McLean seminar

Sec.2 2.8 Exercises Problem 6 2024.5.10

Problem 6

What is the expected value of the Fried parameter at a wavelength of $500 \,\mathrm{nm}$ if the observed seeing is $0.5 \,\mathrm{arcsec}$? What is the corresponding value of r_0 at $1.65 \,\mathrm{microns}$ in the infrared assuming Kolmogorov turbulence? For a $10 \,\mathrm{m}$ telescope, how many sub-apertures does this imply for infrared observations?

Determine the size of the isoplanatic patch and the isokinetic patch at the 0.5-micron wavelength for the case in Problem 5 assuming a turbulent layer at 5 km above the telescope.

In Problem 5, with the observed seeing is 0.5", the expected value of r_0 at the 0.5 um can be derived as follows:

r_0 =
$$\lambda$$
/seeing = $\frac{0.5 \text{ um}}{0.5''} = \frac{0.5 \times 10^{-6} \text{ m}}{0.5 \times \frac{\pi}{180 \times 3600}} = 0.2 \text{ m}$

Therefore, assuming a 10 m telescope and a turbulent layer at 5 km above it, the sizes of isoplanatic patch(θ_{ip}) and the isokinetic patch(θ_{ik}) can be determined,

$$\theta_{\rm ip} = 0.314 \frac{r_0}{H} = 0.314 \frac{0.2 \,\mathrm{m}}{5 \,\mathrm{km}} = 2.6'', \theta_{\rm ik} = 0.3 \frac{D}{H} = 0.3 \frac{10 \,\mathrm{m}}{5 \,\mathrm{km}} = 124''$$