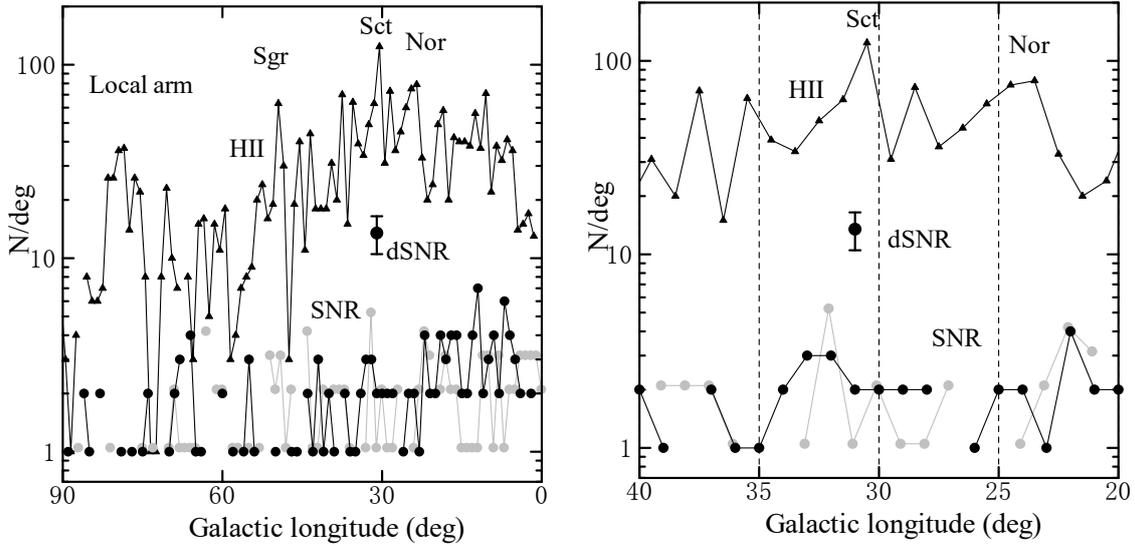
259 It is also emphasized that such molecular bubbles were recognized for the first time thanks to  
 260 the high velocity and angular resolutions of the FUGIN survey. In fact, they are hardly seen in the  
 261 integrated intensity maps [26] or in lower resolution CO surveys [35]. This is because each bubble  
 262 appears in a narrow velocity range within a few  $\text{km s}^{-1}$ .



**Figure 5.** Face-on view of the 4-kpc arm from the north Galactic pole, illustrating the evolution of a molecular cloud and dSNRs along the Galactic flow line by rotation through a galactic shock.



**Figure 6.** Frequency of bubble radii for assumed distance of 5.5 kpc to W43.



**Figure 7.** [Left] Longitudinal number density per one degree  $N$  of Green's catalog SNRs (black and grey circles in the 1st and 4th Galactic quadrants, respectively), HII regions (triangles), and CO bubbles (dSNR) (big circle with error bars). [right] Same, but enlarged around the Scutum Arm.

### 263 3.6. SN rate in the Spiral Arm

264 The rate of SNe in the Galaxy has been estimated to be on the order of  $2 \pm 1$  per 100 y by various  
 265 observations (see table 1 of [14]). Particularly, the rate of core collapse SNe supposed to be responsible  
 266 for shell type SNRs has been rather accurately determined from the  $\gamma$ -ray spectroscopy [12,14,15],  
 267 yielding  $1.9 \pm 1.1$  per 100 y. This predicts  $\sim 200$  shell type SNRs in the Galaxy for an assumed life  
 268 time of a shell of  $\sim 10^4$  y, or  $\sim 2000$  for  $\sim 10^5$  y, strongly dependent on the adopted life time of a  
 269 shell. Estimation of the exact life time of a shell is difficult from observations of SNRs expanding into  
 270 the turbulent ISM with significant deformation. Furthermore, the Galactic plane is observed to be  
 271 full of unidentified radio filaments [23,30,31], suggesting the presence of a large number of debris of  
 272 un-catalogued old SNRs.

