

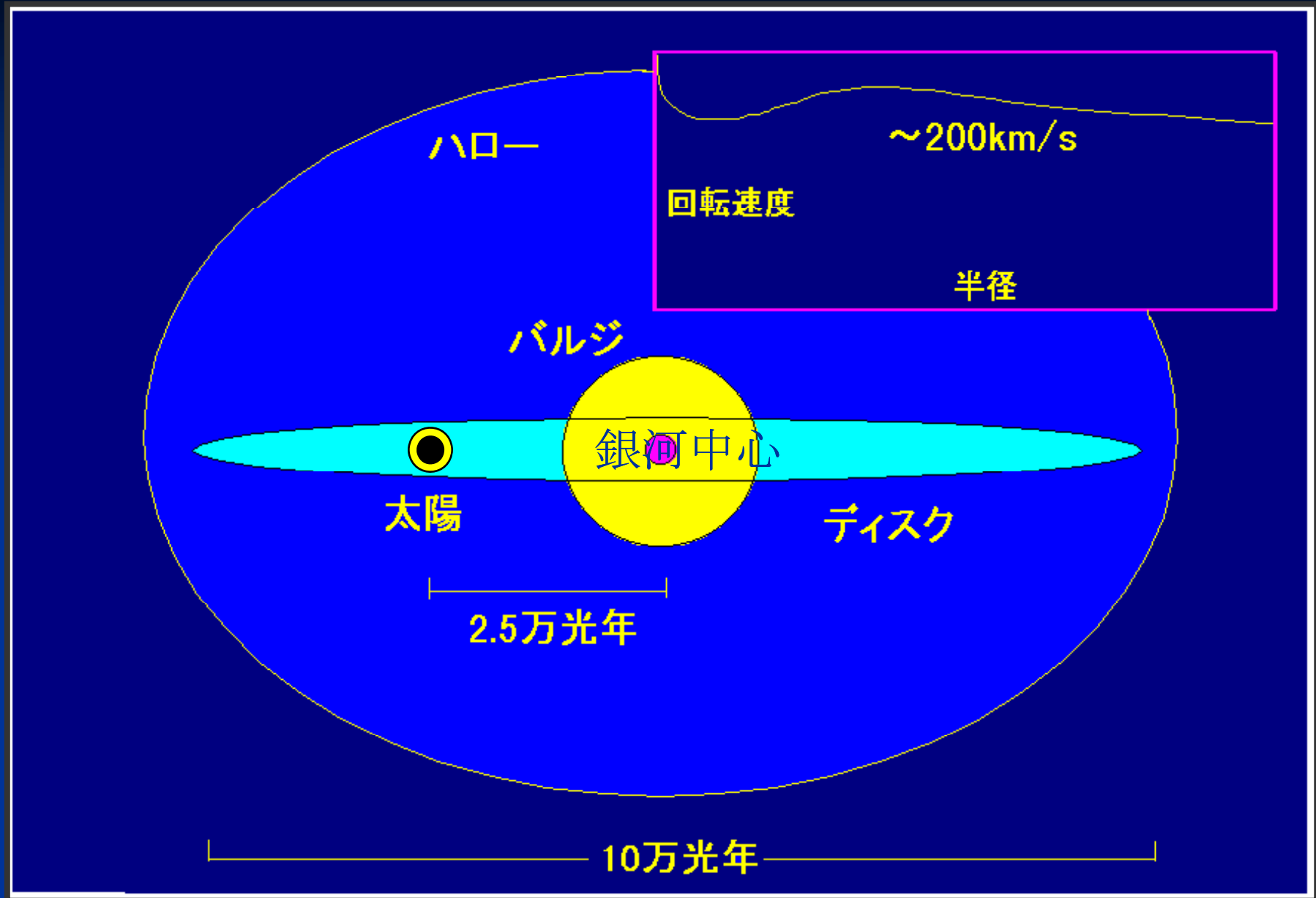
# Galactic Center Rotation Curve and Mass

Yoshiaki Sofue (Meisei Uni.)

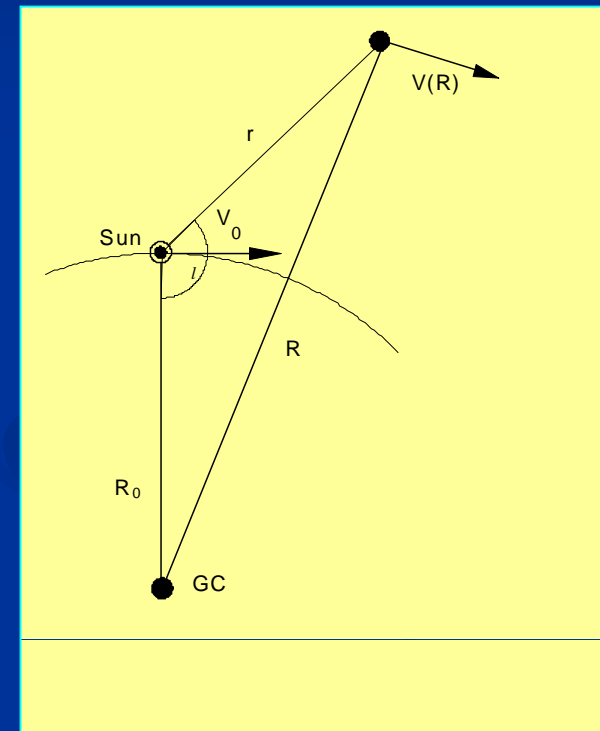
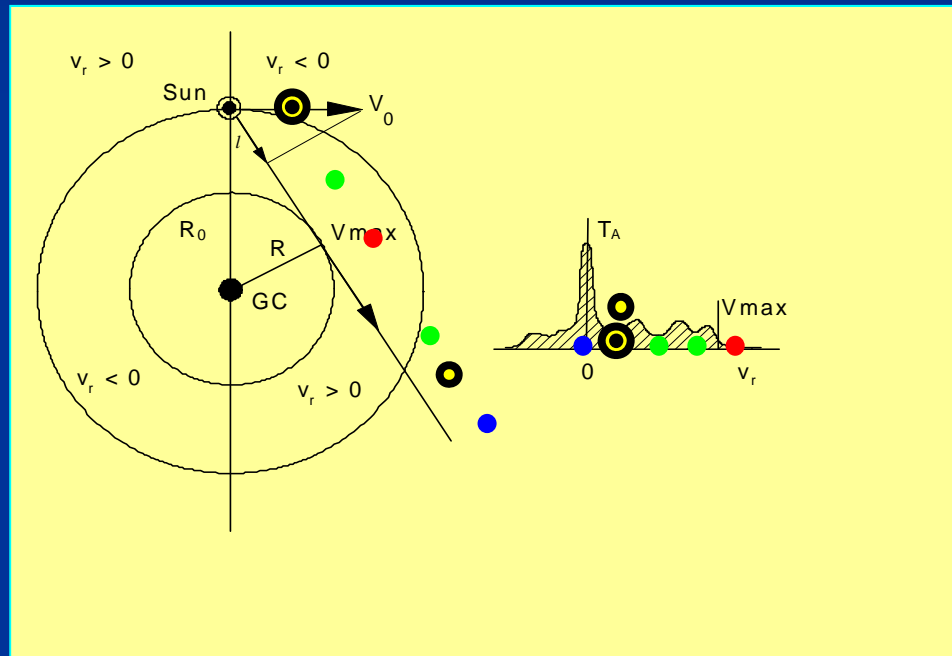
2013 03 28 @ Nagoya University

