

The unified rotation curve of the Galaxy sampled from the nucleus to halo: URC2026

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Abstract

We present the unified rotation curve (URC) of the Milky Way with the highest resolution and most complete sampling from the central super massive black hole (SMBH) to the outermost halo up to ~ 300 kpc. The URC consists of the following five mass components: 1. the fixed central SMBH, 2. massive core by exponential sphere with scale radius and mass of (4 pc, $4 \times 10^7 M_\odot$), 3. bulge by exponential sphere (150 pc, $1.0 \times 10^{10} M_\odot$), 4. exponential disk (3.8 kpc, $1.5 \times 10^{11} M_\odot$), and 5. Navarro-Frenk-White halo with scale radius $h \sim 14$ kpc and density $\rho_0 \sim 9 \times 10^{-3} M_\odot \text{pc}^{-3}$, critical radius and mass with $R_{200} \sim 81$ kpc and $M_{200}^{\text{total}} \sim 4.2 \times 10^{11} M_\odot$. The lower limit to the local DM density at the Sun is estimated as $\sim 0.24 \text{ GeV cm}^{-3}$ ($\sim 6 \times 10^{-3} M_\odot \text{pc}^{-3}$) as the value calculated for the NFW DH profile.

Keywords: galaxies: individual (Milky Way) — galaxies: rotation curve — Galaxy: kinematics and dynamics — galaxies: Cosmology – dark matter

1 Introduction

The rotation curve (RC) is the most fundamental tool for measuring the dynamical mass and its distribution in the Galaxy under the assumption that the galaxy is rotating around its polar axis (Sofue and Rubin 2001; Sofue 2017; Sofue 2020; Lelli et al. 2016; McGaugh 2016; Salucci 2019). In our earlier papers (Sofue et al. 2009; Sofue 2012; Sofue 2013) we have constructed a "unified RC (URC)" of the Galaxy from the nucleus to a half way to M31 including the outer halo by combining the existing rotation data in the decades from 1980's to 2000's. We have also deconvolved the URC into several mass components to obtain fundamental parameters such as the total mass and scale size of each component, as well as the local density of dark matter (DM) (Sofue 2013; Sofue 2020).

In this paper, we revise the URC of the Milky Way by employing the most recent data about Galactic rotation. We integrate the current RCs determined individually for the Galactic Center by the ALMA molecular line survey of the central molecular zone (CMZ) (Longmore et al. 2026; Sofue et al. 2025), the inner disk using the CO and HI-line surveys of the Galactic plane (Sofue & Kohno 2025), the stellar disk by trigonometry of maser sources using VERA (VERA Collaboration et al. 2020) and VLBA (Reid et al. 2019), the disk stars by GAIA trigonometry (Eilers et al. 2019), and 3D velocities of globular clusters and dwarf galaxies with GAIA (Jiao et al. 2023; Sylos Labini 2024). We adopt the Galactic constants $R_0 = 8.18$ kpc (Gravity Collaboration et al. 2019) and $\Theta_0 = 235.1 \text{ km s}^{-1}$ (Sofue & Kohno 2025).

We then use the URC to calculate the mass distribution in the Galaxy assuming circular motion, which is well confirmed by the 3D motion map by the VLBI trigonometry and proper motion observations (VERA Collaboration et al. 2020). There are two major methods to estimate the mass: (1) Dynamical (Virial-theorem)

method and (2) photometry. The dynamical method uses kinematical data such as the rotation curve, and are widely used to measure the dynamical mass of the Galaxy and galaxies (Sofue and Rubin 2001; Sofue 2017; Sofue 2020). This method measures the total mass including black holes, stars, ISM, and dark matter, yielding the radial distribution of the mass density. However, it cannot discriminate the fraction of the individual species like DM from stars. Infrared photometry has been extensively performed of the nuclear stellar cluster, bulge and disk to measure the 3D distribution of red giant stars (Robin et al. 2012; Schödel et al. 2014; Portail et al. 2015; Wegg et al. 2015; Ness & Lang 2016; Valenti et al. 2016; Simion et al. 2017), which has given still spreading masses of the bulge and disk. In this paper, we perform the dynamical determination of the total mass distribution in the Galaxy, which will provide a basis to calibrate the photometry results.

2 Construction of URC26

2.1 Central black hole

The rotation curve around the central supermassive black hole (SMBH) located at the nucleus (Sgr A*) with a mass of $M_1 = 4.0 \times 10^6 M_\odot$ (Ghez et al. 2008; Gillessen et al. 2009) is represented by the Keplerian law.

