

# Dark Halos of M31 and the Milky Way – Their Dynamical Similarity –

Yoshiaki Sofue (U. Tokyo)

2015 03 24 @ MW2015, U.Tokyo

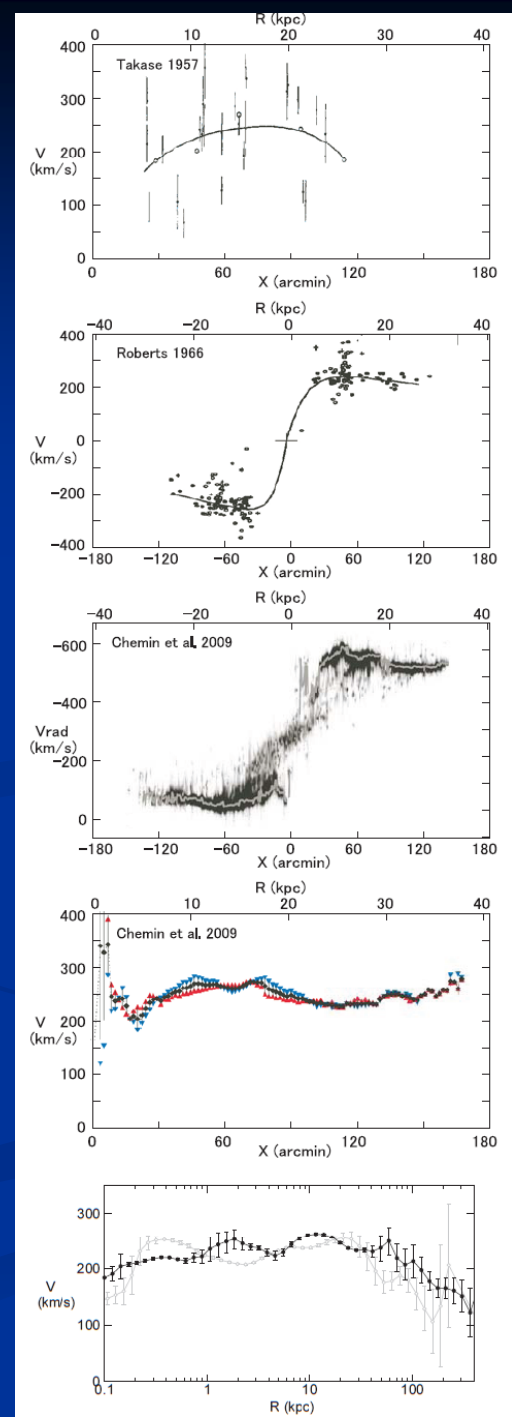
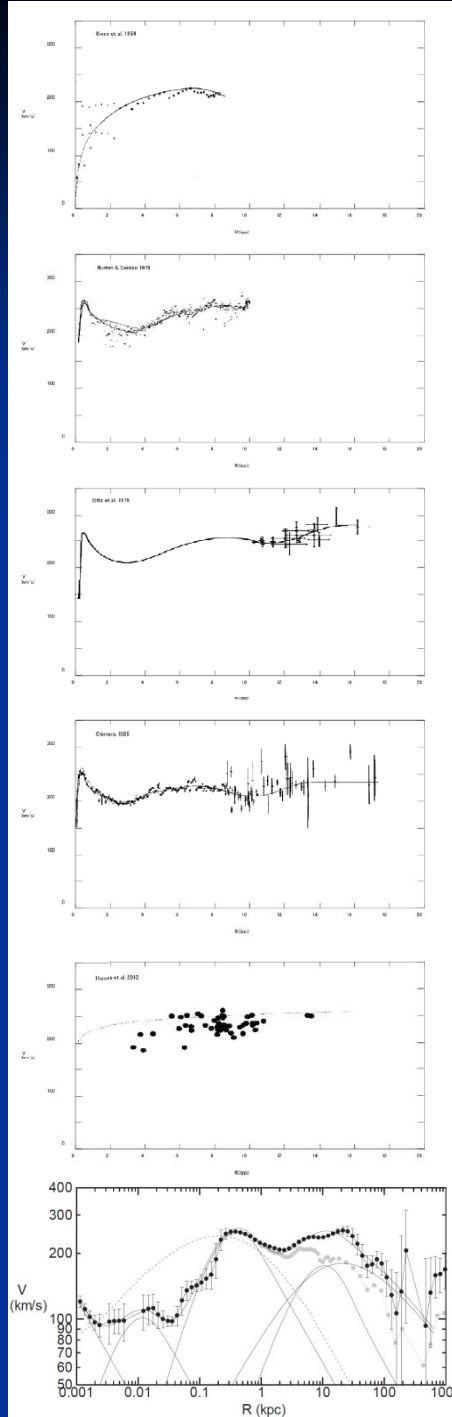
# 1. Introduction