1. Log Rotation Curve
2. Mass models
3. Galactic Center RC
4. BH - Bulge – Disk -DH

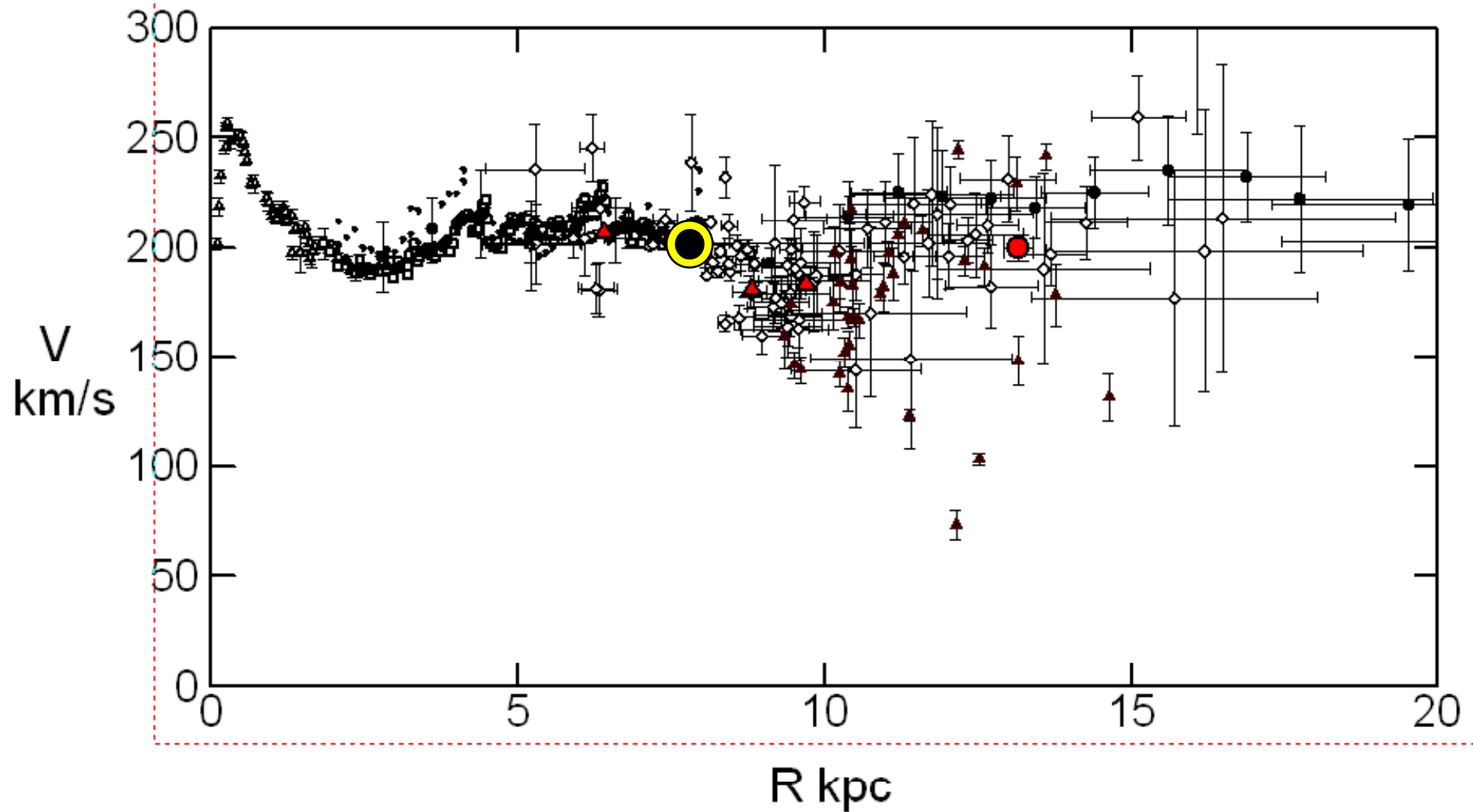
# 1. Rotation Curve



# Rotation velocities inside/outside Solar Circle



# Solar Circular Velocity $V_0=200$ km/s @ $R_0=8$ kpc



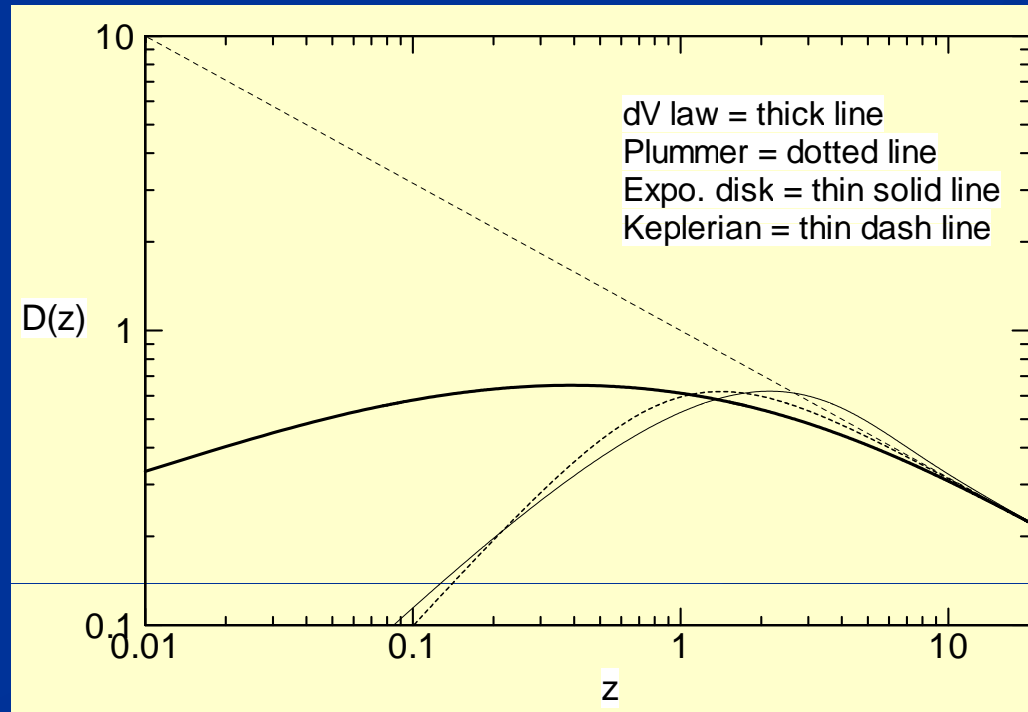
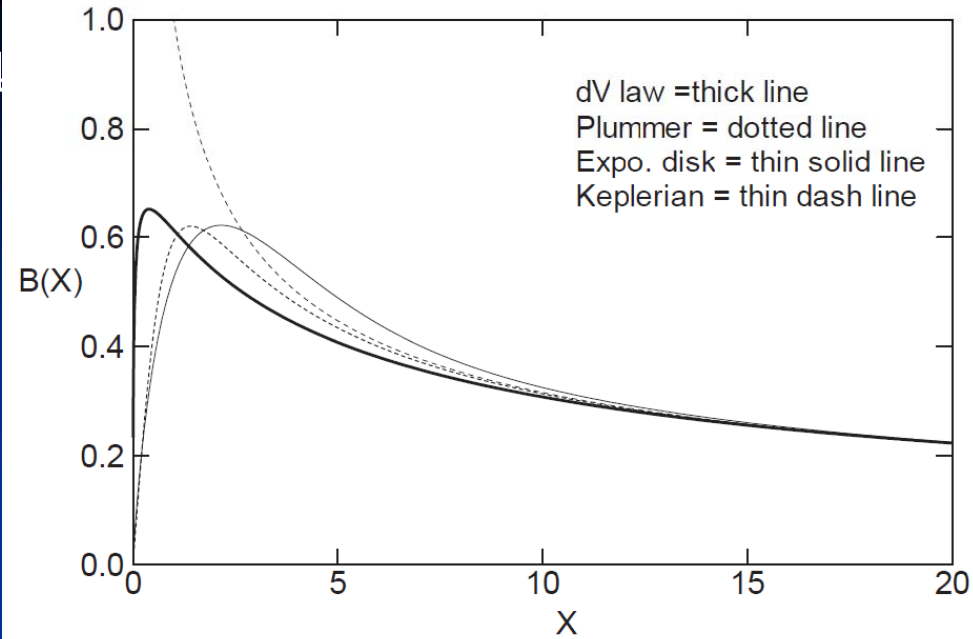
# 2. Mass Model

# RC Fitting by

- (1) Bulge: de Vaucouleurs Law
- (2) Disk: Exponential
- (3) Dark Halo: NFW



$\rho \propto \exp(-r^{1/4})$   
Expo.  
Plummer  
Kepler



# (1) Bulge de Vaucouleurs: $\exp(-r^{1/4})$

$$\Sigma_b(r) = \lambda_b B_b(r) = \Sigma_{be} \exp \left[ -\kappa \left( \left( \frac{r}{R_b} \right)^{1/4} - 1 \right) \right]$$

$$\rho(r) = \frac{1}{\pi} \int_r^\infty \frac{d\Sigma_b(x)}{dx} \frac{1}{\sqrt{x^2 - r^2}} dx$$

$$M_b(R) = 4\pi \int_0^R r^2 \rho(r) dr.$$

$$V_b(R) = \sqrt{\frac{GM_b(R)}{R}}.$$

## (2) Disk: Exponential

$$V_d(R) = \sqrt{\frac{GM_d}{a_d}} \mathcal{D}(X),$$

where  $X = R/a_d$ , and

$$\begin{aligned} \mathcal{D}(X) &= (X/\sqrt{2}) \times \\ &\times [\{I_0(X/2)K_0(X/2) - I_1(X/2)K_1(X/2)\}]^{1/2} \end{aligned}$$