2.2 Central Molecular Zone (CMZ)

We have recently determined the RC in the CMZ using the ACES survey data (Longmore et al. 2026) by applying the terminal velocity method to the longitude-velocity diagrams (LVD) of the CS ($J = 2 - 1$)-line emission from the molecular gas in the CMZ and the H40 α -line from the ionized gas in the minispiral (Sofue et al. 2025). Figure 1 shows the RC inside $R \sim 120$ pc. The entire CMZ

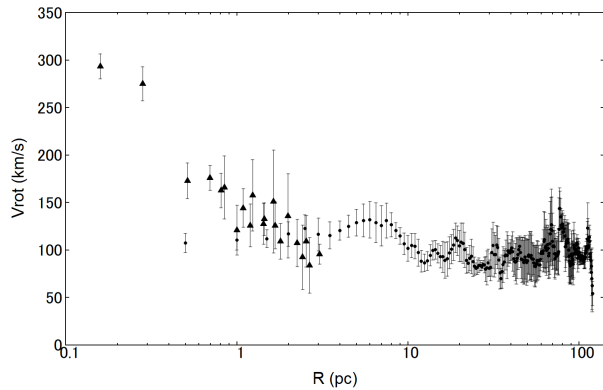


Fig. 1. Rotation curve of the CMZ in the central 120 pc obtained by terminal velocity method for H40 α (triangles) and CS ($J = 2 - 1$) (dots) lines in semilogarithmic scaling (Sofue et al. 2025). Alt text: Rotation curve of the Galactic Center.

61 has a nearly flat RC at $V_{\text{rot}} \sim 100 \text{ km s}^{-1}$ associated with a peak
 62 around $R \sim 5 \text{ pc}$. The innermost V_{rot} within $R \lesssim 1 \text{ pc}$ increases
 63 toward the nucleus, obeying the Keplerian law due to the central
 64 SMBH.

65 2.3 Gas disk by terminal velocities of CO and HI lines

66 Inside the solar circle ($-90^\circ \leq l \leq 90^\circ$), the rotation velocity $V(R)$
 67 at the galacto-centric distance $R = R_0 \sin l$ is calculated simply by
 68 correcting the terminal velocity V_{term} for the circular motion of
 69 the LSR (local standard of rest) at the Sun:

$$70 \quad V_{\text{rot}}(R) = V_{\text{term}} + \Theta_0 \sin l. \quad (1)$$

71 In figure 1 we show the inner RC obtained recently by Sofue &
 72 Kohno (2025), applying TVM to CO and HI line survey data of
 73 the Galactic plane (Dame et al. 2001; HI4PI Collaboration et al.
 74 2016; Umemoto et al. 2017; Braiding et al. 2015; Cubuk et al.
 75 2023).

76 2.4 Stellar disk by VLBI trigonometry of maser sources

77 Recent trigonometric measurements of maser sources using VERA
 78 (VLBI exploration of radio astrometry) (VERA Collaboration et al.
 79 2020) and VLBA (very long baseline array) (Reid et al. 2019)
 80 have provided accurate 3D motions of the sources in the Galactic
 81 disk, which yielded circular rotational rotation curves at high accu-
 82 racy. These results were combined with the inner RC from the
 83 terminal velocity to yield an RC from the Galactic Center to the
 84 halo at $R \sim 15 \text{ kpc}$. In figure 2 we plot the circular velocities of
 85 maser sources from VERA by blue triangles and those by VLBA
 86 measurements by magenta dots.

87 2.5 Stellar disk and halo by GAIA trigonometry

88 The GAIA mission has provided proper motions of billions of stars
 89 in the Milky Way, and yielded high accuracy rotation curves of
 90 the mid to outer Galactic disk at $R \sim 8$ to 25 kpc (Eilers et al.
 91 2019; Jiao et al. 2023; Sylos Labini 2024). We plot the circular
 92 velocities from GAIA DR3 by the inverse triangles in figure 2.

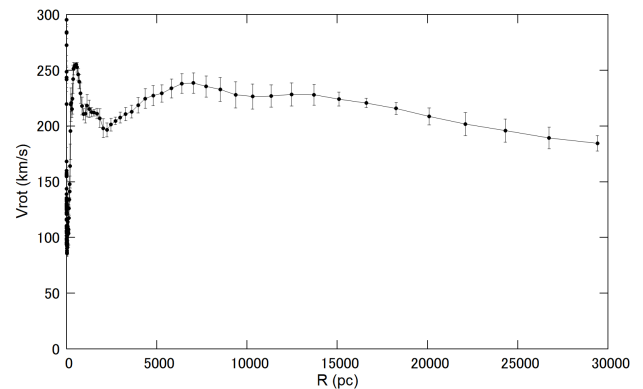
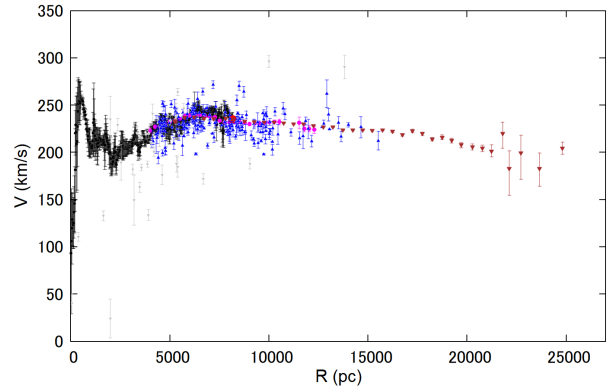


Fig. 2. RC up to 30 kpc by combining the inner RC of the gas disk using the terminal velocity method (black dots) (Sofue & Kohno 2025), trigonometry of maser sources with VERA (blue dots) (VERA Collaboration et al. 2020) and VLBA (magenta dots) (Reid et al. 2019), and disk stars by GAIA DR3 (brown triangles) (Jiao et al. 2023) by combining the RCs in figures 1 and 2. Alt text: URC26 added by $V_{3D}/\sqrt{2}$ of globular clusters and dwarf galaxies.