# Progress in RC 1950's to 2015

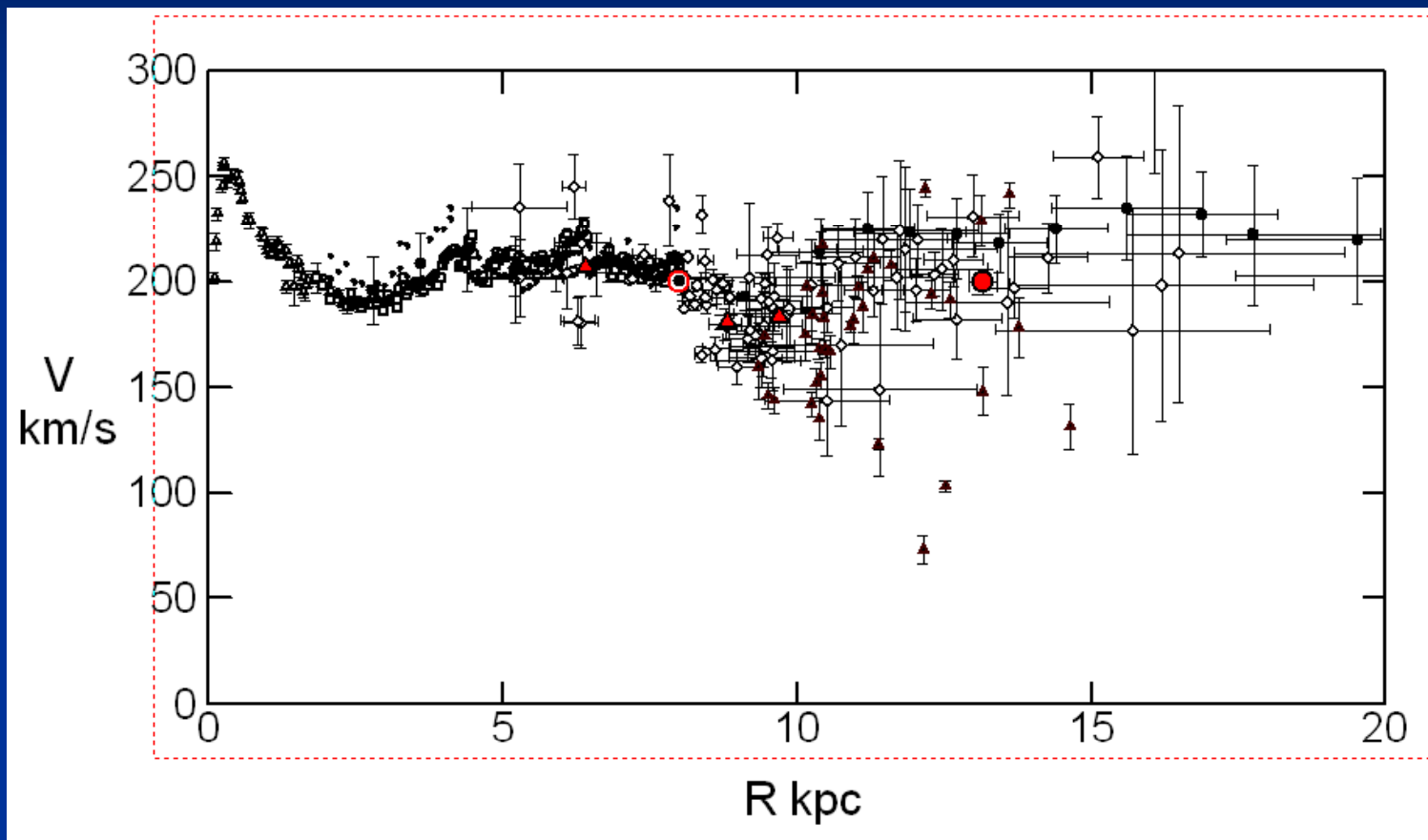
MW  
Kwee (1954) ~  
VERA

VS

M31  
Takase (1957) ~

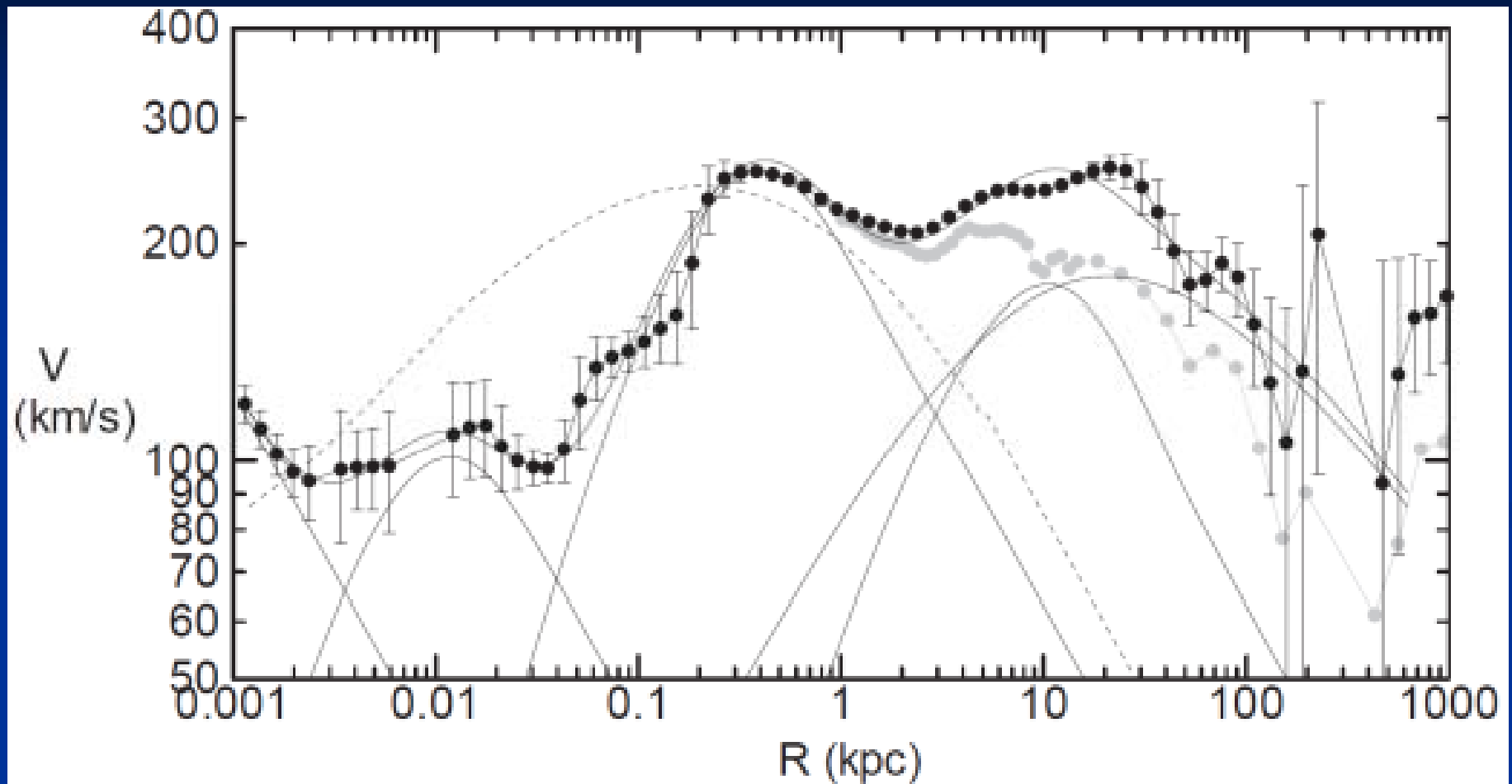


# 今までの Rotation Curve

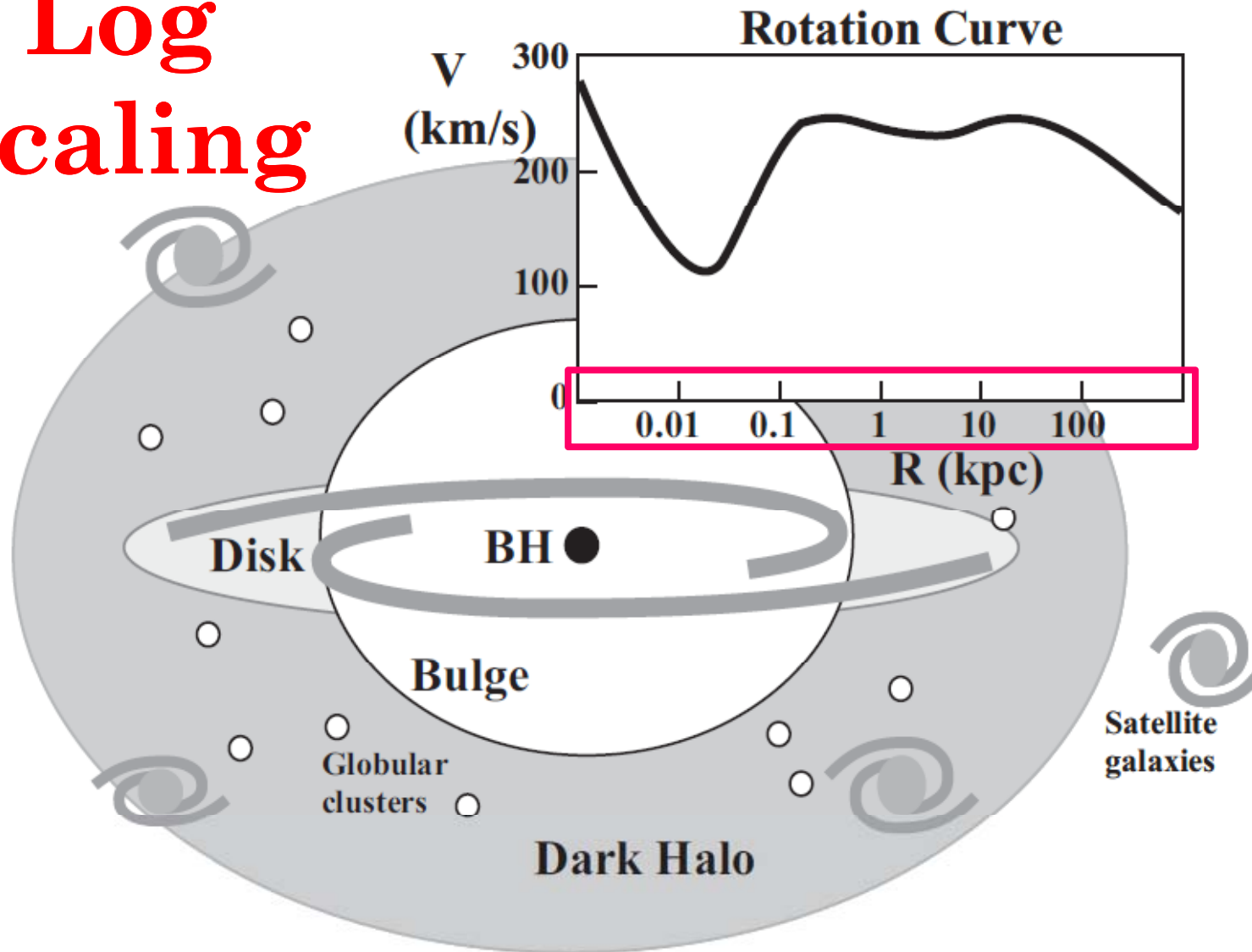


Sofue, Honma, Omodaka 2007

# これからのLog Grand RC

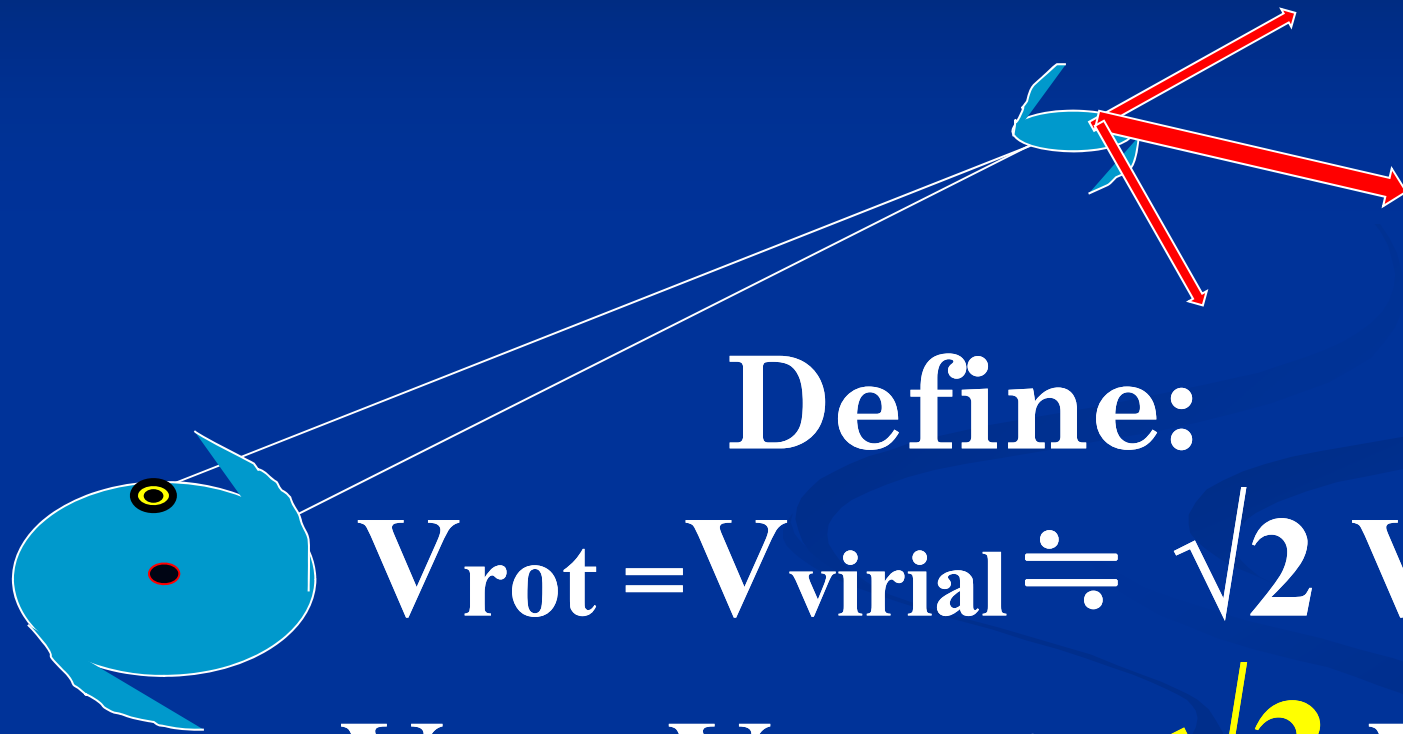


# Log Scaling



$R > 30 \text{ kpc}$

Globular clusters and satellite galaxies



Define:

