

# section2\_Ex.5

2024/05/10

M1 Kensho Tanaka

(1) What is the expected value of the Fried parameter at a wavelength of 500nm if the observed seeing is 0.5 arcsec?

- Since seeing size is represented by  $\lambda/r_0$ ,

$$\frac{\lambda}{r_0} = 0.5 \text{ arcsec}$$
$$r_0 = \frac{500nm}{0.5arcsec} = 21cm$$

(2) What is the corresponding value of  $r_0$  at 1.65 microns in the infrared assuming Kolmogorov turbulence?

- assuming Kolmogorov turbulence, Fried parameter  $r_0$  is proportional to  $\lambda^{6/5}$ .

$$r_0 = 21cm \times \left( \frac{1.65\mu m}{0.5\mu m} \right)^{6/5} = 86cm$$

(3) For a 10m telescope, how many sub-apertures does this imply for infrared observations?

- $D = 10\text{m}$
- $x$  : sub-aperture size
- $y^2$  : the total number of sub-aperture
- $m$  : magnification

$$m = \frac{D}{xy}$$

- $xy$  means the total size on a side.

(3) For a 10m telescope, how many sub-apertures does this imply for infrared observations?

- $D = 10\text{m}$
- $x$  : sub-aperture size
- $y^2$  : the total number of sub-aperture
- assuming the sub-aperture size on the primary mirror corresponds the Fried parameter  $r_0$ ,

$$m \times x = r_0$$

so,

$$y = \frac{D}{r_0} = \frac{10\text{m}}{86\text{cm}} = 11.6$$

- That means the total number of sub-apertures is  $y^2 = 121$