273 We may thus argue that the density of existing shell type SNRs in the Galaxy is on the order of or  
 274 greater than  $\sim 200 - 2000$ . Furthermore, from the  $^{26}\text{Al}$   $\gamma$ -ray spectroscopy and intensity distribution,  
 275 the SNe have been shown to be concentrated around the Galactic Centre within  $|l| \lesssim 30^\circ$  [14].  
 276 This means that we may expect a higher density of shell-type SNRs in the presently studied region  
 277 than  $N \sim 200 - 2000/60^\circ$  or 3 to 30 per degree of longitude. Furthermore, if the SNRs are spatially  
 278 correlated with the SF arms, they must be more concentrated in the tangential direction of the spiral  
 279 arms. Thus, we may expect a much higher, or the highest longitudinal SNR density in the tangential  
 280 direction of the Scutum arm (4-kpc molecular ring) at  $l \sim 30^\circ$  nesting W43, the most active SF site in  
 281 the first quadrant of the Galaxy.

282 If the bubbles are relic of buried SNRs, the radii and expanding velocities suggest that their ages  
 283 are on the order of  $\sim 0.4$  My. This is an upper limit to the age, and the real dSNRs would have evolved  
 284 a bit rapider due to cooling effects. So, we here assume that their ages are on the order of  $10^5$  y. As  
 285 counted in the Appendix, the number of CO bubbles in the longitude range from  $l = 30^\circ$  to  $32^\circ$  is  
 286  $N \pm \sqrt{N} = 27 \pm 5$  per 2 degrees in longitude, or  $13.5 \pm 3$  per degree. On the other hand, the catalogued  
 287 SNRs yields  $N \sim 3$  per degree in the same direction. In figure 7 we plot the thus estimated counts in  
 288 comparison with those of the catalogued SNRs [4,5] as well as with the number of HII regions per  
 289 degree [36].

290 Although the longitudinal number density of the catalogued SNRs shows enhancement in the  
 291 tangential directions of the spiral arms, it is significantly weaker than that of the HII regions. It may be

292 also mentioned that the density peak of SNRs is about one degree shifted toward outer longitude side  
 293 from the peak of HII regions. This means that the SNR arm is located outside the star-forming arm by  
 294 about 100 pc, which is consistent with the evolutionary scenario of SNRs in the spiral arm (figure 5).

295 We finally mention that an advantage of using CO bubbles is that the bubbles simultaneously  
 296 yields radial velocities, and hence, kinematic distances of the dSNRs. Statistical analyses using a larger  
 297 number of dSNRs with known distances would have implication to estimate the supernova rate in the  
 298 spiral arms more accurately.

#### 299 4. Summary

300 Numerous round-shaped bubbles and cavities of CO-line emission with radii of  $\sim 5 - 10$  pc were  
 301 found in the molecular complex around W43 (G31+00+90 km s<sup>-1</sup>) in the tangential direction of the  
 302 4-kpc star-forming arm.

303 The bubbles are quiet in radio continuum emission, unlike usual supernova remnants (SNR) or  
 304 HII regions, and are dark in infrared dust emission, unlike molecular bubbles around YSOs. The CO  
 305 bubbles are interpreted as due to dSNR, or fully evolved SNRs buried in dense molecular clouds  
 306 after rapid exhaustion of released energies by SNe. Increased velocity width in the bubbles as seen in  
 307 the LV diagrams compared with that in the ambient molecular gas may be a direct evidence for the  
 308 acceleration of interstellar turbulence by SN explosions.

309 From the number count of the "dark" SNRs in W43 complex, we argue that the supernova rate  
 310 currently estimated from the catalogued SNRs has been significantly under-estimated. Such correction  
 311 of the SN rate in the Galactic disc would affect the star formation history in the Milky Way. We proposed  
 312 to use the CO bubbles to search for a more number of dSNRs. Taking advantage of simultaneously  
 313 obtained radial velocities, and hence kinematic distances to the dSNRs, we will be able to perform a  
 314 more accurate statistical analyses of the correlation between SNR and HII regions in the Galaxy.

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 316 of the Galactic plane using the Nobeyama 45-m telescope. The data analysis was partially carried out at the  
 317 Astronomy Data Center of the National Astronomical Observatory of Japan. The data underlying this article are  
 318 available in the URL <http://nro-fugin.github.io>.

319 **Conflicts of Interest:** The author declares no conflict of interest.