$$V_{\text{rot}} = V_{\text{virial}} \doteq \sqrt{2} V_{\text{GC}}$$

$$V_{\text{rot}} = V_{\text{virial}} \doteq \sqrt{3} V_{\text{GC}}$$

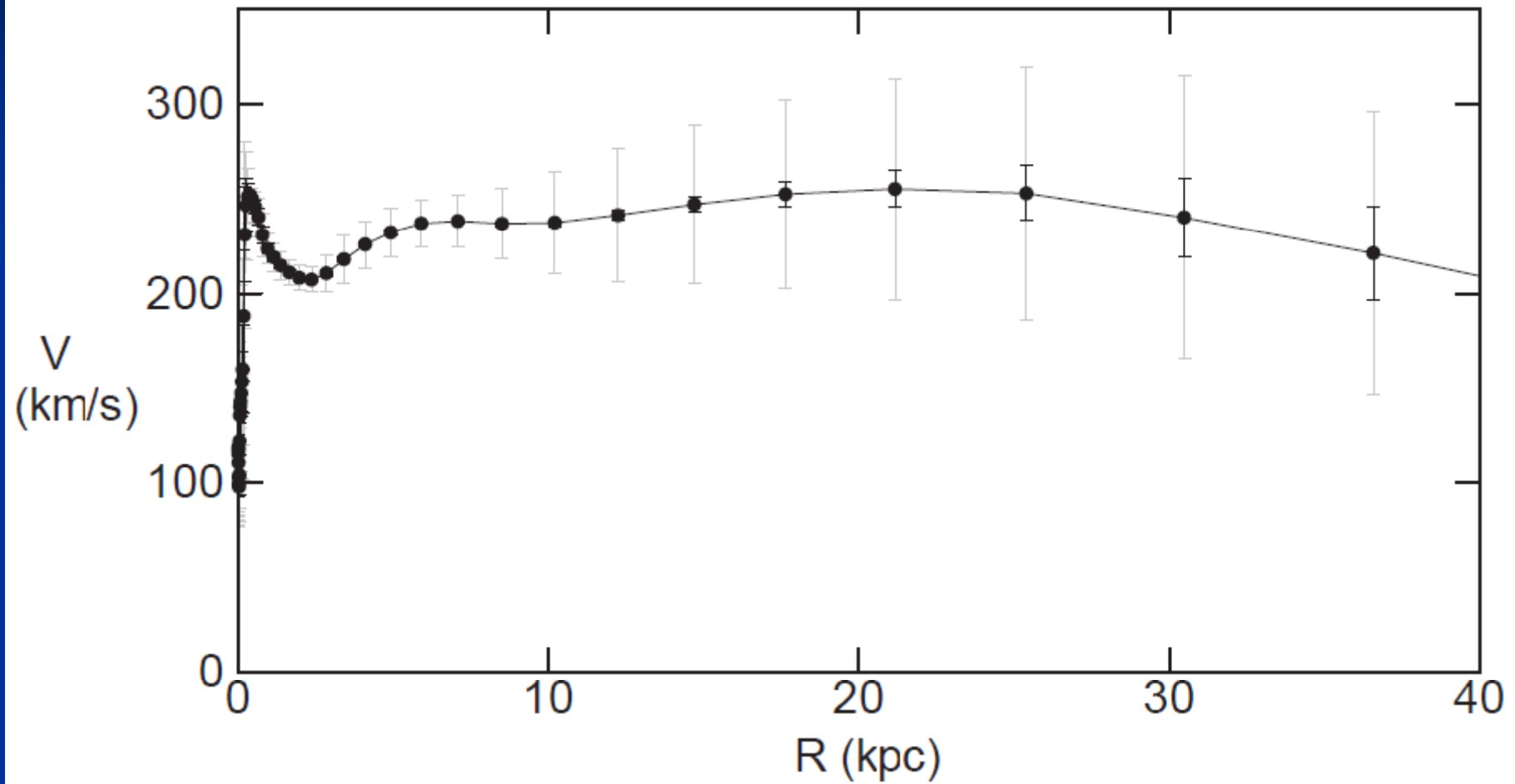
# 2. Log. Grand Rotation Curve



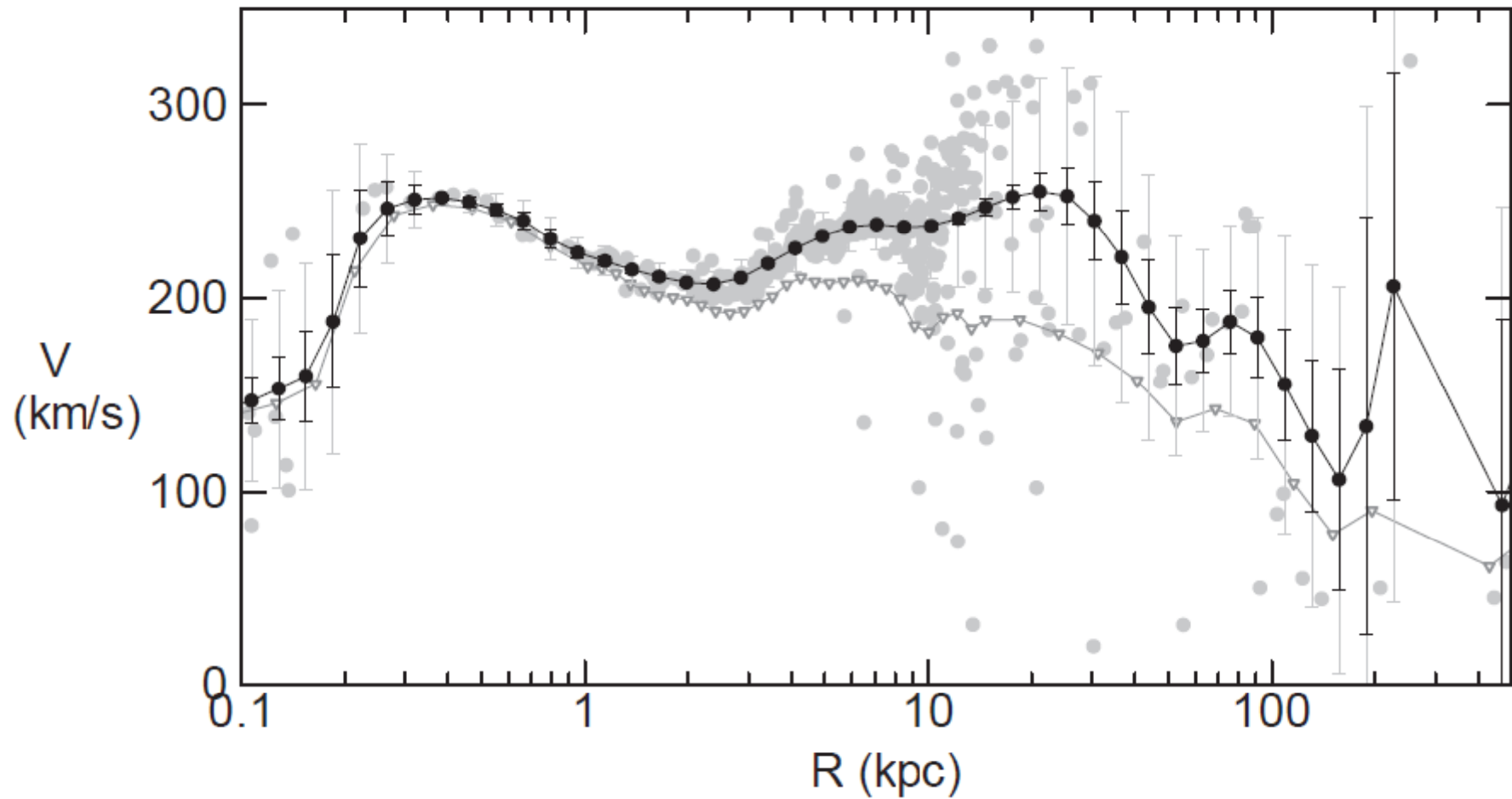
# Milky Way

A stylized graphic of the Milky Way galaxy, consisting of several overlapping, curved, light blue bands that sweep across the bottom right portion of the dark blue background.

(8 kpc, 238 km/s)