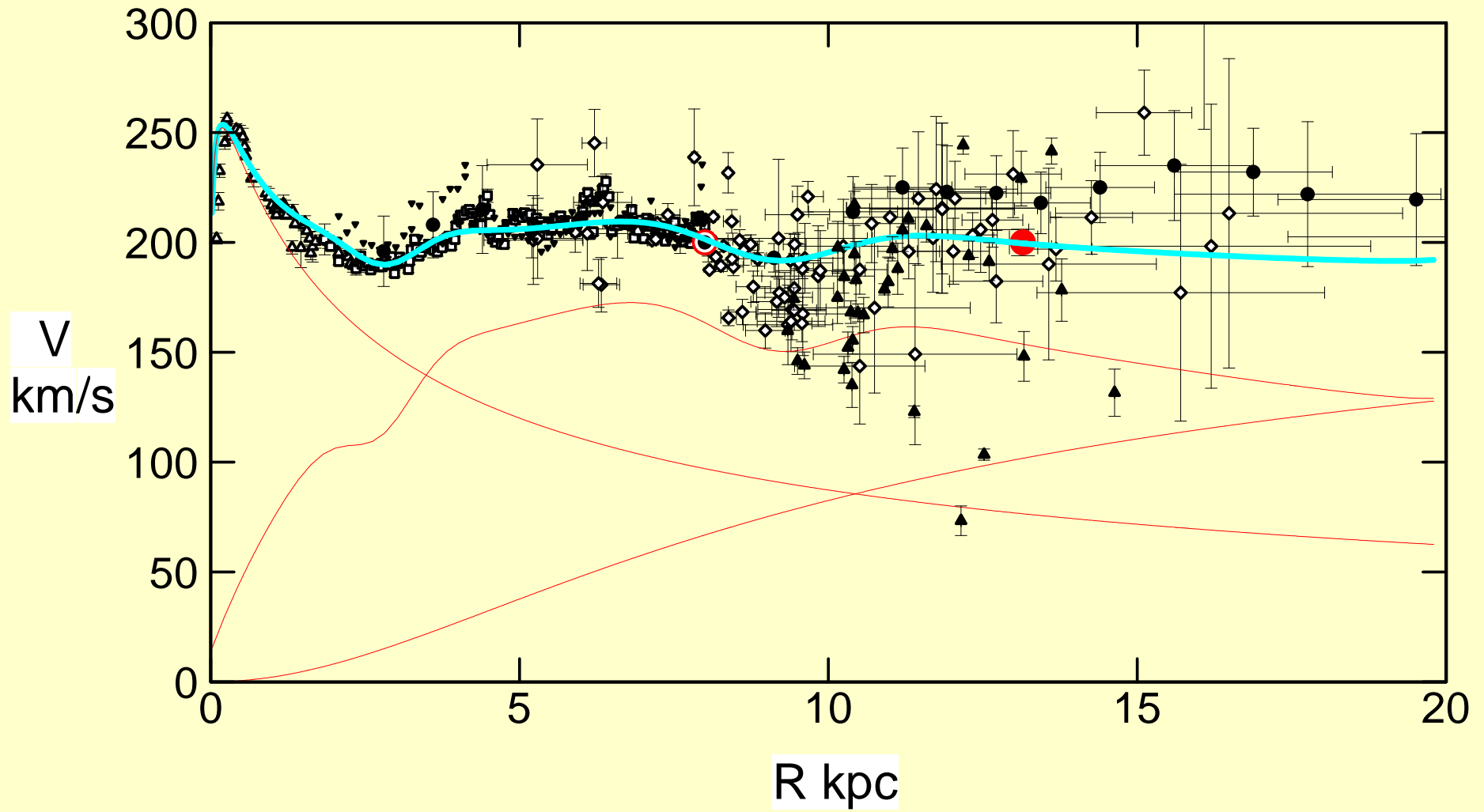
### (3) Dark Halo NFW Density Profile

$$X = R/h$$

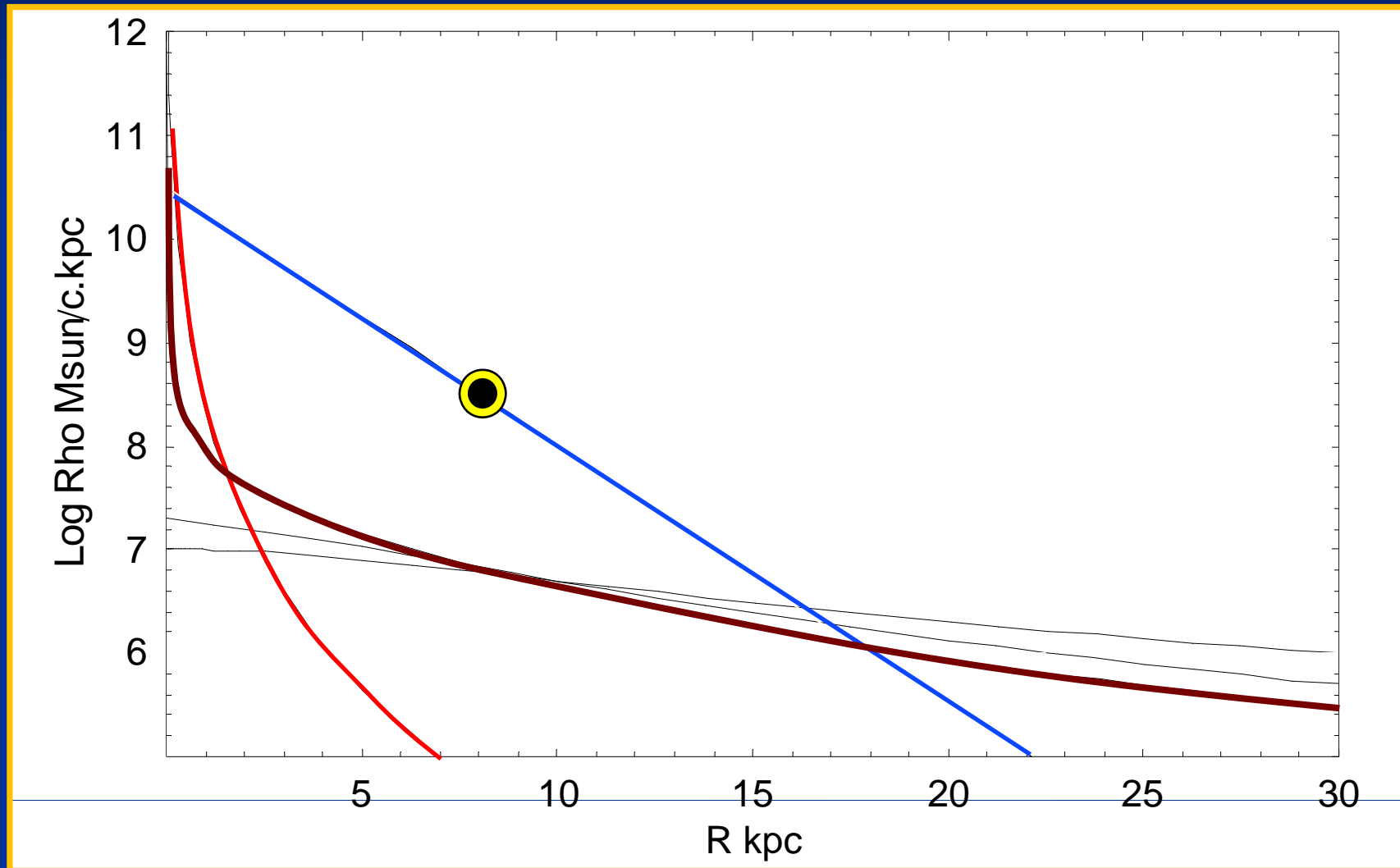
$$\rho(R) = \frac{\rho_0}{X(1+X)^2},$$

$$M_h(R) = 4\pi\rho_0h^3 \left\{ \ln(1+X) - \frac{X}{1+X} \right\}.$$

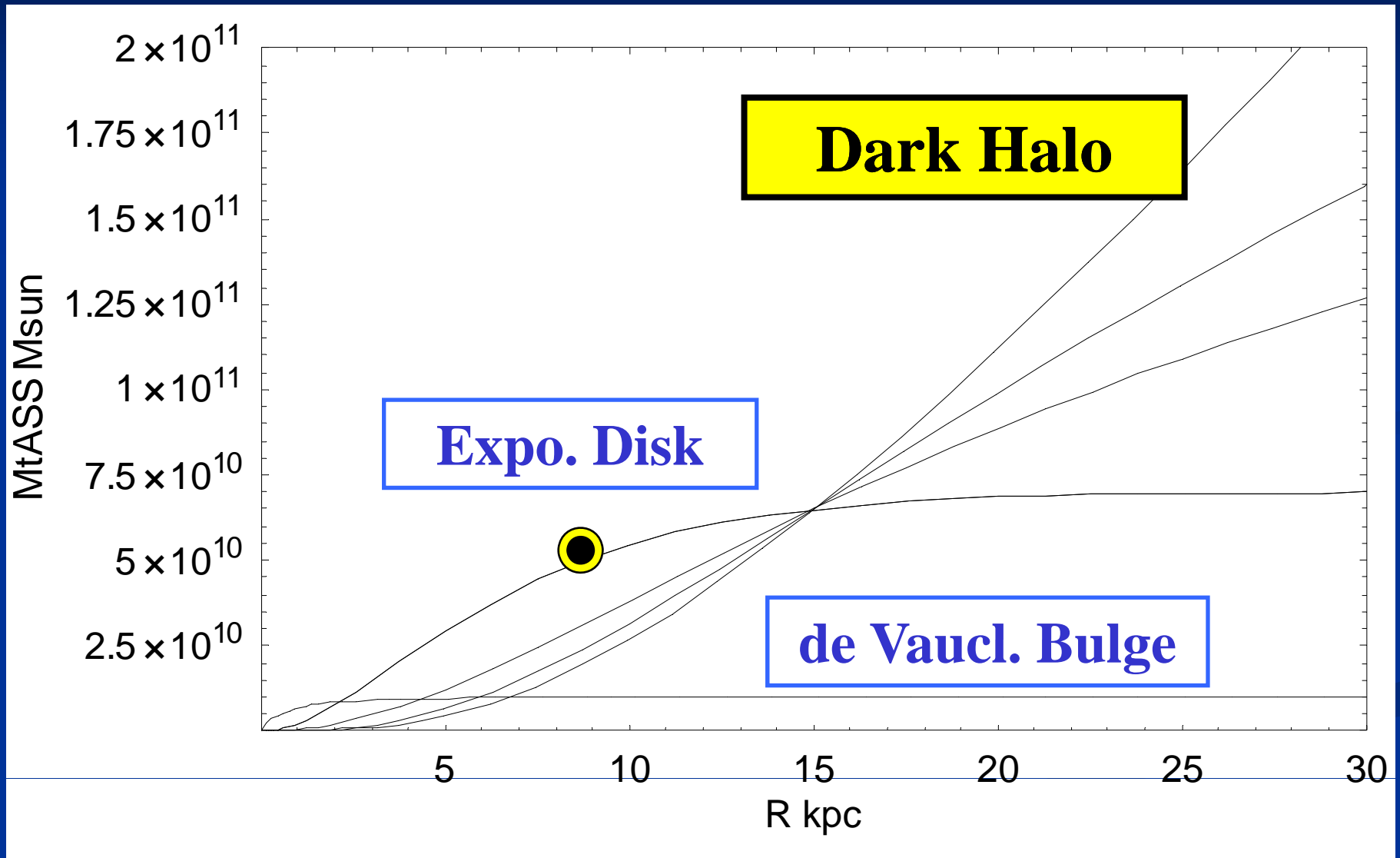