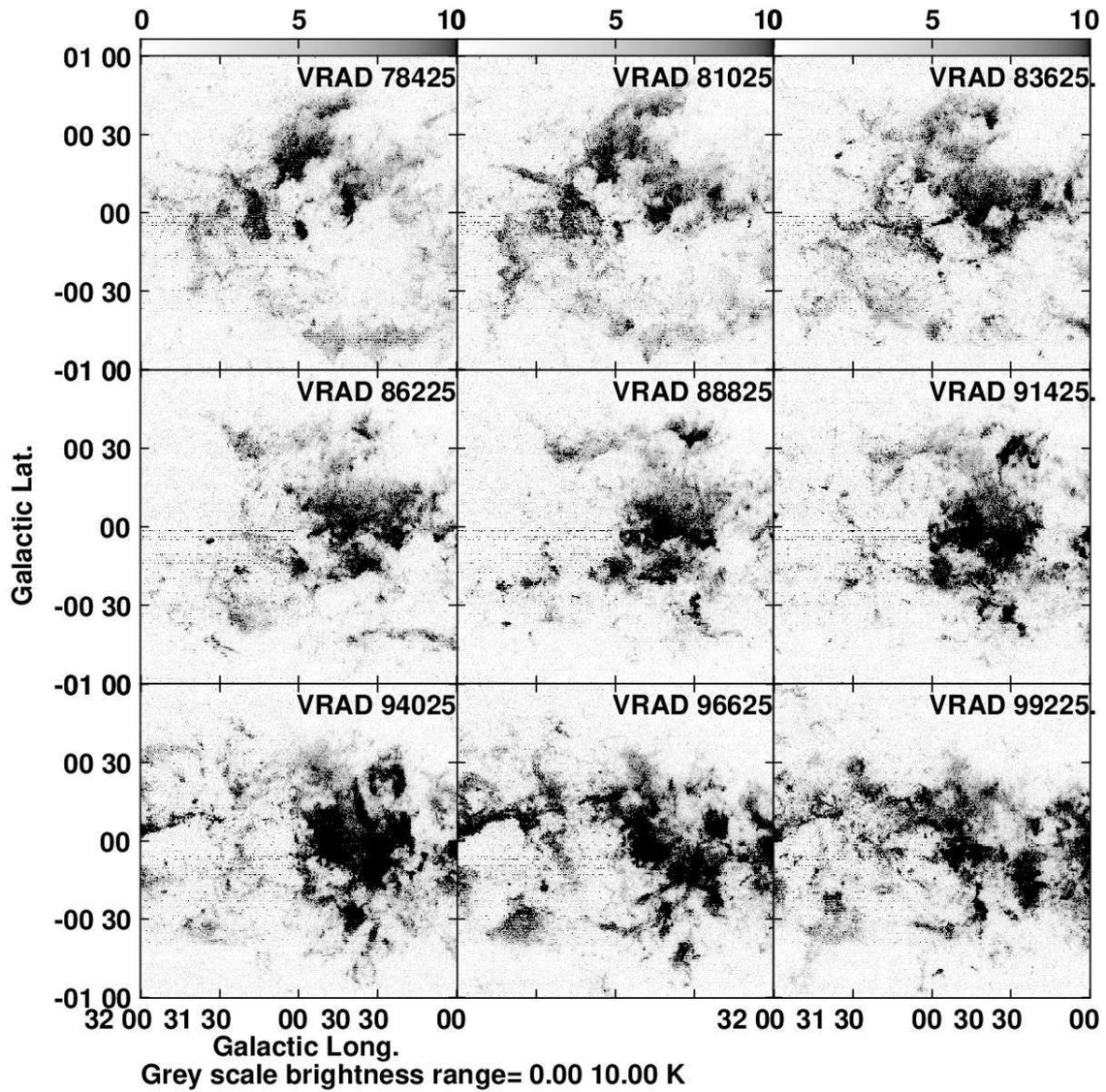
#### 320 Appendix A. Channel maps and background-filtered images

321 In figure A1 we present channel maps of the <sup>12</sup>CO brightness temperature,  $T_B$ , in a  $2^\circ \times 2^\circ$  region  
 322 around W43 Main centered on G31+00+90 km s<sup>-1</sup> every 4 original channels, or every  $= 4 \times 0.65 = 2.6$   
 323 km s<sup>-1</sup> velocity interval. W43 Main is located at  $l = 30^\circ.8$ ,  $b = 0^\circ$  embedded in the giant molecular  
 324 cloud at  $v_{lsr} \sim 93$  km s<sup>-1</sup>. The used FITS cube data are available on the FUGIN web pages at  
 325 <http://nro-fugin.github.io>. Figure A2 shows the same, but extended structures with scale sizes greater  
 326 than  $\sim 3'$  have been subtracted in order to enhance smaller scale clouds and filaments. The figures  
 327 exhibit numerous bubbles, arcs and filaments.