# GRC (8 kpc, 238 km/s)

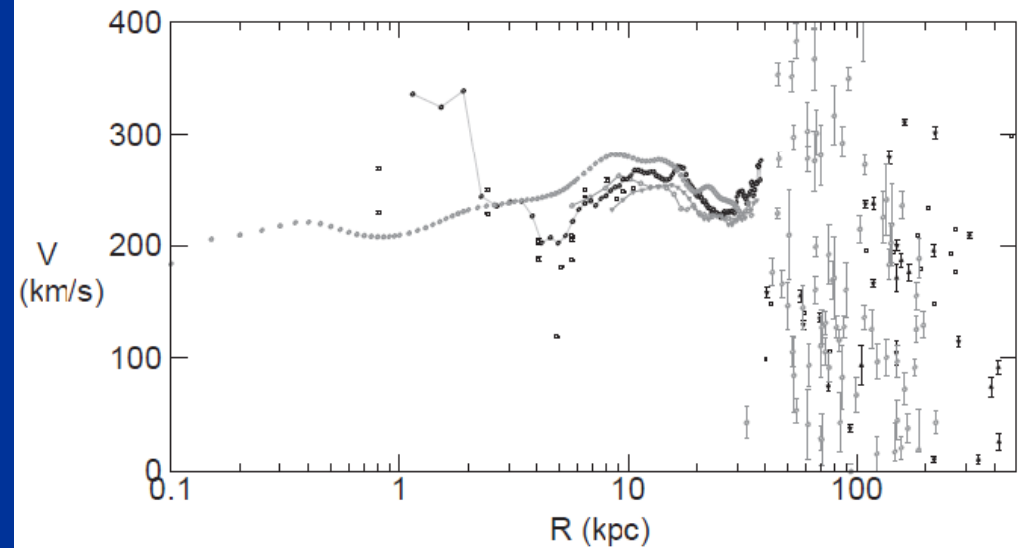
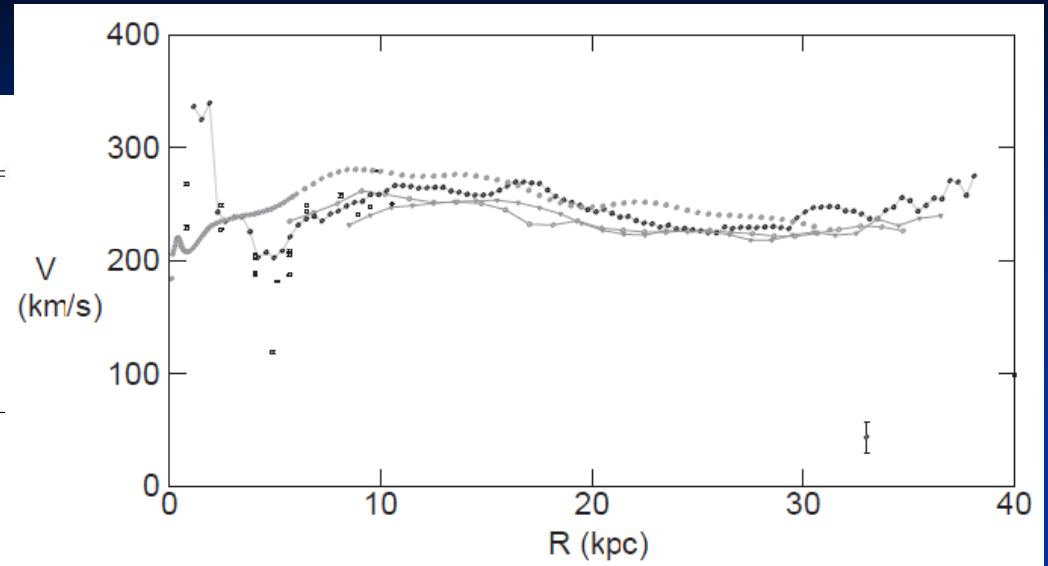


M31

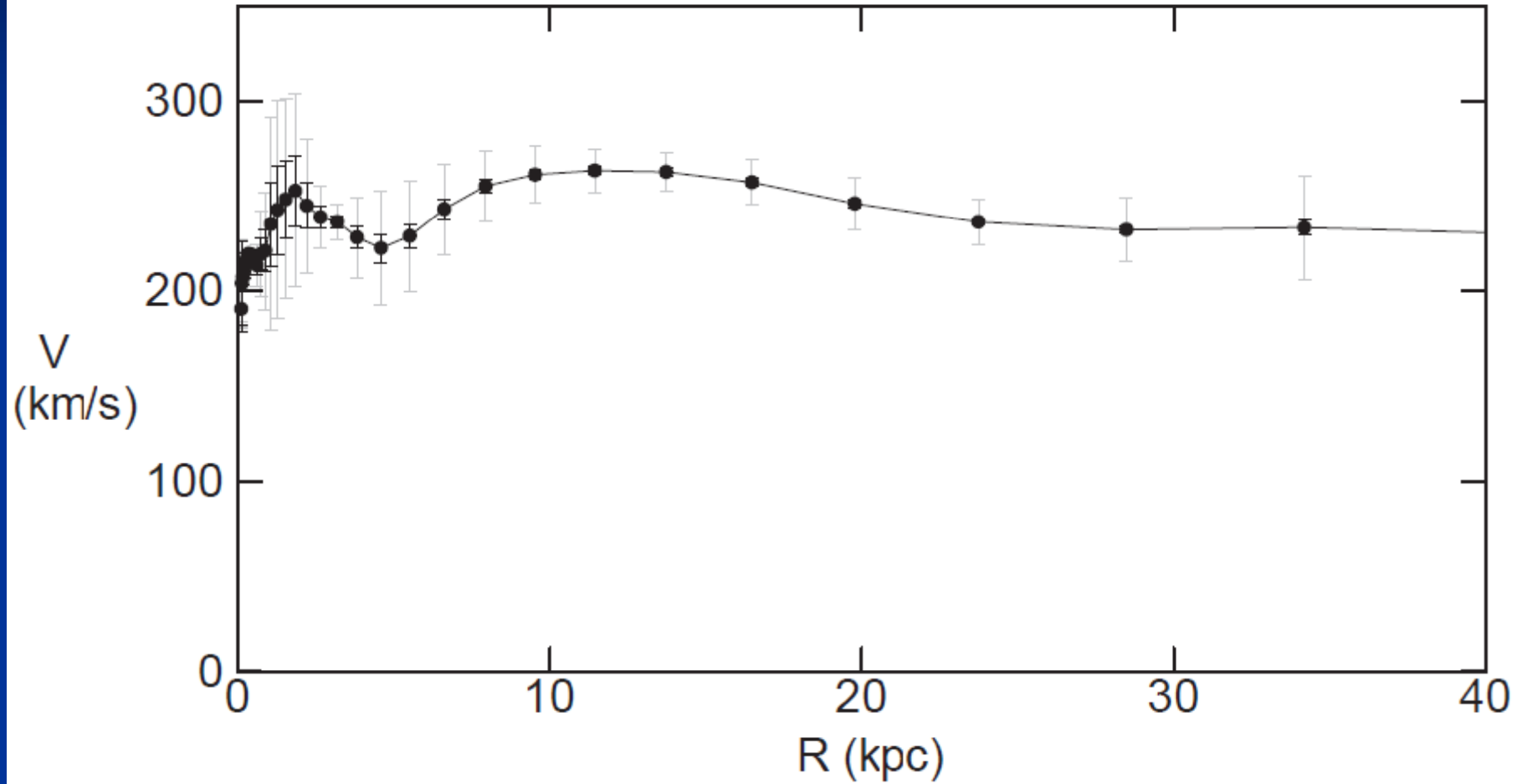
# M31

Table 1. References to the data in figure 1

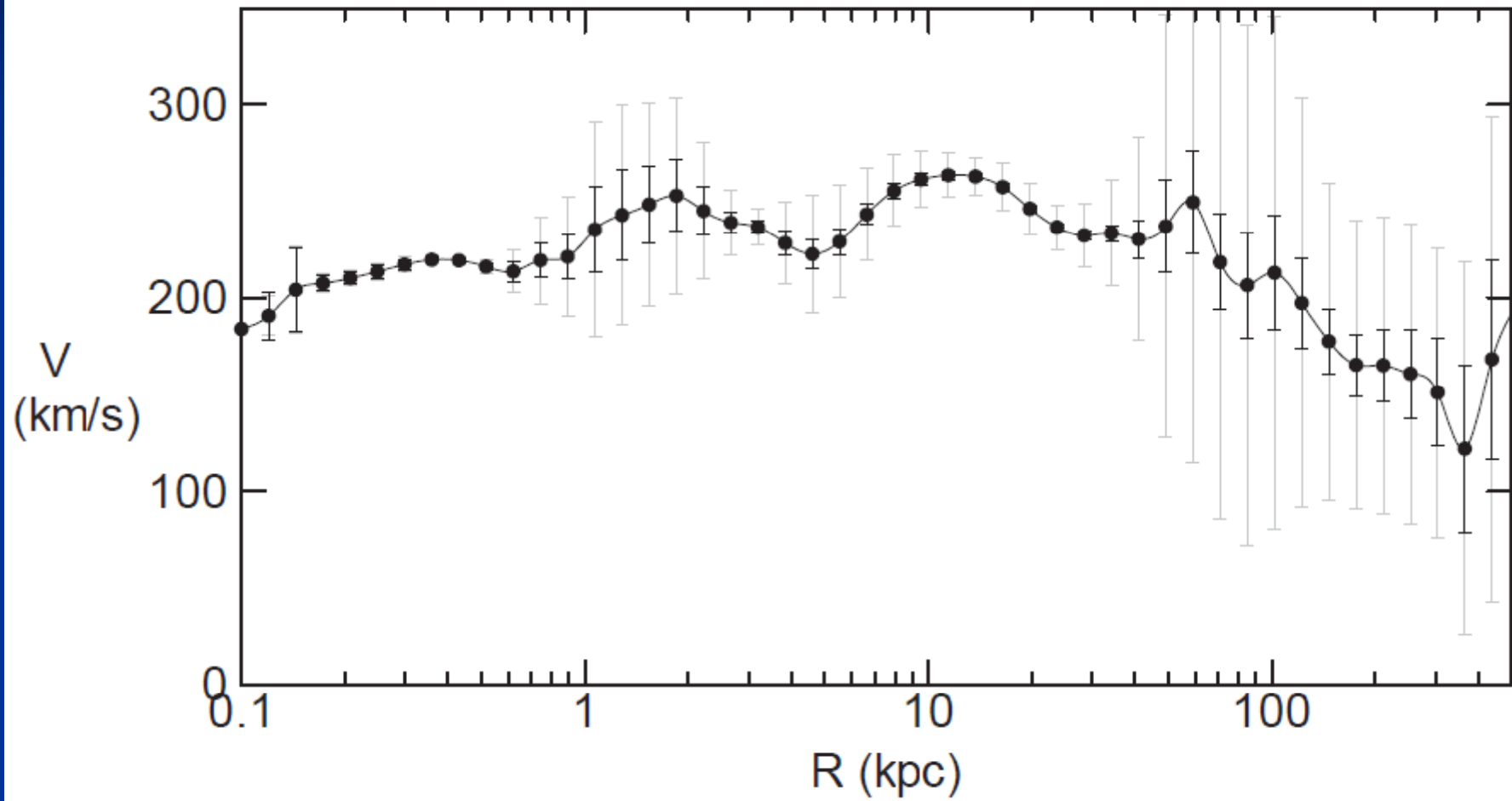
Rectangles at $R < 10$ kpc	Disk RC (CO)	Loinard et al. (1995)
Grey circles at $R < 32$ kpc	ibid (combi: HI, CO, opt)	Sofue et al. (1981, 1999)
Grey open circles linked by line	ibid (HI)	Carignan et al. (2006)
Black-grey circles linked by line	ibid (HI, CO)	Chemin et al. (2009)
Grey reverse triangles linked by line	ibid (HI)	Corbelli et al. (2010)
Rectangles at $R > 40$ kpc	galaxies around M31	Metz et al. (2007)
Triangles with bars	ibid	van der Marel et al. (2008)
Reverse triangle at $R > 40$ kpc	ibid	Tollerud et al. (2012)
Open circles with bars	Globular clusters	Veljanovski et al. (2014)