# Sofue, Honma, Omodaka 2009



# Volume Densities for Bulge, Disk, and Halo (Isoth, NFW, Burkert)



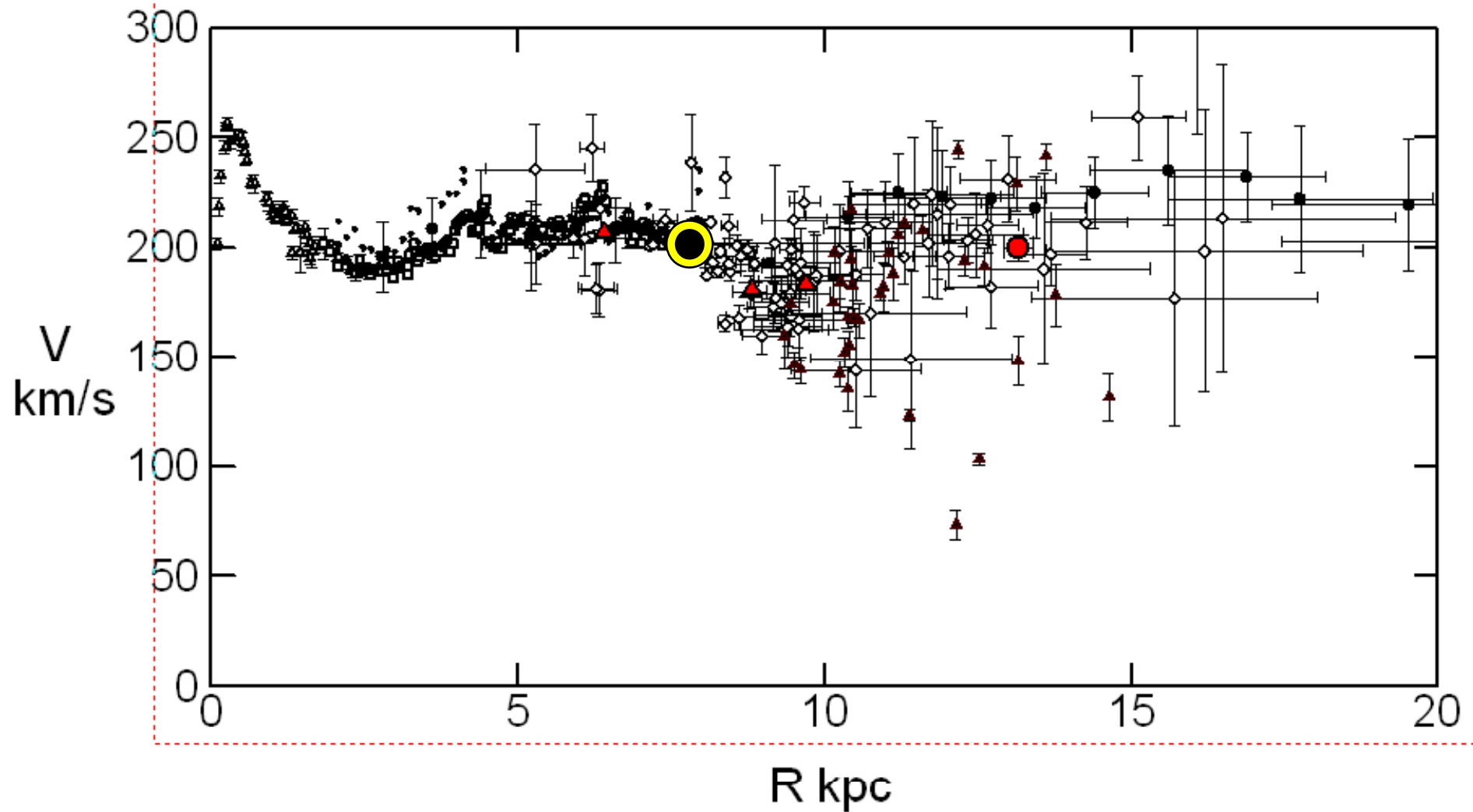
# Total Masses



# 3. Grand Rotation Curve



# Solar Circular Velocity $V_0=200$ km/s @ $R_0=8$ kpc

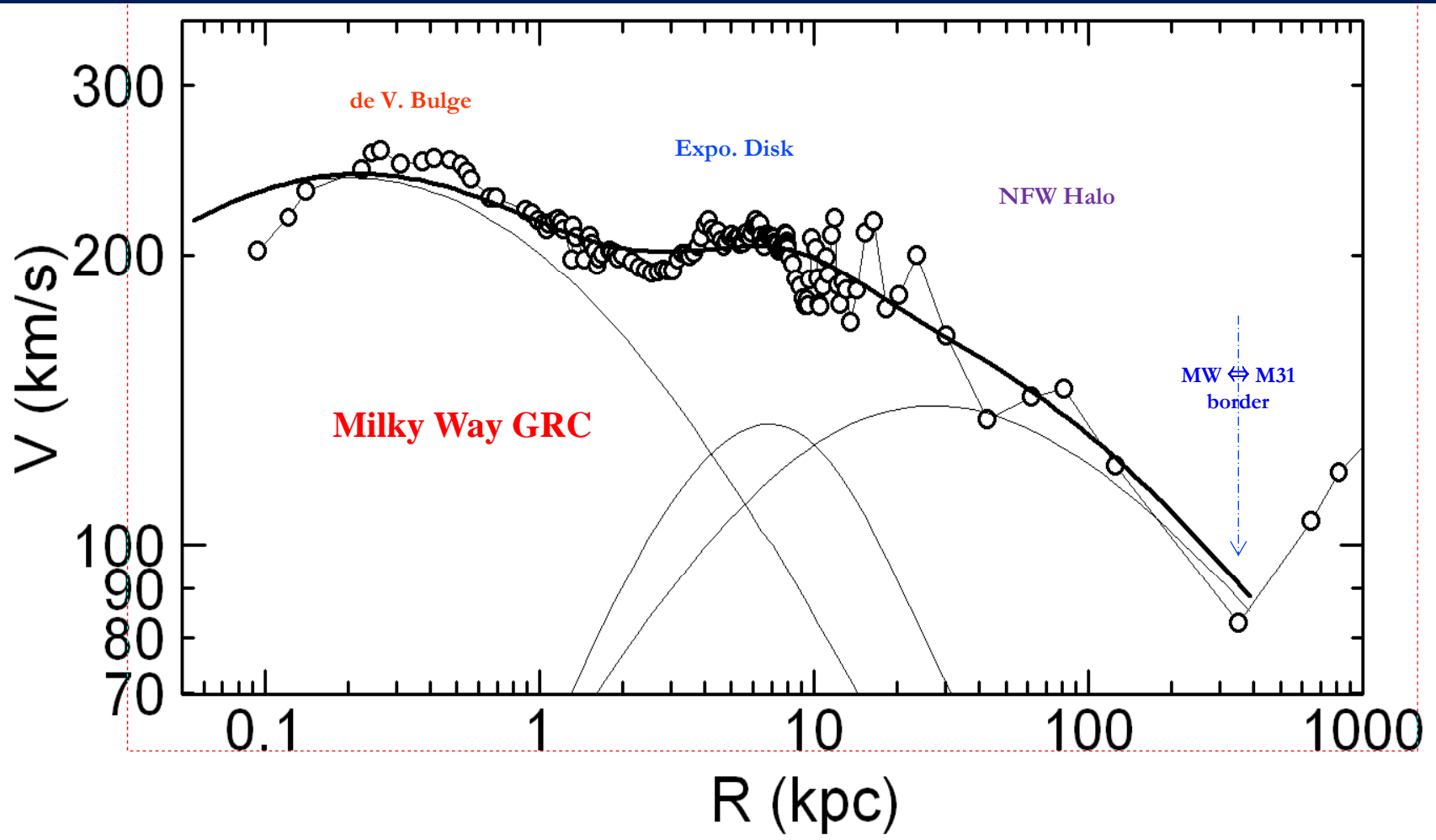


# Rotation curve at $R > 30$ kpc assuming random motion of satellite galaxies



Define:

$$V_{\text{rot}} = V_{\text{virial}} \doteq \sqrt{2} V_{\text{GC}}$$

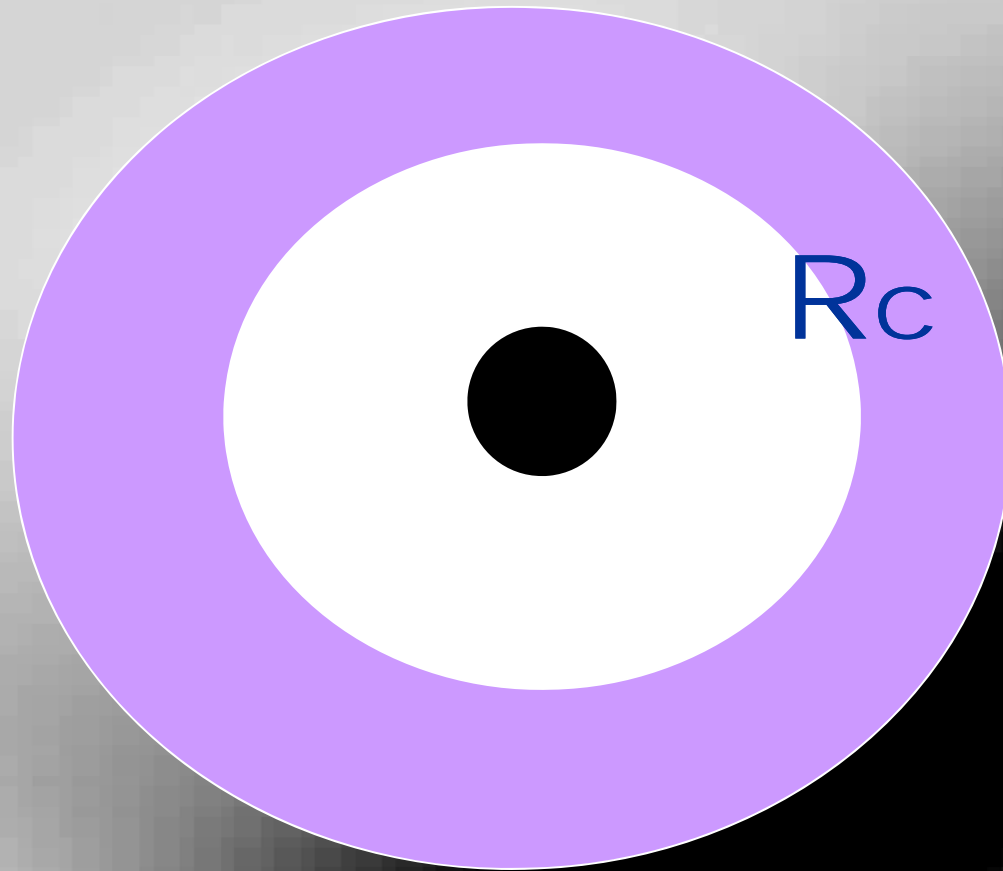


**Table 1.** Best-fit parameters for the mass components of the Galaxy

Mass component	Mass; Density	Scale Radius
Bulge param.	$M_b = (1.652 \pm 0.083) \times 10^{10} M_\odot$	$a_b = 0.522 \pm 0.037$ kpc
Disk param.	$M_d = (3.41 \pm 0.41) \times 10^{10} M_\odot$	$a_d = 3.19 \pm 0.35$ kpc
<b>B+D Mass</b>	$M_{b+d} = (5.06 \pm 0.97) \times 10^{10} M_\odot$	
B/D ratio	$M_b/M_d = 0.48 \pm 0.09$	
DH param.	$\rho_0 = (1.06 \pm 0.14) \times 10^{-2} M_\odot \text{pc}^{-3}$ $= 0.403 \pm 0.051 \text{ GeV cm}^{-3}$	$h = 12.53 \pm 0.88$ kpc
Local DM dens. at $R_0 = 8$ kpc	$\rho_0^\odot = (6.12 \pm 0.80) \times 10^{-3} M_\odot \text{pc}^{-3}$ $= 0.235 \pm 0.030 \text{ GeV cm}^{-3}$	
<b>DH Mass<sup>†</sup></b>	$M_h(R \leq 8\text{kpc}) = (2.71 \pm 0.42) \times 10^{10} M_\odot$ $M_h^*(\leq h) = (5.05 \pm 0.78) \times 10^{10} M_\odot$ $M_h(\leq 20\text{kpc}) = (8.87 \pm 1.37) \times 10^{10} M_\odot$ $M_h(\leq 385\text{kpc}) = (6.52 \pm 1.01) \times 10^{11} M_\odot$	
<b>Galaxy Mass</b>	$M_{b+d+h} = (7.03 \pm 1.01) \times 10^{11} M_\odot$	$(R \leq 385 \text{ kpc})$
<b>Baryon Fraction</b>	$M_{b+d}/(M_{b+d+h}) = \mathbf{0.072 \pm 0.018}$	