328 Using the original channel maps between  $v_{lsr} = 80$  and  $100$  km s<sup>-1</sup> at velocity increment of  $0.65$   
 329 km s<sup>-1</sup>, we have traced CO bubbles by eye estimate. Thereby, each bubble was identified as a loop of  
 330  $T_B$  ridge that can be traced over a couple of neighboring channels. Their positions and radii are shown  
 331 in figure 6, and are listed in table A1 along with radial velocities,  $v_{lsr}$ . Half velocity widths of the  
 332 bubbles,  $\delta v_{lsr}^{1/2}$ , defined as half the velocity range in which a bubble can be traced on the neighboring  
 333 channel maps, were also measured and listed in the table. It is shown that the expanding velocity of a  
 334 bubble measured on the LV diagram is about three times the here listed half velocity width. We also  
 335 list typical brightness temperature of each bubble edge as read on the relieved channel maps.

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**Figure A1.** Channel maps of  $^{12}\text{CO}$  brightness temperature of the W43 complex from 78 to 100  $\text{km s}^{-1}$  every  $2.6 \text{ km s}^{-1}$  (every 4 original channels). Radial velocities (VRAD) of the channels are indicated in  $\text{m s}^{-1}$  in the individual panels.

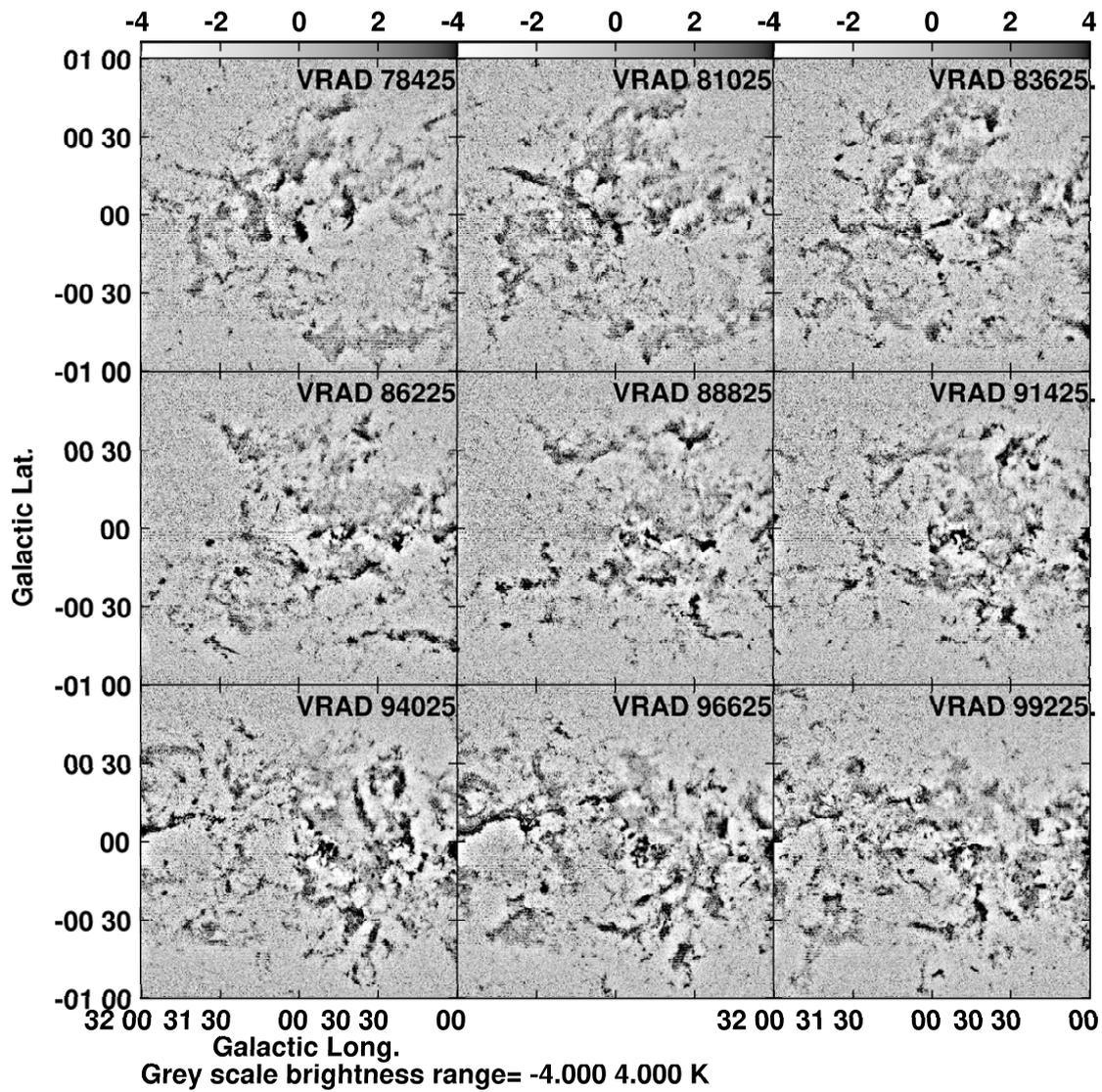
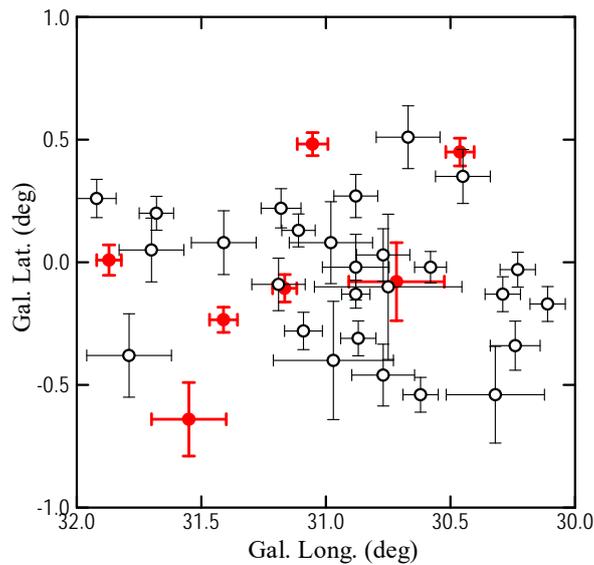