# Grand Rotation Curve



# Grand Rotation Curve



# 3. Deconvolution into Bulge, Disk, & Dark Halo



# (1) Bulge de Vaucouleurs:

$$\Sigma_b(r) = \lambda_b B_b(r) = \Sigma_{be} \exp \left[ -\kappa \left( \left( \frac{r}{R_b} \right)^{1/4} - 1 \right) \right]$$

$$\rho(r) = \frac{1}{\pi} \int_r^\infty \frac{d\Sigma_b(x)}{dx} \frac{1}{\sqrt{x^2 - r^2}} dx$$

$$M_b(R) = 4\pi \int_0^R r^2 \rho(r) dr. \quad M_b = 22.665 a_b^2 \Sigma_{be}$$

$$V_b(R) = \sqrt{\frac{GM_b(R)}{R}}.$$

## (2) Disk: Exponential

$$V_d(R) = \sqrt{\frac{GM_d}{a_d}} \mathcal{D}(X),$$

where  $X = R/a_d$ , and

$$\mathcal{D}(X) = (X/\sqrt{2}) \times \\ \times [\{I_0(X/2)K_0(X/2) - I_1(X/2)K_1(X/2)\}]^{1/2}$$

### (3) Dark Halo

## Navarro-Frenk-White (1996)

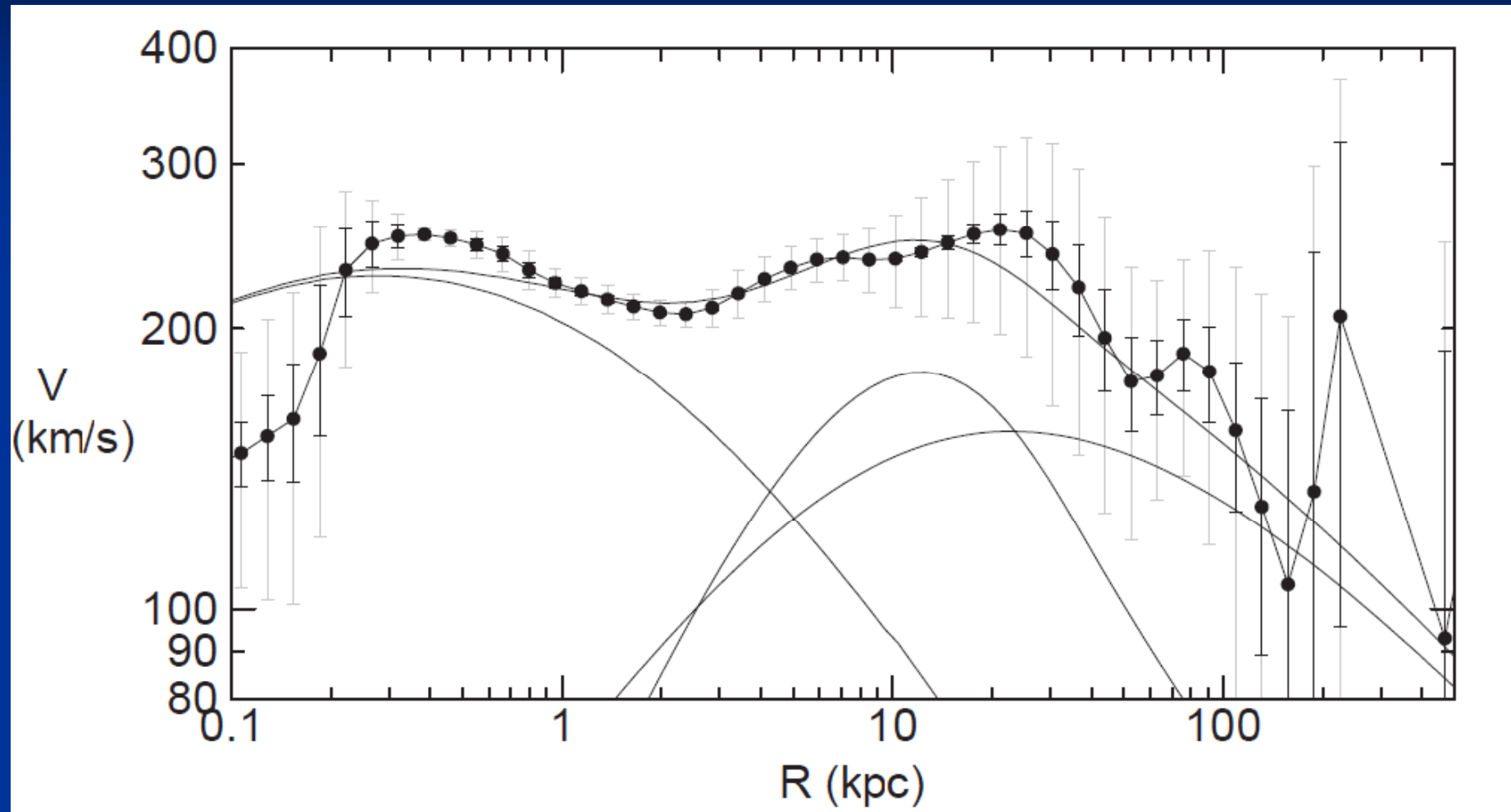
## Density Profile

$$X = R/h$$

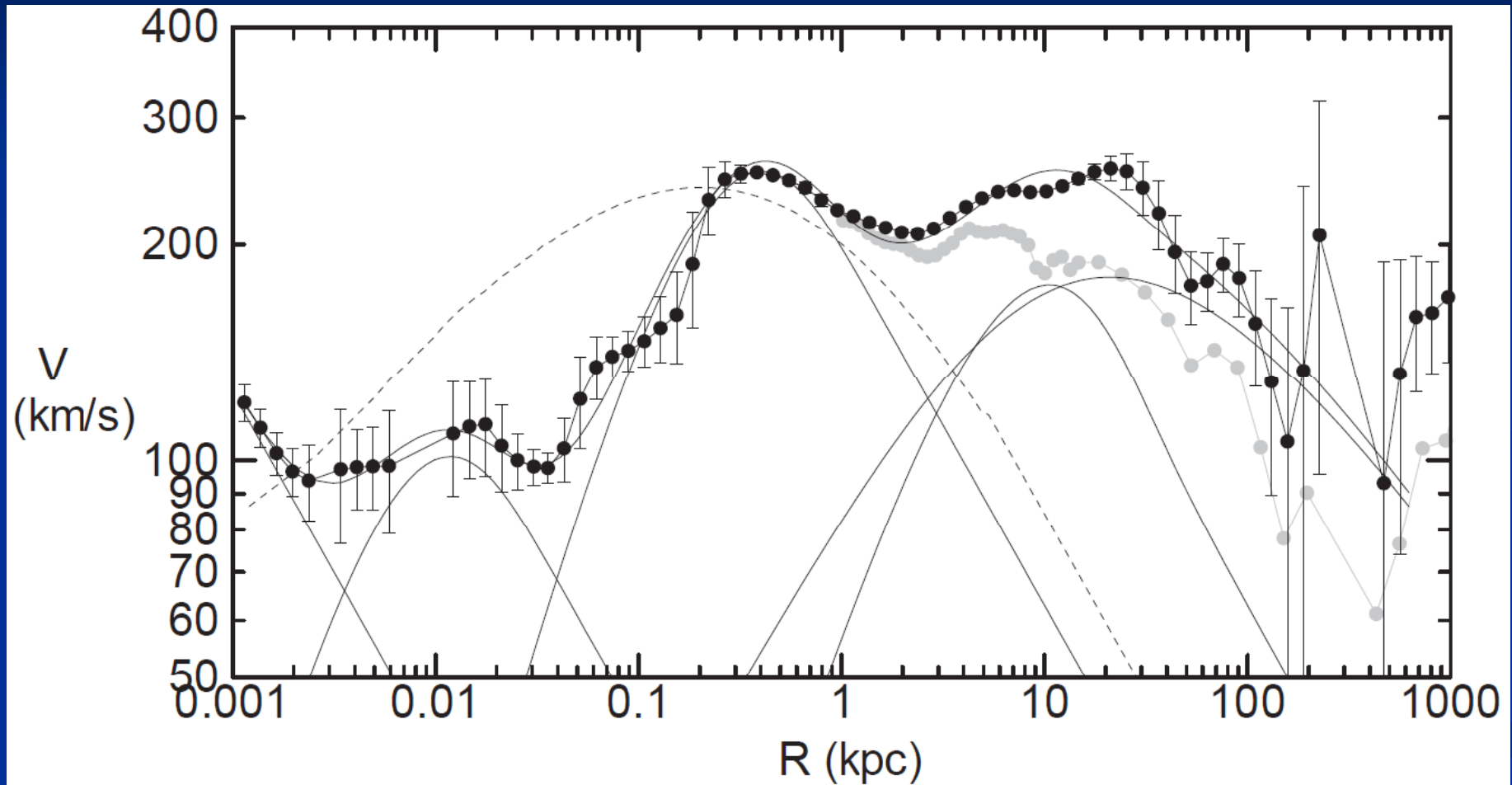
$$\rho(R) = \frac{\rho_0}{X(1+X)^2},$$

$$M_h(R) = 4\pi\rho_0h^3 \left\{ \ln(1+X) - \frac{X}{1+X} \right\}.$$

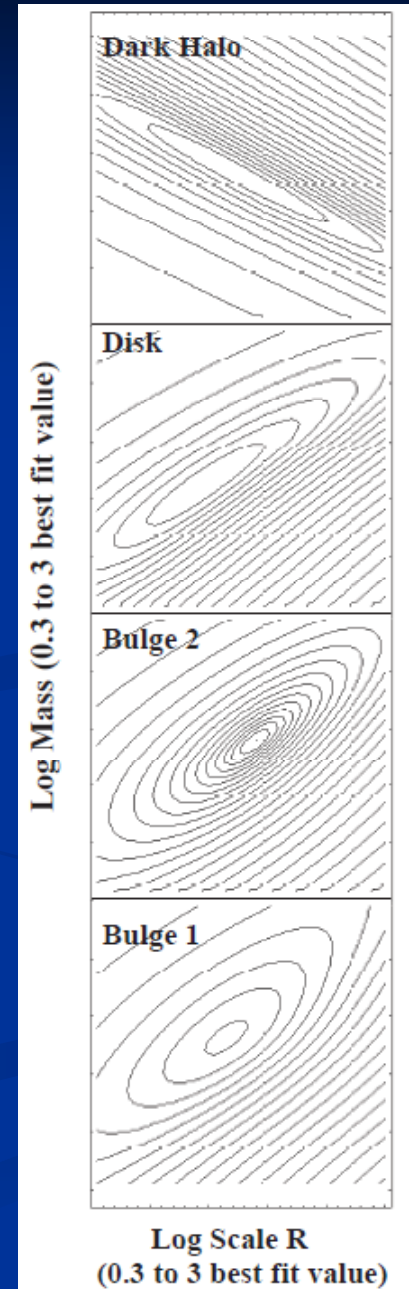
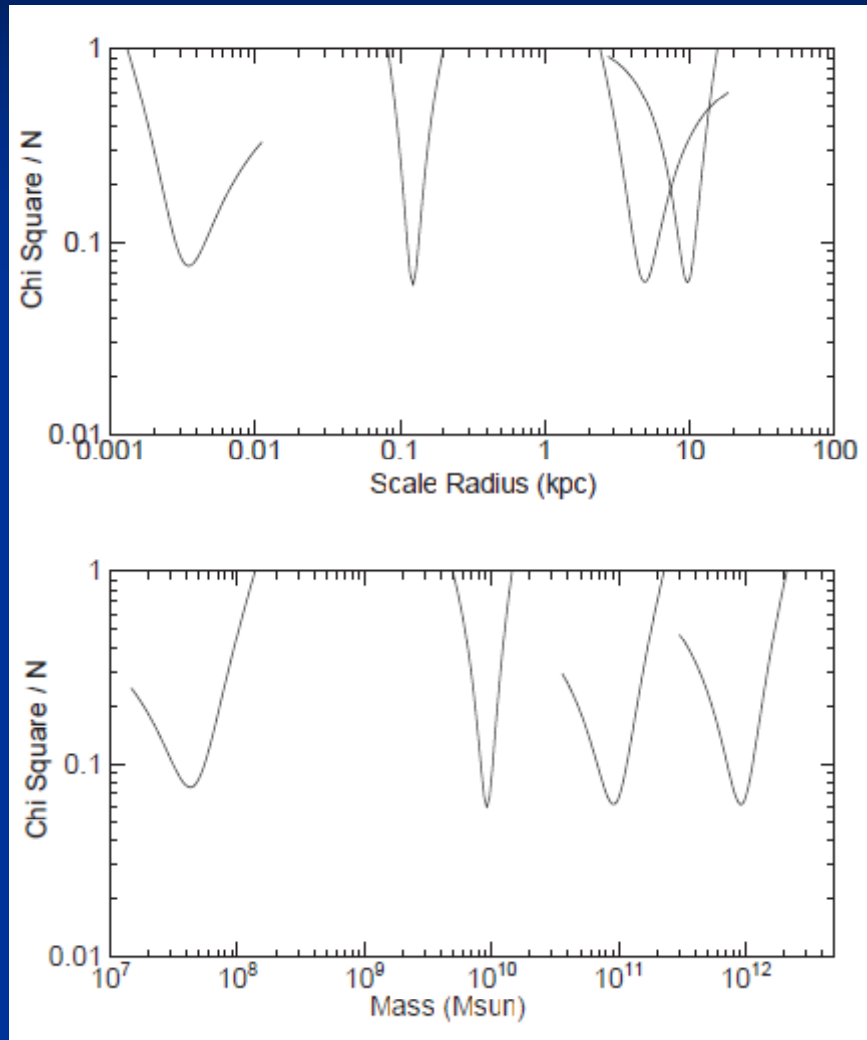
# MW GRC Decomposition