93 2.6 Halo RC from 25 to 100 kpc by globular clusters

94 For the outer Galactic halo, we employ GAIA trigonometric mea-
 95 surements of globular clusters (Vasiliev & Baumgardt 2021; Wang
 96 et al. 2022). In figure 3 we plot the circular rotation velocities pre-
 97 sented by Wang et al. (2022), which cover $R \sim 25$ to $\sim 100 \text{ kpc}$.

98 2.7 Halo RC from 25 to 300 kpc by dwarf galaxies

99 For ~ 25 to 300 kpc we use the 3D velocities observed by the
 100 GAIA trigonometry of dwarf galaxies (Li et al. 2017; Li et al.
 101 2021; Hammer et al. 2021; Hammer et al. 2023). Following Sofue
 102 (2013) we introduce a "pseudo" rotation velocity of dwarf galaxies
 103 defined by

$$104 \quad V_{\text{rot}} = \eta V_{3D} = \eta \sqrt{v_{\text{RA}}^2 + v_{\text{Dec}}^2 + v_{\text{radial}}^2}. \quad (2)$$

105 Here, v_i ($i = \text{RA}, \text{Dec}, \text{radial}$) are the velocities calculated for the
 106 proper motions and radial velocity with GAIA and η is a conver-
 107 sion factor of the 3D velocity to a pseudo circular velocity at the
 108 same radius. We assume $\eta \sim 1/\sqrt{2}$, considering that the dwarfs are
 109 half way to their apocenters and the orbital inclinations to the
 110 line of sights are random. We also examine a case with $\eta = 1$, which
 111 will yield the upper limit of the circular velocity. Using the veloci-
 112 ties thus converted we perform the Gaussian running average and
 113 plot them in figure 3. This "dwarf correction factor" η could vary

114 between $\eta \sim 1$ and $\sim 1/\sqrt{3}$, depending on the dynamical condition
 115 of the halo. This means that the dark halo mass estimation in this
 116 paper includes a systematic error of a factor of ~ 2 .

117 2.8 URC26: Unified RC from the GC to outermost halo

118 We then construct a unified RC (URC) by taking the Gaussian run-
 119 ning average (GRA) of the circular velocities $V(R_i)$ measured at
 120 $R = R_i$ for the i -th data points by the individual methods. The
 121 GRA value of V at a radius R is calculated by

$$122 \quad V(R) = \frac{\sum_{i=1}^N V_i w_i}{\sum_{i=1}^N w_i} \quad (3)$$

123 and

$$124 \quad \delta V = \left[\frac{\sum (V(R) - V_i)^2 w_i}{\sum w_i} \right]^{1/2}, \quad (4)$$

125 where

$$126 \quad w_i = \exp \left[-\frac{(R_i - R)^2}{\delta R^2} \right] \sigma_i^{-2}, \quad (5)$$

127 and σ_i is the error of the observed value of the i -th data point and
 128 $\delta R \sim 0.1R$ is the smoothing width. We plotted the URC in figure
 129 3 at the same logarithmic radius interval.

131 Figure 4 shows a simultaneous plot of the RC that includes the
 132 SMBH, CMZ, bulge, disk, halo, and outer halo up to ~ 300 kpc,
 133 about half way to the Andromeda galaxy, in logarithmic scaling.
 134 We name this diagram the "URC26" (unified rotation curve 2026).

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136 3 Discussion

137 3.1 Basic methods to derive the dynamical mass

138 We use the dynamical method based on the Virial theorem, which
 139 is a direct method using kinematical data such as the rotation
 140 curve. Widely adopted models to represent the bulge and disk
 141 are exponential sphere, exponential disk, Sérsic type potential,
 142 Miyamoto-Nagai potential, and the Plummer potential. We here
 143 adopt the exponential sphere for the core and bulge, and a flat
 144 exponential disk for the disk component. We comment that all
 145 these models yield rotation curves similar to each other composed
 146 of a rigid-body rise, a peak at ~ 2 scale radii, and a Keplerian
 147 decrease, coinciding within a few percent with each other. The
 148 good agreement for different models is due to the long range of
 149 the gravitational force and the fast decrease in the density outside
 150 the scale radius in these models. However, NFW type potentials
 151 for the halo behaves quite differently, diverging outward because
 152 of the slow decrease of density.