Figure A2. Same as Fig.A1, but extended structures have been subtracted in order to enhance shells and arcs.

**Table A1.** Parameters of CO bubbles

$l$ (deg)	$b$ (deg)	$r$ (deg)	$r$ (pc)	$v_{\text{lsr}}$ (km s <sup>-1</sup> )	$\delta v_{\text{lsr}}^{1/2}$ (km s <sup>-1</sup> )	$T_{\text{B}}$ (K)
30.11	-0.17	0.071	6.8	101.2	3	6
30.23	-0.03	0.071	6.8	82.3	3	4
30.24	-0.34	0.100	9.6	86.6	2	7
30.29	-0.13	0.071	6.8	94.7	2	9
30.32	-0.54	0.197	18.9	88.8	3	9
30.45	0.35	0.110	10.6	94.6	2	12
30.58	-0.02	0.064	6.1	83.0	3	6
30.62	-0.54	0.071	6.8	91.4	2	7
30.67	0.51	0.128	12.3	83.6	2	4
30.75	-0.10	0.296	28.4	84.9	4	6
30.77	0.03	0.107	10.3	79.2	2	6
30.77	-0.46	0.126	12.1	96.6	3	5
30.87	-0.31	0.071	6.8	99.2	3	4
30.88	-0.02	0.134	12.8	79.7	4	9
30.88	-0.13	0.057	5.5	98.6	2	4
30.88	0.27	0.088	8.4	79.1	1	5
30.97	-0.40	0.241	23.1	99.3	3	3
30.98	0.08	0.167	16.3	81.7	3	5
31.09	-0.28	0.076	7.3	91.4	4	4
31.11	0.13	0.067	6.4	81.0	3	5
31.18	0.22	0.080	7.7	81.7	3	6
31.19	-0.09	0.107	10.3	81.7	2	7
31.41	0.08	0.130	12.5	96.6	2	6
31.68	0.20	0.069	6.6	99.2	3	4
31.70	0.05	0.130	12.5	96.0	3	11
31.79	-0.38	0.170	16.3	98.0	2	2
31.92	0.26	0.078	7.5	96.6	2	3



**Figure A3.** Open circles with thin bars indicate positions of CO bubbles traced in the channel maps between 80 and 100 km s<sup>-1</sup> shown in figures A1 and A2, and approximate extent by the bar lengths. Thick red circles and bars show positions and extents of extended radio continuum sources at 5.8 GHz from the VLA observations [29].

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