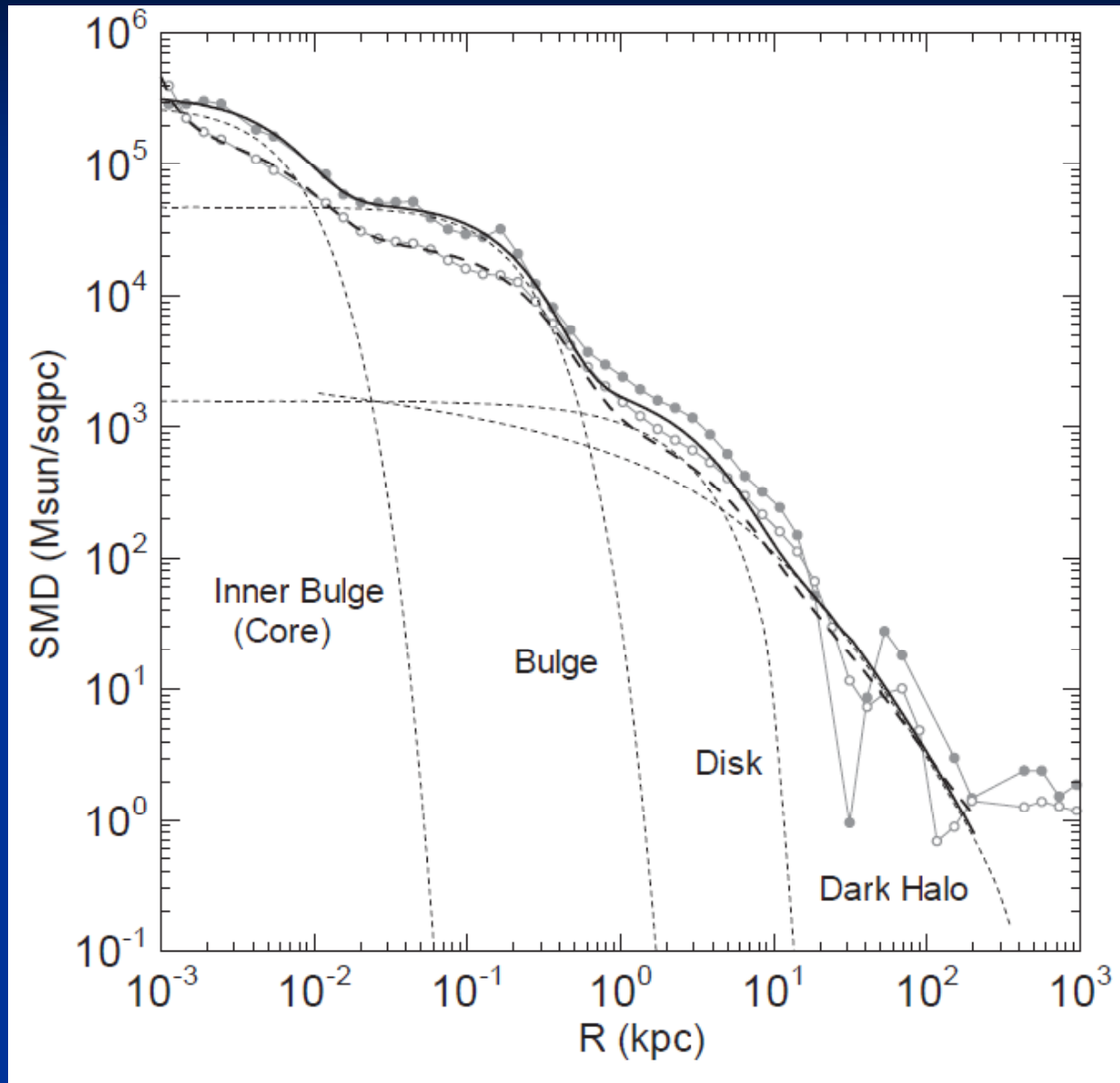
# Two-Expo. Bulge Decomposition



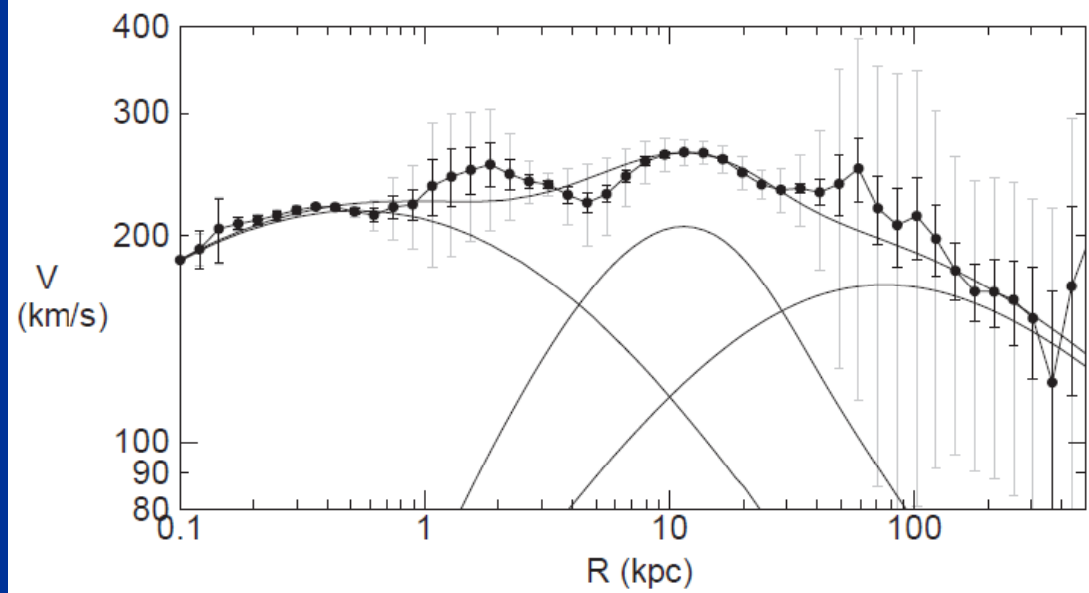
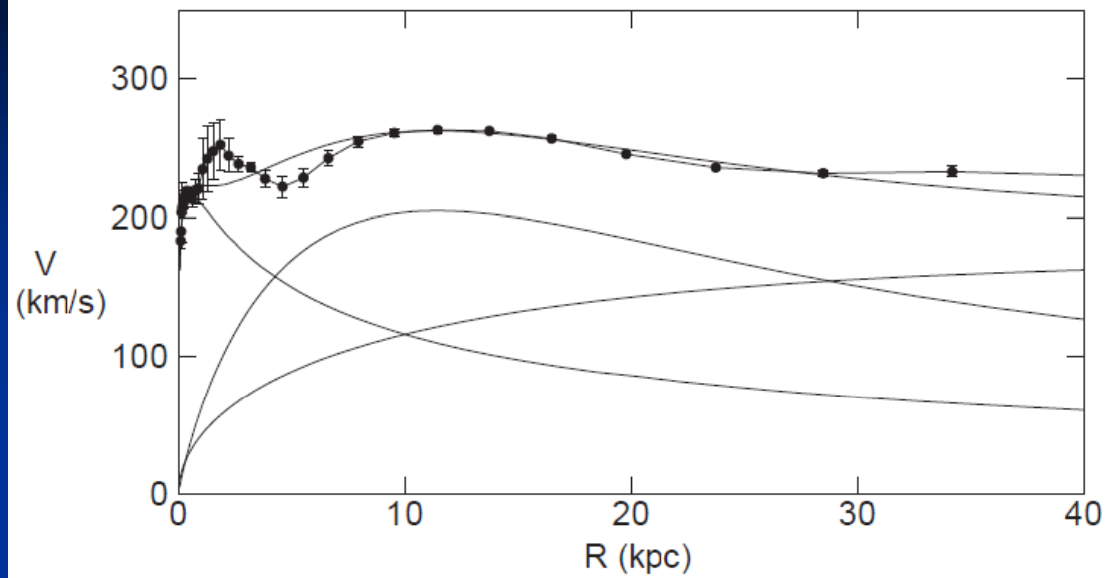
# Chi-Square Fitting