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154 3.2 Deconvolution of URC26 into dynamical mass 155 components

156 The rotation curve is represented by a superposition of N dynamical
 157 mass components as

$$158 \quad V_{\text{rot}}(R) = \sqrt{\sum_{i=1}^N V_i(R)^2}, \quad (6)$$

159 where $V_i(R)$ is the circular velocity at radius R due to the i -th
 160 component. By a close look into URC26 in figure 4 we recognize
 161 five ($N = 5$) distinct mass components characterized by five ve-
 162 locity peaks at the center ($R \sim 0$ pc), $R \sim 5$ pc, ~ 500 pc, ~ 5000
 163 pc and an outskirts that extends to $R \sim 300$ kpc. We here attribute
 164 these peaks to 1) SMBH, 2) core, 3) bulge, 4) disk, and 5) dark
 165 halo, and try to fit URC26 by superposition of these mass com-
 166 ponents by employing the following profiles. We then decompose

the observed RC into the five components by the least- χ^2 method
 using the following functions representing the individual compo-
 nents. The fitted parameters are listed in table 1

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170 3.2.1 Supermassive black hole

The innermost rotation curve at $R \lesssim 1$ pc is represented by the
 Keplerian law for the massive black hole with $M_{\text{BH}} = 4 \times 10^6 M_{\odot}$
 (Ghez et al. 2008; Gillessen et al. 2009):

$$174 \quad \phi = GM_1/R, \quad (7)$$

and

$$175 \quad V(R) = V_1/\sqrt{R/a_1} \quad (8)$$

with $V_1 = 131.5$ km s $^{-1}$ and $a_1 = 1$ pc.

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178 3.2.2 Core and bulge by exponential spheres

The disk to mid-halo RC at ~ 1 to ~ 15 kpc can be fitted by three
 components of a core, bulge, and disk. We adopt exponential den-
 sity profile expressed as

$$182 \quad \rho_i(R) = \rho_0^i \exp(-R/a_i), \quad (9)$$

where ρ_0^i and a_i are the central density and scale radius of the i -th
 mass component. The rotation velocity is calculated by

$$185 \quad V_{\text{rot}_i}(R) = \sqrt{GM_i(R)/R}, \quad (10)$$

where

$$186 \quad M_i(R) = \int_0^R \rho_i(r) 4\pi r^2 dr \quad (11)$$

187 is the enclosed mass inside R . We stress that because gravity has
 188 a long range force, the Plummer potential is a good approxima-
 189 tion to that of an exponential density distribution, and any similar
 190 mass concentrations with sufficiently rapid density decrease, in an
 191 accuracy of a few percent (Sofue 2017).
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By fitting to URC we obtain the scale radius and mass for the
 bulge to be $a_2 \simeq 2.4$ pc and $M_2 \simeq 3.3 \times 10^7 M_{\odot}$, and for bulge
 $a_3 \simeq 163$ pc and $M_3 \simeq 1.10 \times 10^{10} M_{\odot}$.

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196 3.2.3 Exponential disk

The galactic disk is generally represented by an exponential disk
 (Freeman 1970), where the surface mass density (SMD) is ex-
 pressed as

$$199 \quad \Sigma_d(R) = \Sigma_0 \exp(-R/a_d). \quad (12)$$

Here, Σ_d is the central value, R_d is the scale radius. The total mass
 of the exponential disk is given by $M_{\text{disk}} = 2\pi \Sigma_0 a_d^2$. The circular
 velocity is expressed by

$$204 \quad V_d(R) = V_0 \sqrt{y^2 [I_0(y)K_0(y) - I_1(y)K_1(y)]}, \quad (13)$$

where

$$205 \quad V_0 = \sqrt{4\pi G \Sigma_0 a_d} = \sqrt{2GM_{\text{disk}}/a_d} \quad (14)$$

or

$$206 \quad M_{\text{disk}} = \frac{1}{2} \frac{a_d V_0^2}{G}, \quad (15)$$

with $y = R/(2a_d)$, and I_i and K_i are the modified Bessel func-
 tions.

By fitting we obtain the disk radius and mass of $a_4 \simeq 3.8$ kpc
 and $M_4 \simeq 1.6 \times 10^{11} M_{\odot}$.