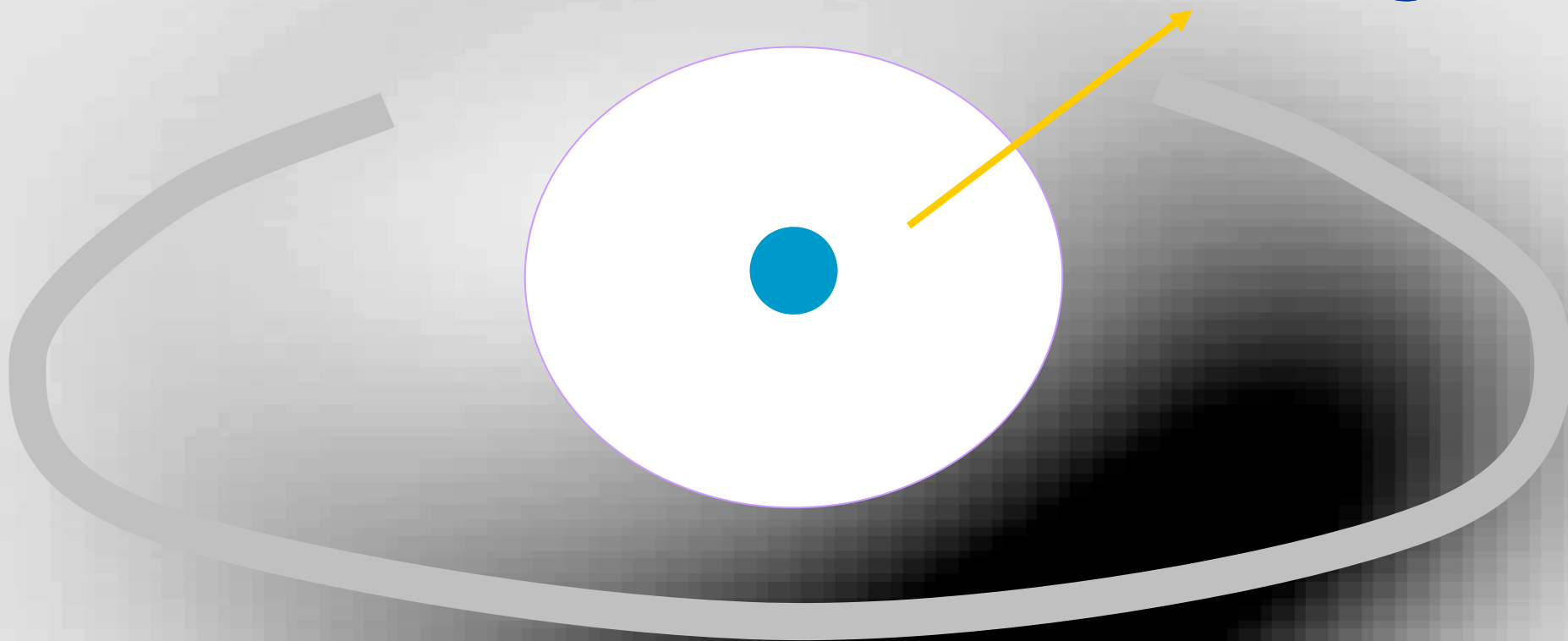
# 4. Galactic Center & BH

# 質量空白域 or DM cusp

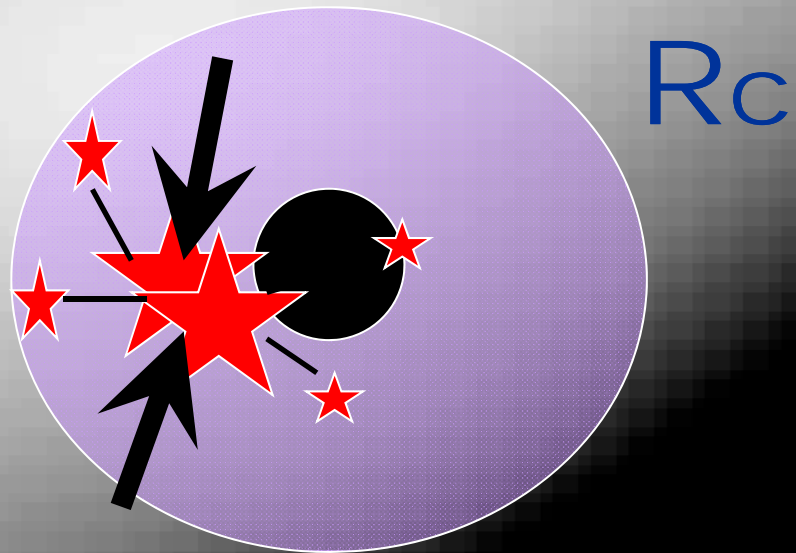


# 銀河質量研究の空白領域 BH - Bulge

Log R

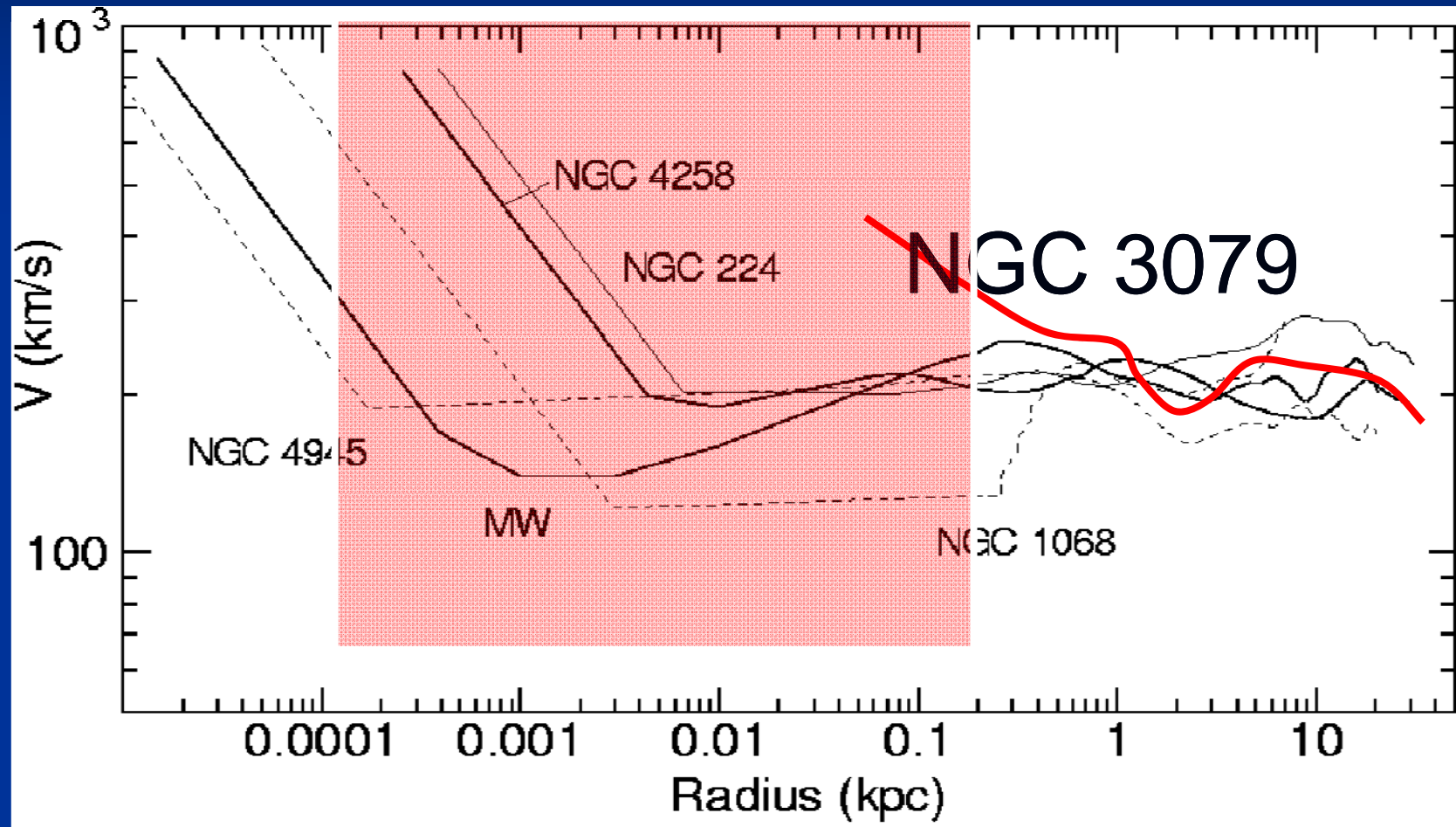


# BH formation in core/cusp

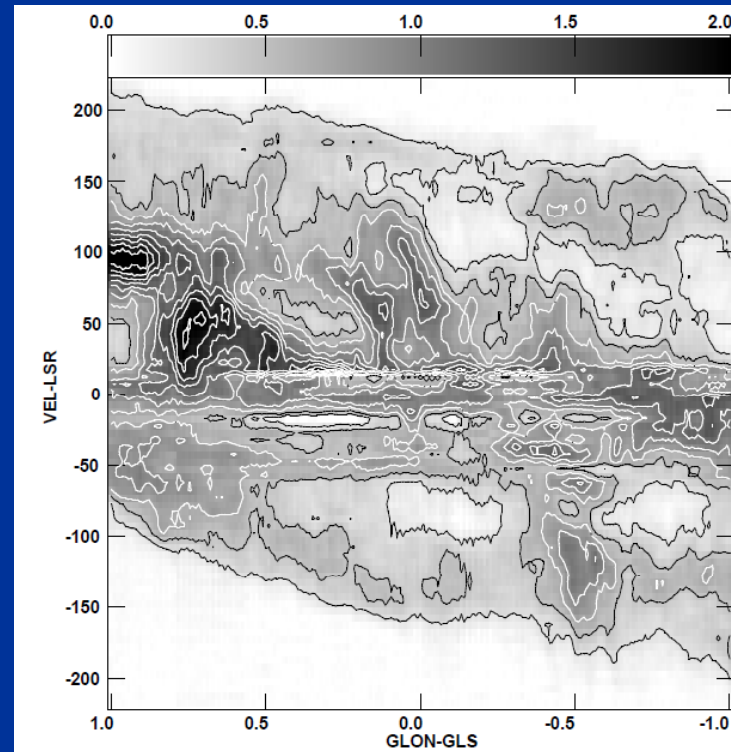
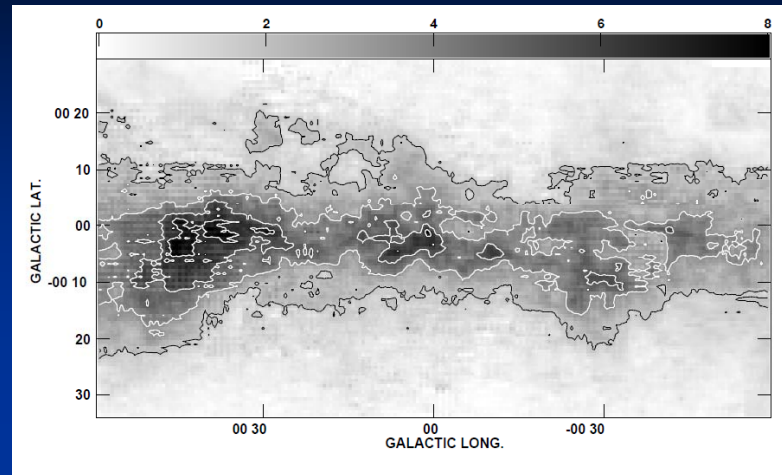




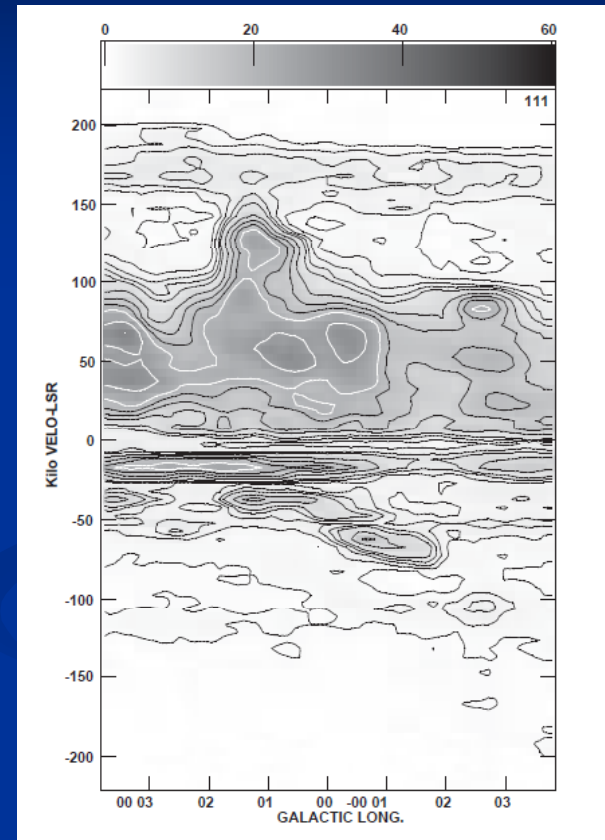
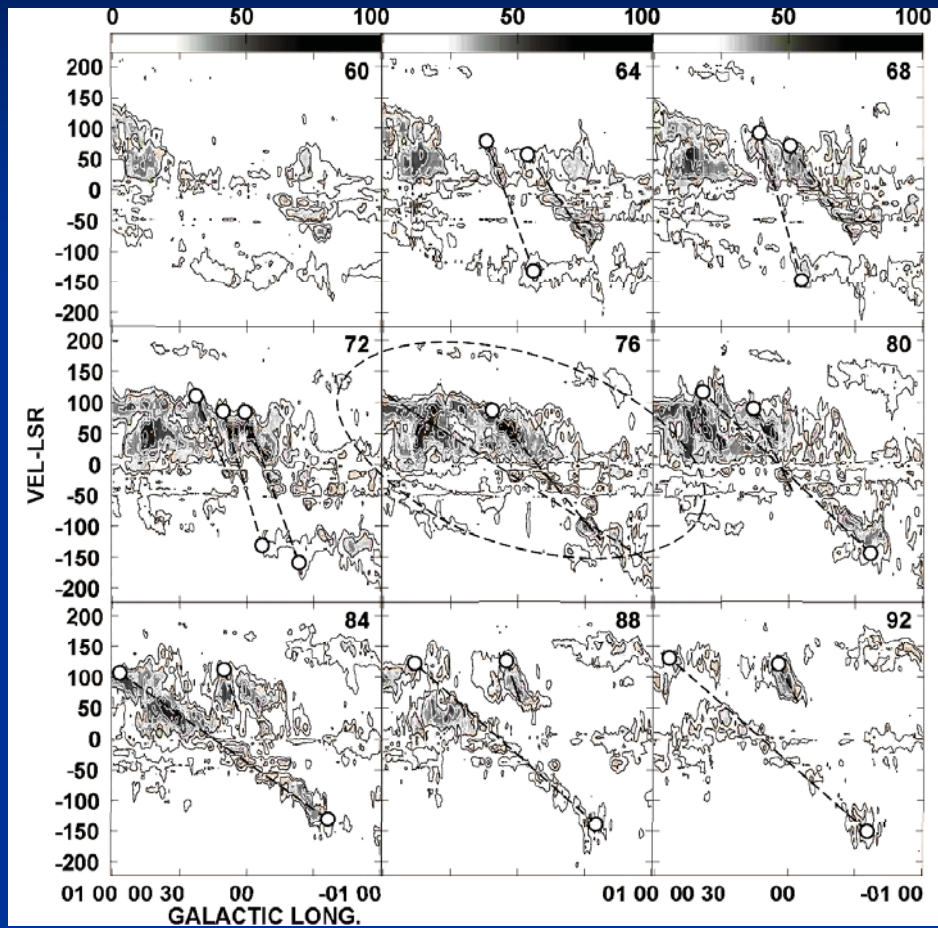
# BH – Bulge – Disk