# SMD : Obs vs Model

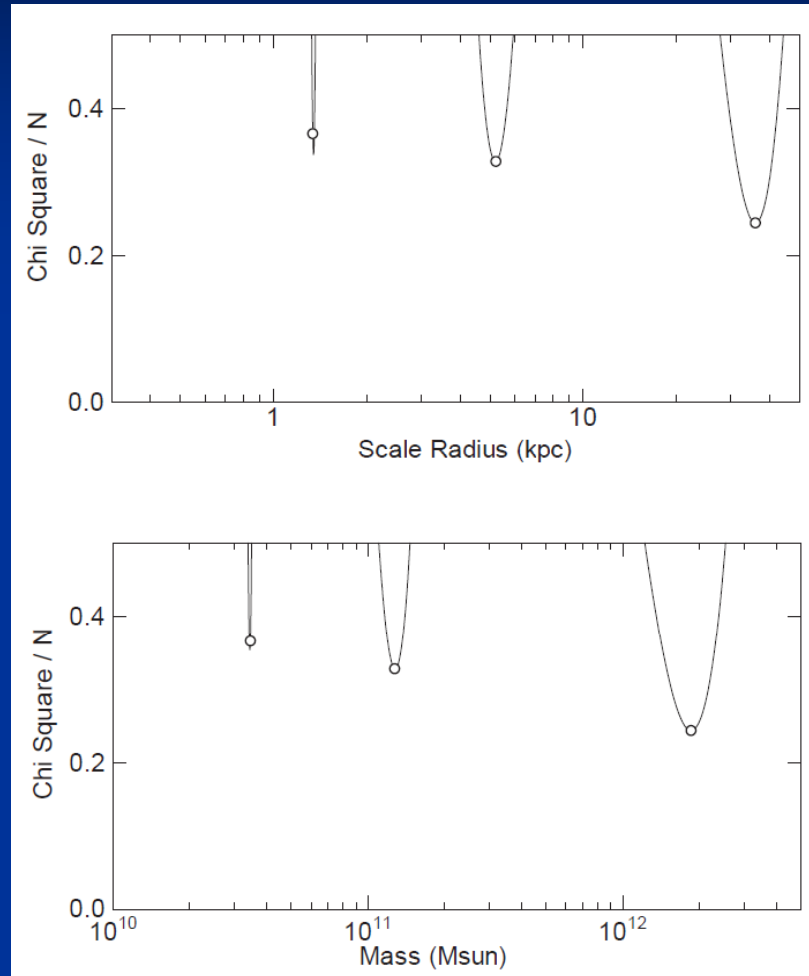


# M31 Fitting



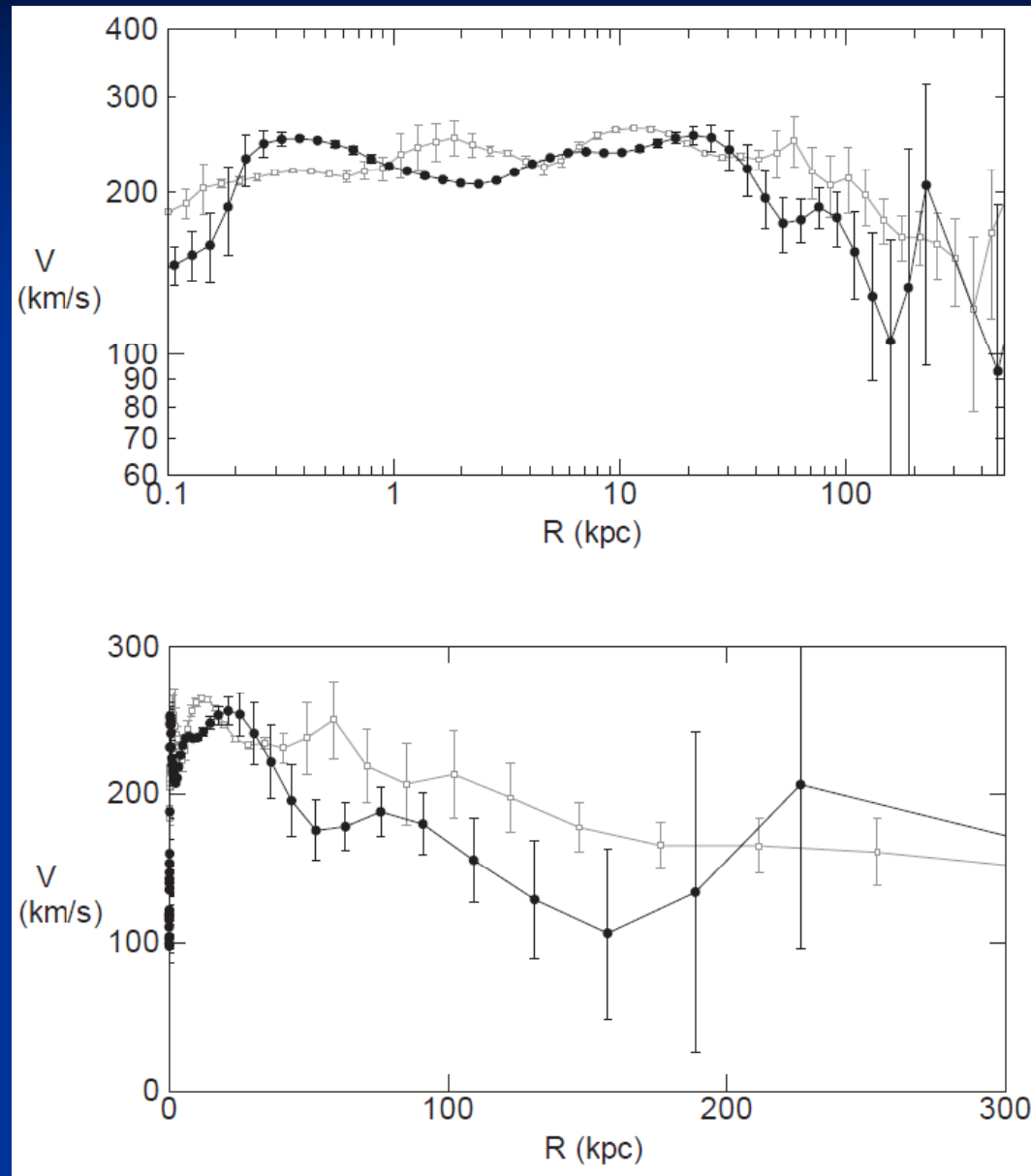


# Chi square map

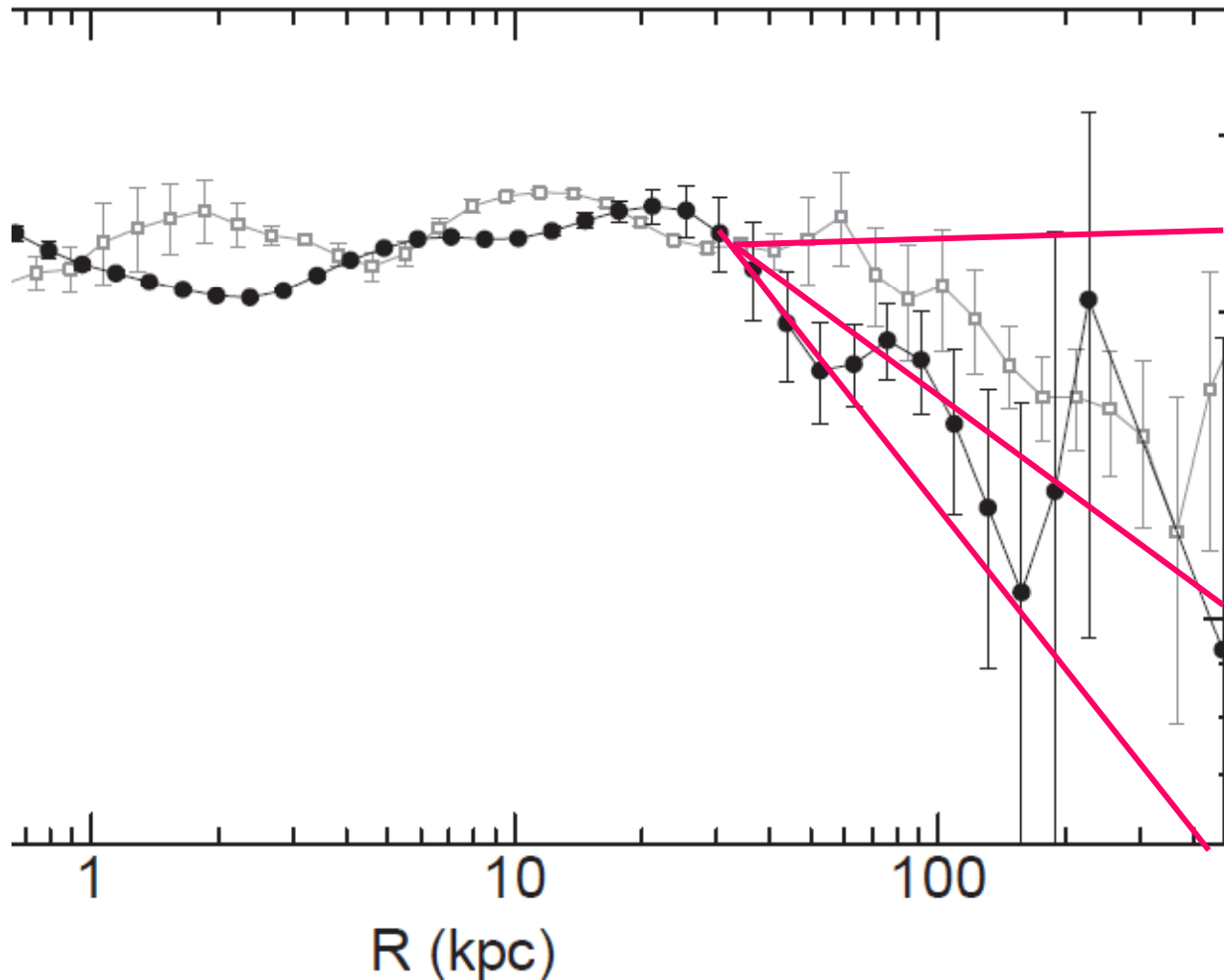


# 5. Dark Halo Similarity in MW and M31

# Log RC: MW / M31 Dark Halos



# Universal Dark Halo RC

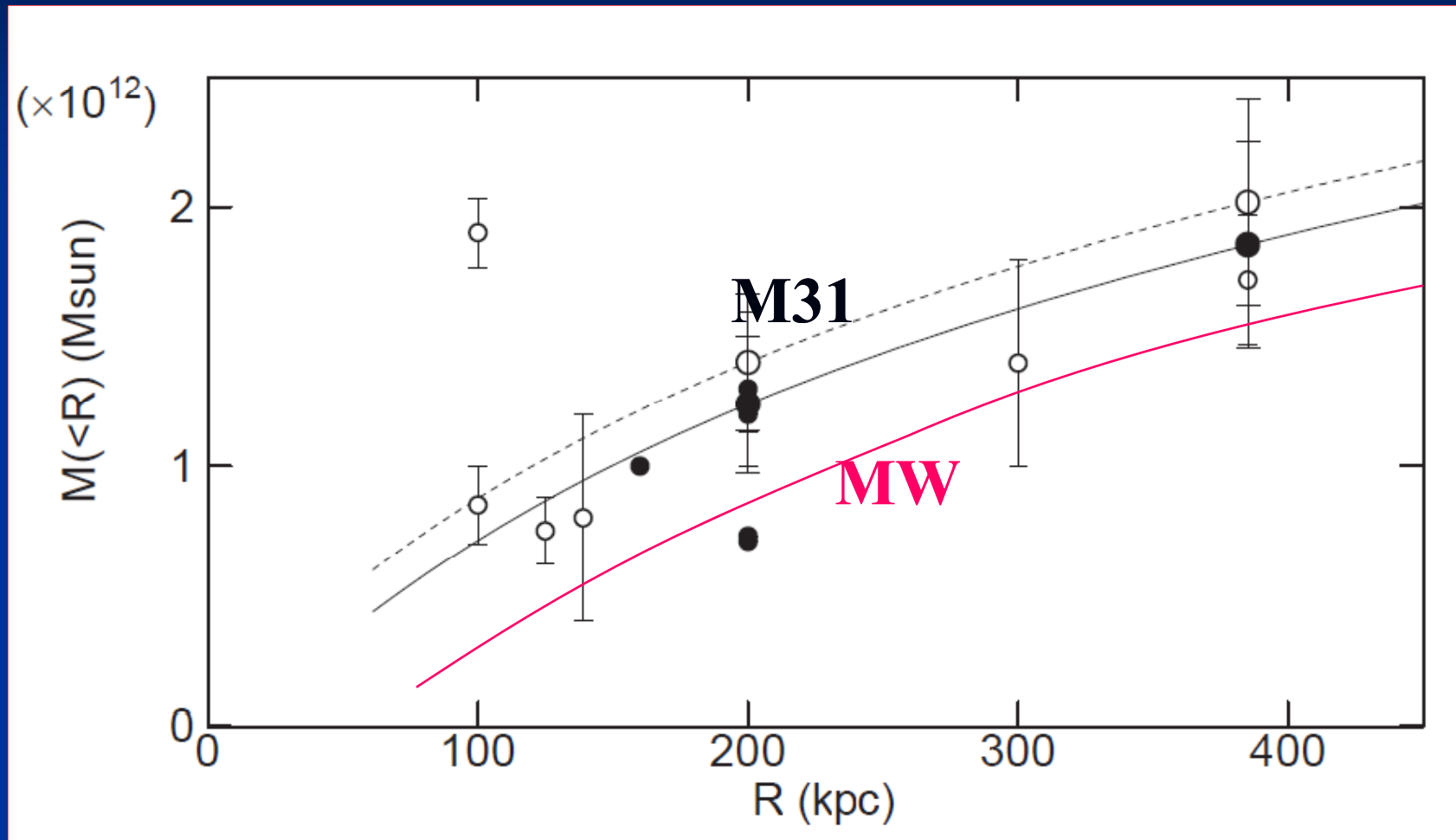


Isotherma

NFW

Kepler

# DH Mass: M31 vs MW



# Best Fit Parameters

Table 2. The best fit dynamical parameters for M31 and the Galaxy†

Component	Parameter	M31	Milky Way
Bulge	$a_b$ (kpc)	$1.34 \pm 0.02$	$0.72 \pm 0.07$
	$M_b(10^{11} M_\odot)$	$0.35 \pm 0.00$	$0.20 \pm 0.02$
Disk	$a_d$ (kpc)	$5.23 \pm 0.32$	$5.68 \pm 1.21$
	$M_d(10^{11} M_\odot)$	$1.27 \pm 0.08$	$1.10 \pm 0.40$
NFW Halo	$h$ (kpc)	$36.01 \pm 2.20$	$10.56 \pm 2.86$
	$\rho_0(10^{-3} M_\odot \text{pc}^{-3})$	$2.05 \pm 0.23$	$18.46 \pm 7.55$