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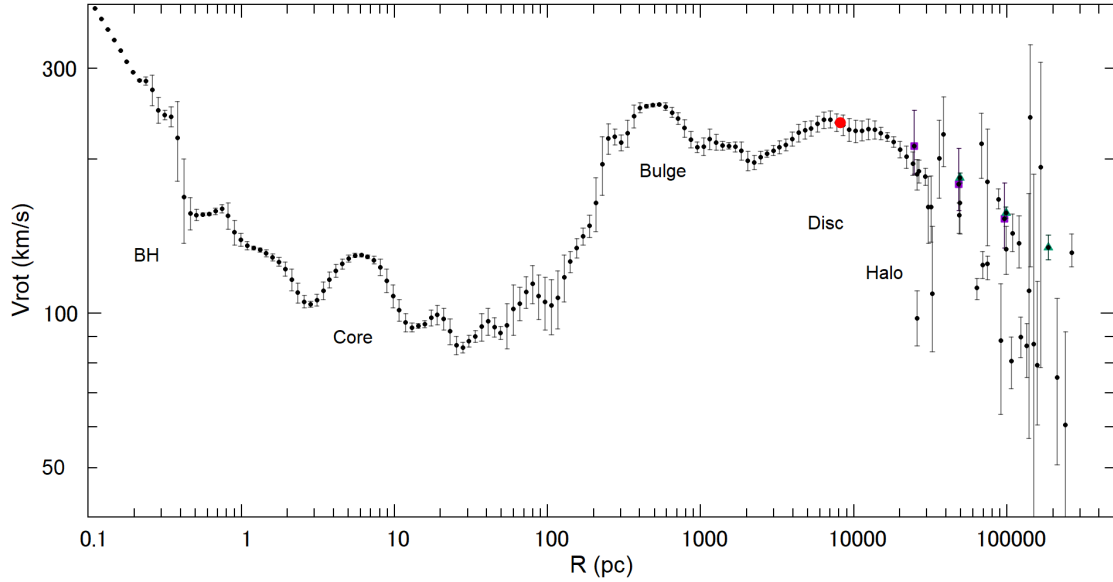


Fig. 3. The unified rotation curve URC2026 from figures 1 and 2 with GAIA trigonometric rotation curves of globular clusters from $R \gtrsim 25$ to 100 kpc by blue triangles and diamonds (Eadie & Jurić 2019; Vasiliev & Baumgardt 2021; Wang et al. 2022) and dwarf galaxies for $\eta = 1/\sqrt{2}$ by black dots (Li et al. 2021; Hammer et al. 2021; Hammer et al. 2023). Grey dots are disk RC from figure 2. The innermost Keplerian curve represents the SMBH of $4 \times 10^6 M_\odot$ (Ghez et al. 2008). We recognize five major components (velocity maxima) which can be attributed to the SMBH (component 1), core (component 2), bulge (3), and disk (4) and the dark halo (5). The big dot marks the Sun at (8.2 kpc, 235 km s⁻¹). Alt text: Unified rotation curve from the GC to halo.

3.2.4 Dark halo by NFW profile

The extended outskirts of the URC beyond $R \sim 15$ kpc can be fitted by the dark halo represented by the NFW density profile (Navarro et al. 1997),

$$\rho_5(x) = \frac{\rho_0}{x(1+x)^2}, \quad (16)$$

where $x = R/h$ and $h = a_5$ is the scale radius. The rotation velocity is given by

$$V_{\text{rot}5}(R) = \sqrt{GM_5(R)/R}, \quad (17)$$

and the mass inside R is given by

$$M_5(R) = 4\pi\rho_0 h^3 [\ln(1+x) - x/(1+x)]. \quad (18)$$

By fitting we obtain $h \sim 13.6$ kpc and $\rho_0 = 8.8 \times 10^{-3} M_\odot \text{pc}^{-3}$. Combining these values with those obtained for the bulge and disk and referring to URC26, as shown in figure 5, we obtain the critical radius and mass of the Galaxy to be $R_{200} \sim 80$ kpc at which the mass density becomes equal to the cosmological critical density, $\rho_{200} = 200 \times (3H_0^2)/(8\pi G) = 1.9 \times 10^{-27} \text{g cm}^{-3} = 2.8 \times 10^{-5} M_\odot \text{pc}^{-3}$ with $H_0 = 71 \text{ km s}^{-1} \text{Mpc}^{-1}$ being the Hubble constant. The critical mass is obtained as $M_{200} = M(R_{200}) \sim 4 \times 10^{11} M_\odot$.

3.2.5 Mass and density distributions

The least χ^2 fitting results using these functions are summarized in table 1. The circular velocity was calculated using the fitted parameters and plotted in Figure 4. The calculated RC reproduces URC26 from the center to R 30 kpc well, and the outer halo (up to 300 kpc) also shows a reasonable fit within the margin of error. URC26 demonstrates the existence of a massive halo in the outermost region up to $R \sim 300$ kpc, which can be reasonably represented by the NFW mass model. However, URC26 does not support the Keplerian decrease in rotation velocity at $R \gtrsim 25$ kpc.