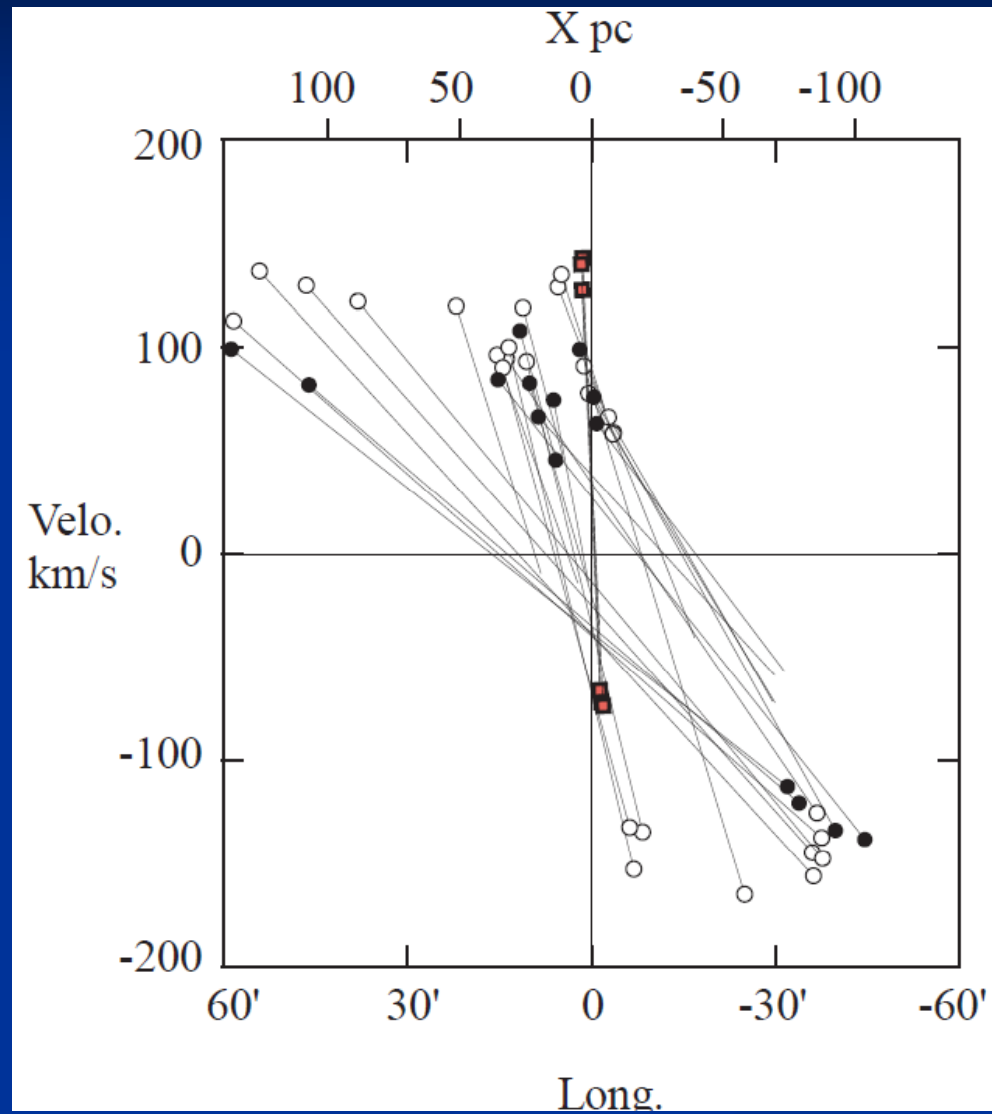
# GC CO map & LV diagrams



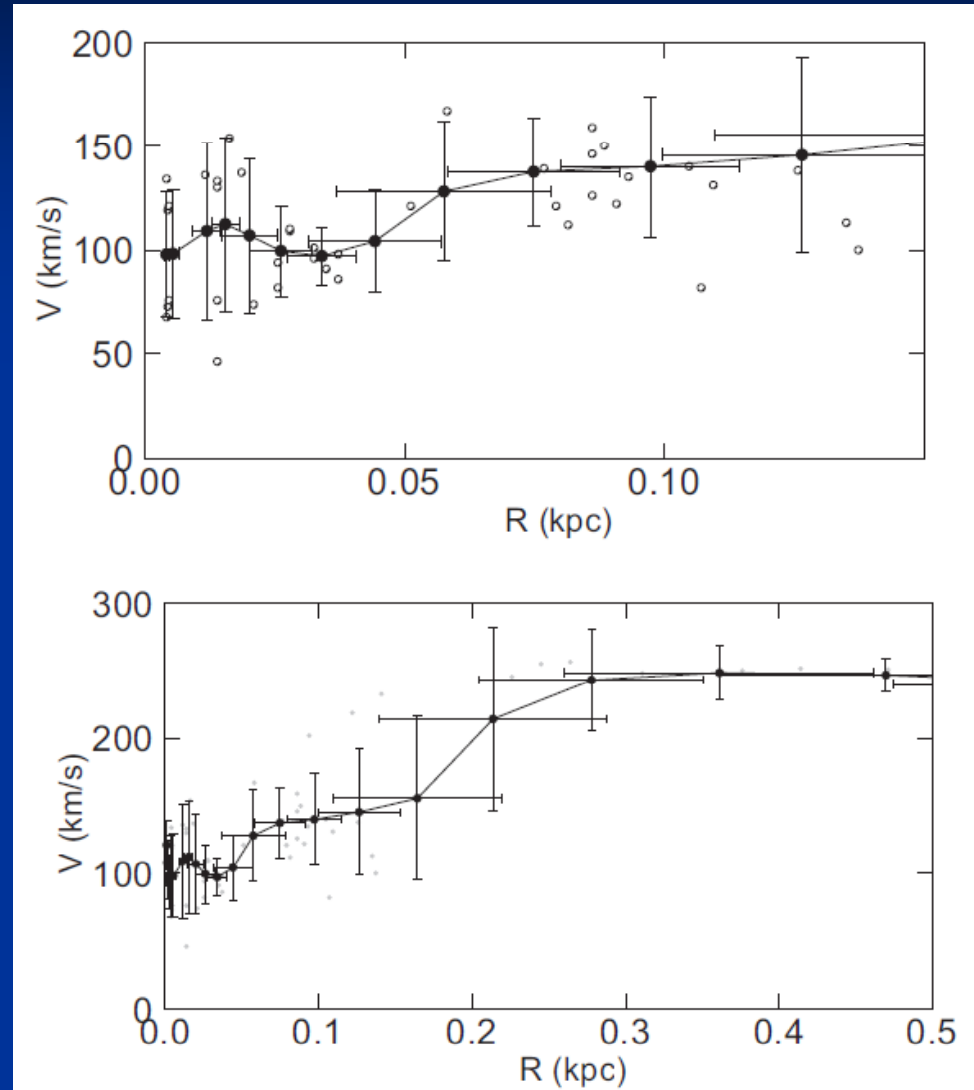
# CO LV diagrams



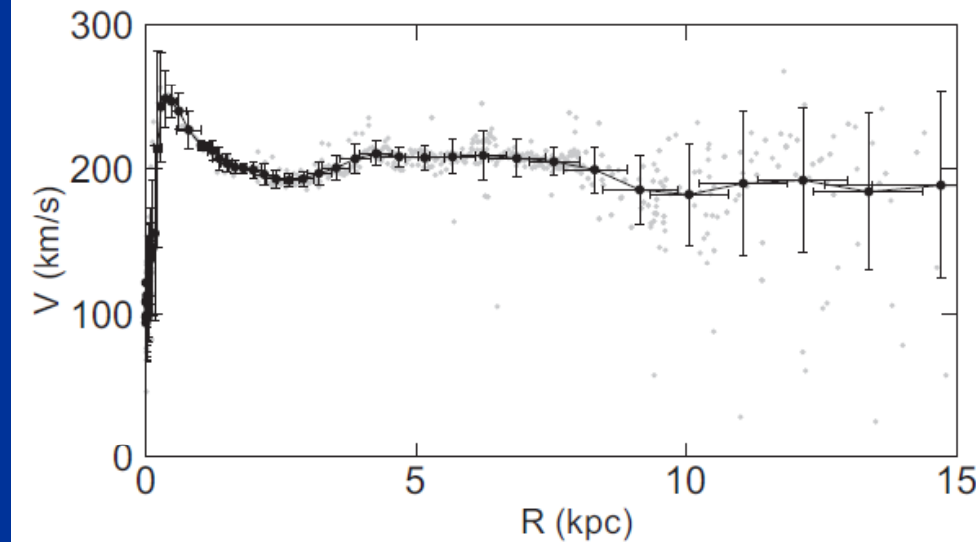
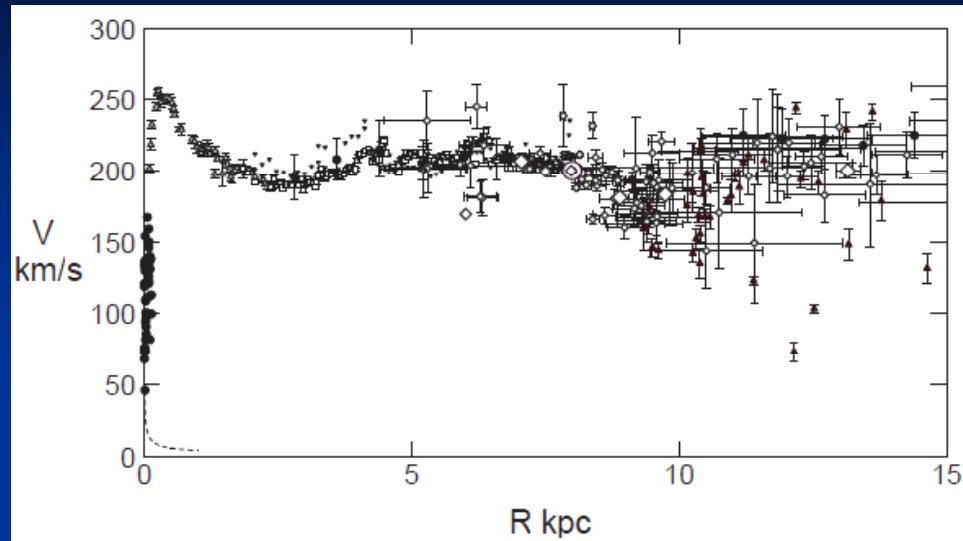
# Terminal Velocities