	$\rho_{8 \text{ kpc}}(10^{-3} M_\odot \text{pc}^{-3})$	$6.17 \pm 0.68$	$7.89 \pm 3.22$
	$-(\text{GeV cm}^{-3})$	$0.23 \pm 0.03$	$0.30 \pm 0.12$
	$M_{h:200}(10^{11} M_\odot)$	$12.40 \pm 2.65$	$5.58 \pm 5.07$
	$M_{h:385}(10^{11} M_\odot)$	$18.55 \pm 3.96$	$7.24 \pm 6.58$
Total Mass	$M_{\text{tot}:200}(10^{11} M_\odot)$	$14.02 \pm 2.65$	$6.88 \pm 5.09$
	$M_{\text{tot}:385}(10^{11} M_\odot)$	$20.17 \pm 3.96$	$8.54 \pm 6.59$

# Conclusion and Implication

1. GRC MW similar to M31.
2. NFW is a good model.  
(vs Isothermal, Plummer)
3. Assume NFW universal.
4. Determine DH in  $\sim 100$  galaxies.
5. Statistics: Baryonic Bulge, Disk,  
vs Dark Halo.

For references, visit

[http://www.ioa.s.u-tokyo.ac.jp/  
~sofue/h-rot.htm](http://www.ioa.s.u-tokyo.ac.jp/~sofue/h-rot.htm)