Table 1. Fitting parameters of the URC26 for $\eta = 1/\sqrt{2}$.

i -th component	Parameter
1. SMBH	$M_1 \simeq 4.0 \times 10^6 M_\odot$ ‡
2. Core	$a_2 \simeq 2.44 \pm 0.03 \text{ pc}$ $M_2 \simeq (3.33 \pm 0.06) \times 10^7 M_\odot$
3. Bulge	$a_3 \simeq 162 \pm 1.3 \text{ pc}$ $M_3 \simeq (1.12 \pm 0.01) \times 10^{10} M_\odot$
4. Disk	$a_4 \simeq 3.82 \pm 0.06 \text{ kpc}$ $M_4 \simeq (1.66 \pm 0.04) \times 10^{11} M_\odot$
5. Dark halo	$4\pi\rho_0 h^3 \sim (2.78 \pm 0.08) \times 10^{11} M_\odot$ $\rho_0 = (8.82 \pm 0.25) \times 10^{-3} M_\odot \text{pc}^{-3}$ $a_5 = h \simeq 13.6 \pm 0.5 \text{ pc}$ $R_{200} \sim 81 \text{ kpc}$ $M_{200} \sim 4.2 \times 10^{11} M_\odot$

‡ Ghez et al. (2008)

Using dynamically fitted parameters, the density distribution and cumulative mass were calculated as a function of R and plotted in Figure 5. This diagram shows that mass is concentrated at a high density over a range of more than 10 orders of magnitude, from the dark halo to the nucleus.

The local density of DM is a key parameter for the direct detection experiments of DM. Using figure 5 (equation 16) we obtain the local density of DM at the Sun due to the dark halo alone to be $\rho_\odot^{\text{DM}} \sim 6.2 \times 10^{-3} M_\odot \text{pc}^{-3} \simeq 0.24 \text{ GeV cm}^{-3}$. Note that this value represents only the dark halo contribution, not including the DM in the disk and bulge. So, this is a lower limit of the DM density near the Sun.

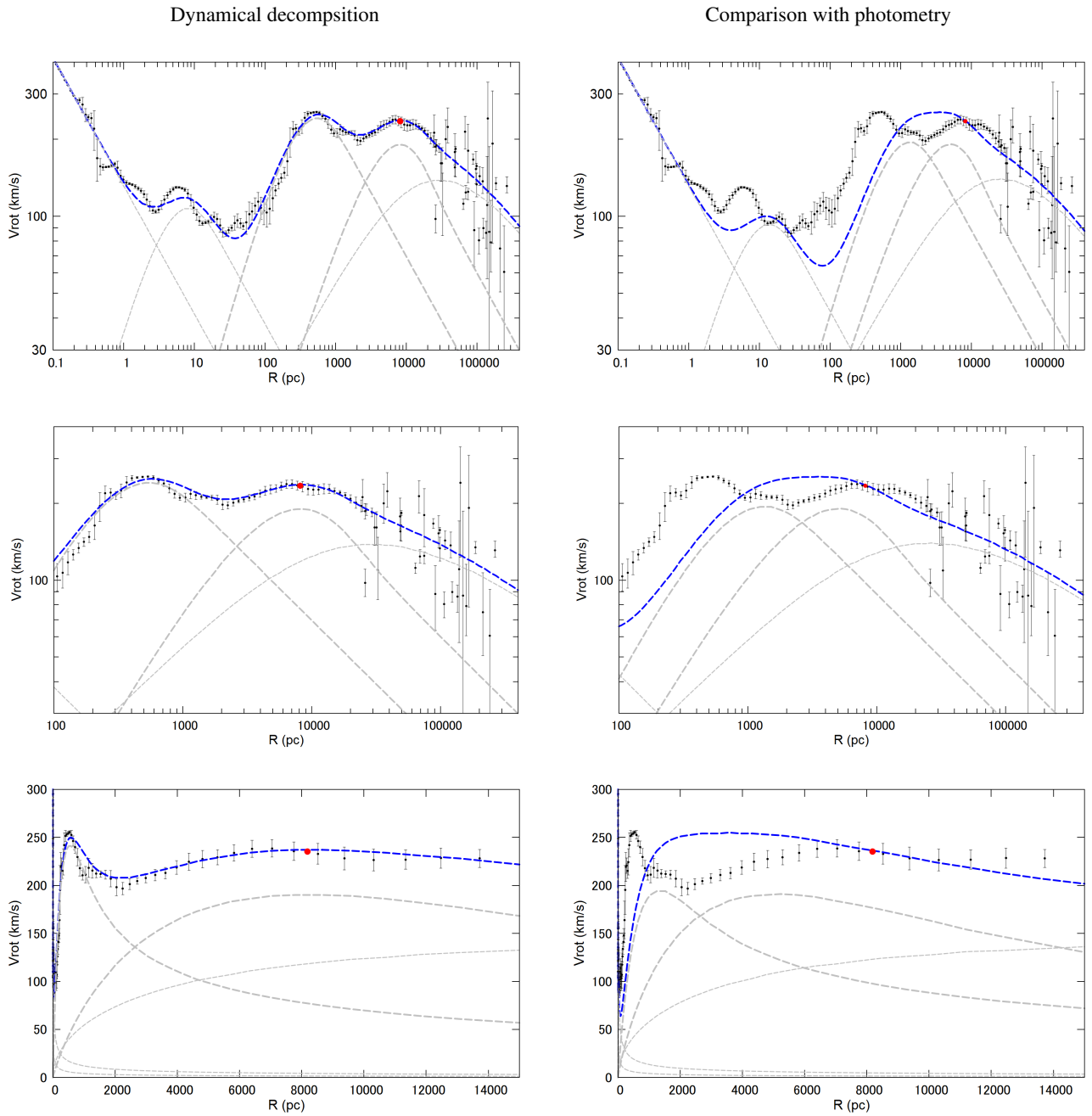


Fig. 4. χ^2 fitting result of URC26 by five dynamical mass components for parameters given in table 1 (left panels) compared with a rotation curve calculated for the photometry values for the core, bulge and disk (right panels). [Top] Logarithmic plot from the nucleus to outer halo. [Middle] Close up from the disk to halo. [Bottom] Close up of the inner Milky Way in linear scaling. Alt text: URC26 compared with that calculated for photometric results and possible fitting by 5 dynamical components.

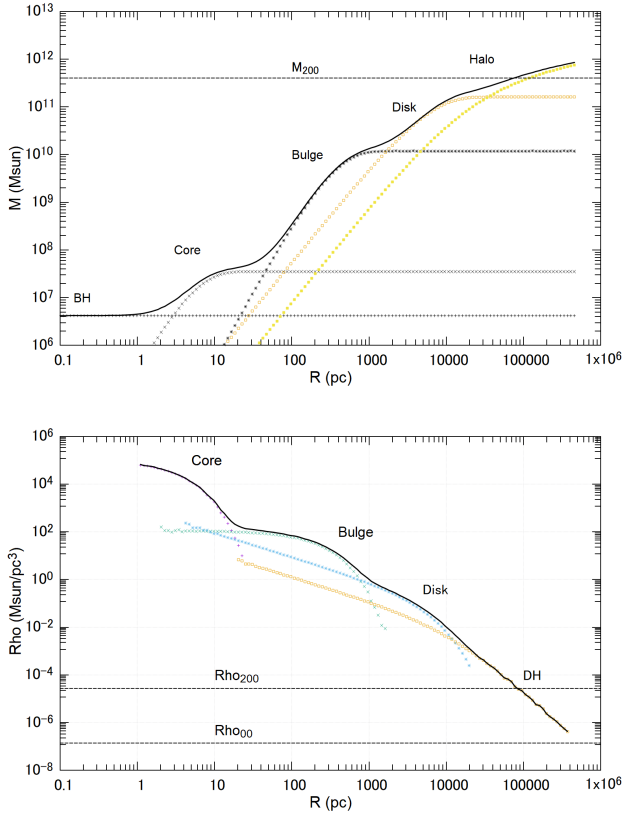


Fig. 5. [Top] Cumulative mass $M(R)$ calculated for the observed values of rotation velocity $\eta = 1/\sqrt{2}$ (dots) and least- χ^2 fitted URC using Plummer potential for the core, bulge and disk (thin line). Magenta triangles show the mass calculated for $\eta = 1$ (open triangles). [Bottom] Volume density calculated for the fitted URC in the top panel. Alt text: Cumulative mass and density distributions.

3.3 Comparison with the results by photometry

Extensive photometric observations in infrared wavelengths at ~ 2 to $\sim 4\mu\text{m}$ have been obtained of the central stellar disk (Schödel et al. 2014), the bulge and disk (Robin et al. 2012; Robin et al. 2014; Wegg et al. 2015; Portail et al. 2015; Ness & Lang 2016; Valenti et al. 2016; Simion et al. 2017; Marasco et al. 2025). We here calculate circular velocities using the parameters obtained by photometry, and compare with the observed URC26 and the dynamical fitting result. For the SMBH and dark halo, we use the results from the previous subsections.

3.3.1 Photometric core (nuclear stellar disk)

We adopt the photometric scale radius and mass of the central stellar cluster, $a_2 \simeq 4.1$ pc and $M_2 \sim 4.2 \times 10^7 M_{\odot}$, from the infrared photometry by Schödel et al. (2014). These values are close to the dynamical values in table 1, and the resulting circular velocity is consistent with the dynamical RC in figure 4.

3.3.2 Photometric bulge

There have been extensive photometric measurements of the scale radius and luminous mass of the Galactic bulge. As median values of the current photometric measurements (Robin et al. 2012; Robin et al. 2014; Wegg et al. 2015; Portail et al. 2015; Ness & Lang 2016; Valenti et al. 2016; Simion et al. 2017), we provisionally

adopt a scale radius of $a_3 \sim 400$ pc corresponding to the minor axis radius of the barred bulge and mass of $M_3 \sim 1.8 \times 10^{10} M_{\odot}$. The amplitude of the calculated circular velocity for the photometric parameters agrees with the observation, while the maximum velocity radius is largely displaced from that of the URC26 by about three times corresponding to the ratio of the photometric to dynamical radii of ~ 400 pc and ~ 150 pc. This causes the too mild rise of the photometric rotation curve to fit the observed steep rise.

Several reasons are considered for the disagreement between the photometric and dynamical RCs of the bulge.

- Photometry might miss a higher concentration near the Galactic plane because the analyses are done avoiding the highly obscured belt in the Galactic plane at $|b| \lesssim 2$ deg.
- The conversion from surface brightness from photometry [Jy str^{-1} to dynamical mass [g cm^{-2}] might miss some spatial effect.
- The observed radial velocity used in the URC might represent non-circular motion due to eccentric orbits in the barred potential as indicated by photometry. However, this requires for the eccentric motion to occur far inside the photometric bulge, which is dynamically difficult. Also, no high eccentric motion is observed in the 3D motion of maser sources in the region under discussion (VERA Collaboration et al. 2020).

Therefore, the large difference of the photometric and dynamical RCs of the inner Milky Way remains a mystery.

3.3.3 Photometric disk

We adopt a scale radius of $a_4 \simeq 2.4$ kpc according to the surface photometry by Robin et al. (2014); Simion et al. (2017), and adjust the total mass to $M_4 \simeq 1.5 \times 10^{11} M_{\odot}$ so that the rotation velocity at the Sun matches the local value of $V_0 = 235 \text{ km s}^{-1}$. The calculated RC well agrees with the dynamical RC fitted in the previous sections, and the parameters are close to each other. Although the dynamical scale radius of 3.8 kpc is slightly greater than the photometry value of 2.4 kpc, difference would be within an allowable range of uncertainty considering the photometry measures only the luminous stars not sensitive to gas and dark matter coexisting in the disk.

3.4 Scaling relation

The deconvolution of the RC into the components enables us to examine the scaling relation between the scale radius, a_i , and total mass, M_i , of the five mass components of the BH, core, bulge, disk and dark halo. For the BH, we define the scale radius as the radius at which the gravity of the BH dominates that of the core component, i.e., $a_{\text{BH}} \sim 0.5$ pc. Figure 6 shows the total masses thus derived against the scale radii of the five components. We find a linear proportionality between the radius and the total mass, which varies by more than six orders of magnitude, and is expressed by $M \sim 10^7 M_{\odot} (R/1 \text{ pc})^{1.1}$, as shown by the straight line in the figure. The diagram may provide a scaling relation within an individual galaxy about the coevolution of the BH, bulge, disk, and dark halo. This provides a complementary relation to the scaling law between the masses of the BHs and bulges among different galaxies (Kormendy & Ho 2013).

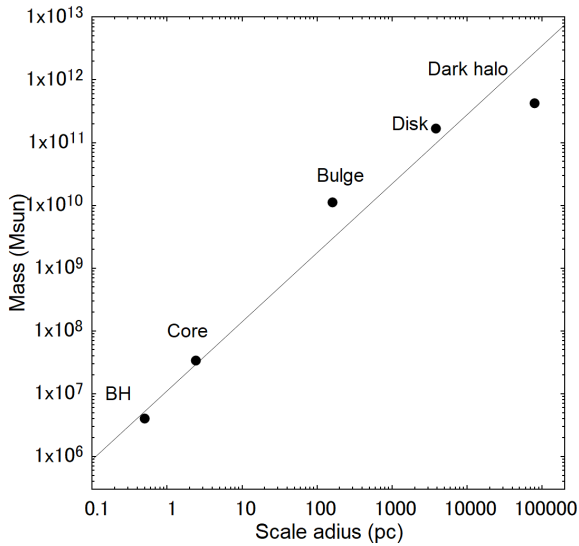


Fig. 6. Scale radius vs total mass of the five mass components of the Milky Way. The radius for BH is approximated by its 'gravity dominant radius'. The upper and lower dots for the DH represent M_{200} (including bulge and disk) and M_{200}^{DM} (DH component alone), respectively. The straight line indicates $M = 10^7 (R/1\text{pc})^{1.1} M_{\odot}$. Alt text: Scaling relation among the deconvolved mass components.

4 Summary

We derived the most completely sampled unified rotation curve of the Milky Way (URC26) from the central super massive black hole to the outer halo of radius ~ 300 kpc, which has the highest resolution and accuracy ever performed. The URC was decomposed into five dynamical components of the central black hole with a mass of $M_1 = 4 \times 10^6 M_{\odot}$, the core with $M_2 \simeq 3.3 \times 10^7 M_{\odot}$ (core), the bulge with $M_3 \simeq 1.1 \times 10^{10} M_{\odot}$ (bulge), disk with $M_4 \simeq 1.6 \times 10^{11} M_{\odot}$ (disk), and the dark halo with the critical mass of $M_{200} \sim 4.2 \times 10^{11} M_{\odot}$ in the critical radius $R_{200} \sim 81$ kpc. The local dark matter density near the Sun due to the dark halo alone is estimated to be $\rho_{\text{DM}}^{\text{local}} \sim 0.24 \text{ GeV cm}^{-3}$. We found a linear proportionality between the scale radius and the mass of individual components.

Acknowledgments

Data analysis was performed at the NAOJ Astronomy Data Center.

Conflict of interests

The author declares that there are no conflicts of interest.

Data availability

The rotation curve used in this paper is downloadable from the PASJ supplementary cite at "http: (to be given by PASJ)".

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