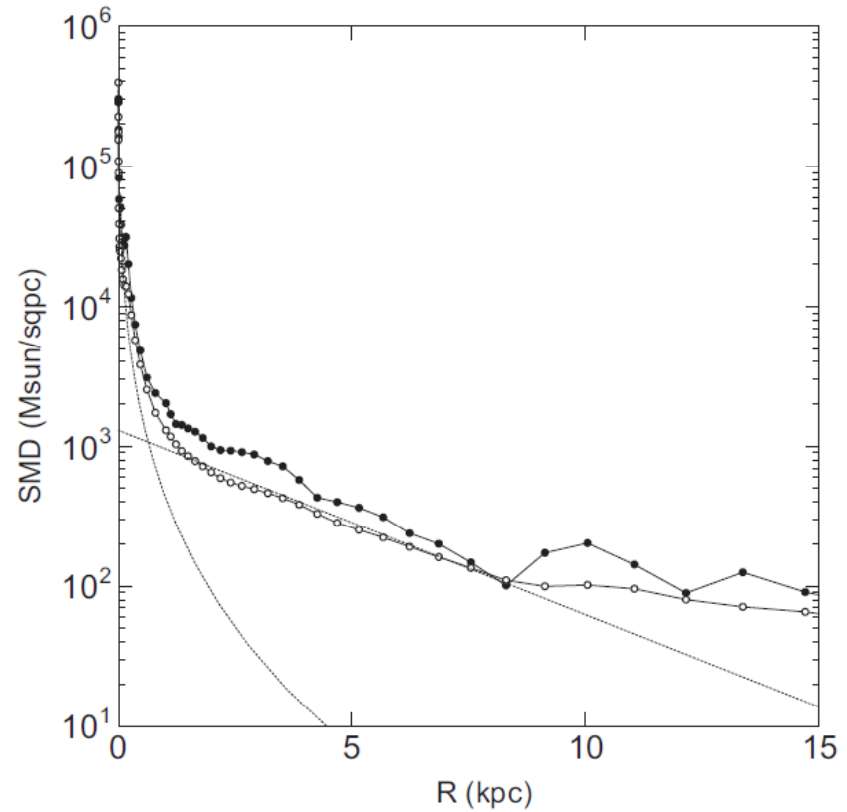
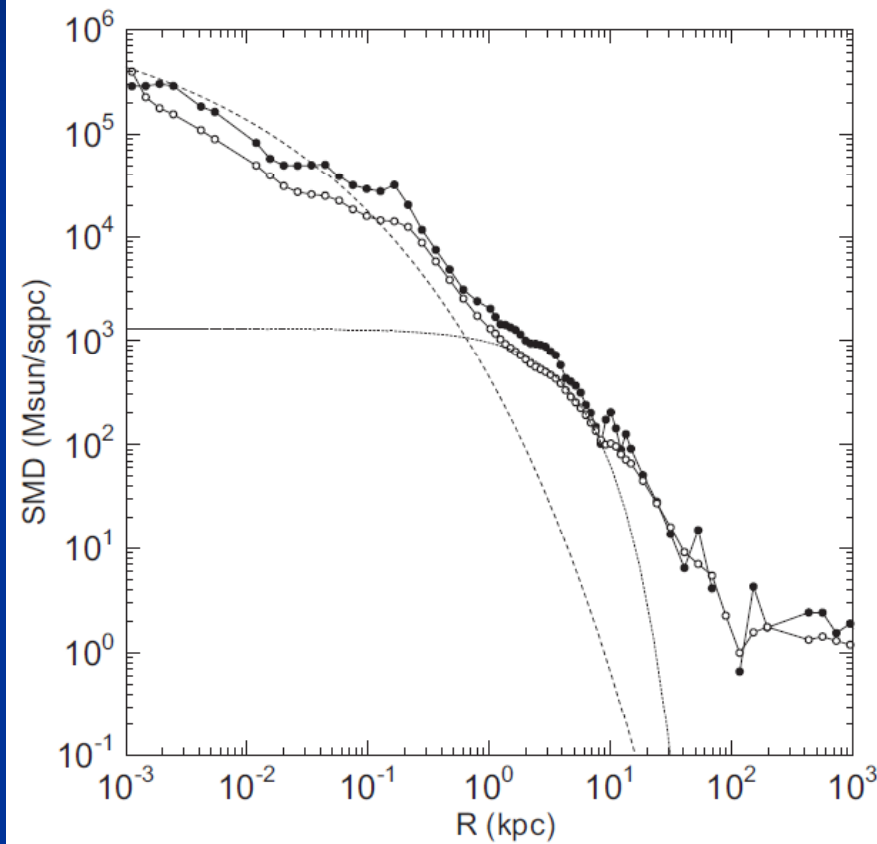
# GC Rotation Curve



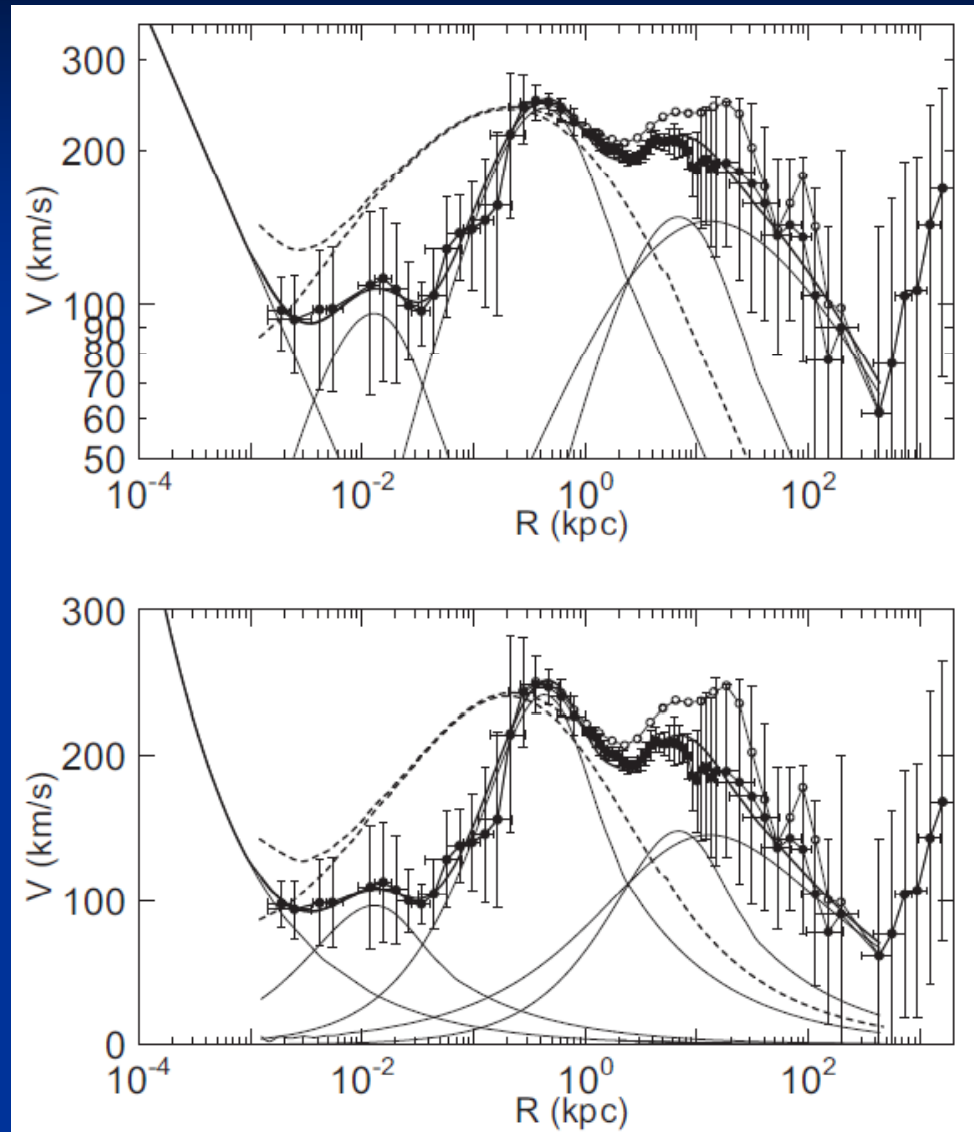
# Galaxy Rotation Curve



# Surface Mass Density

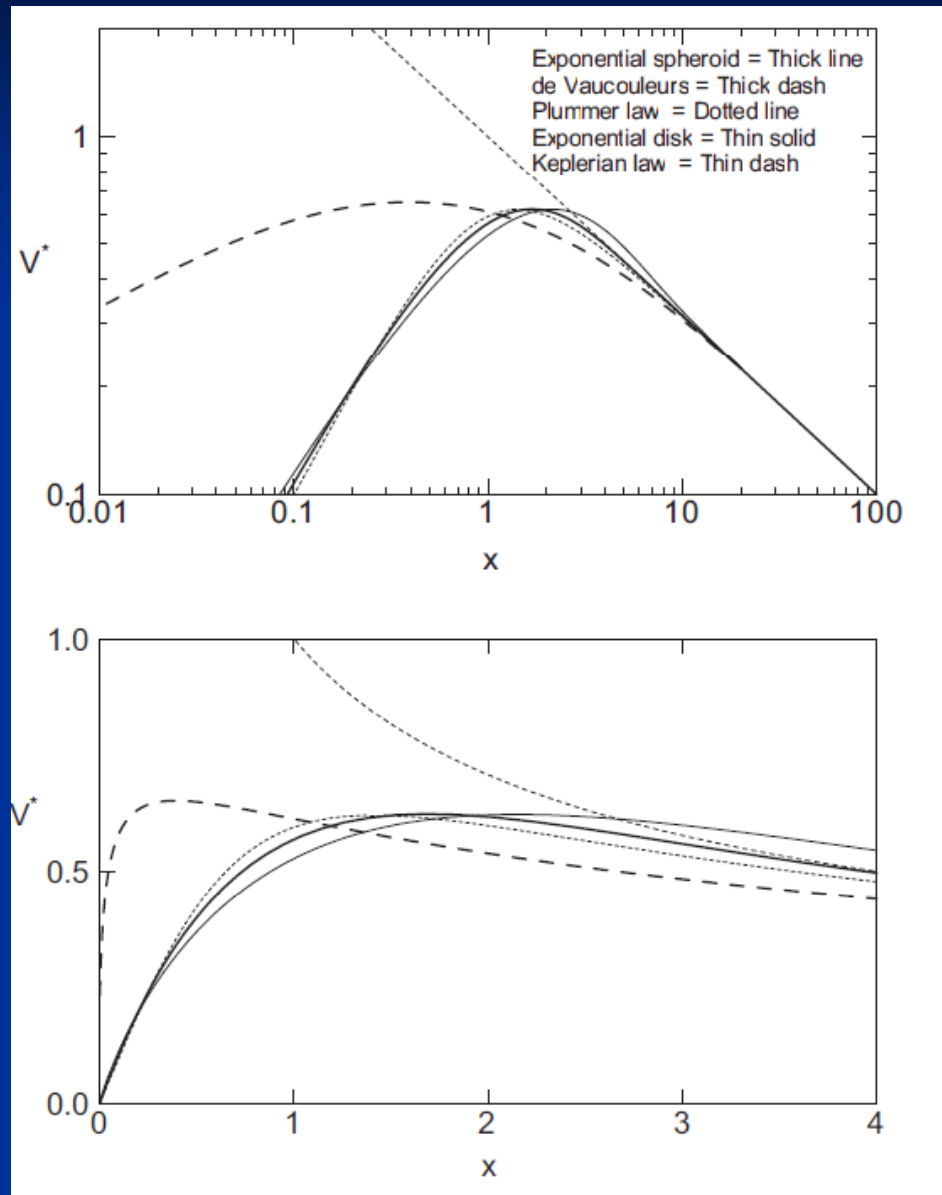


# Deconvolution of RC

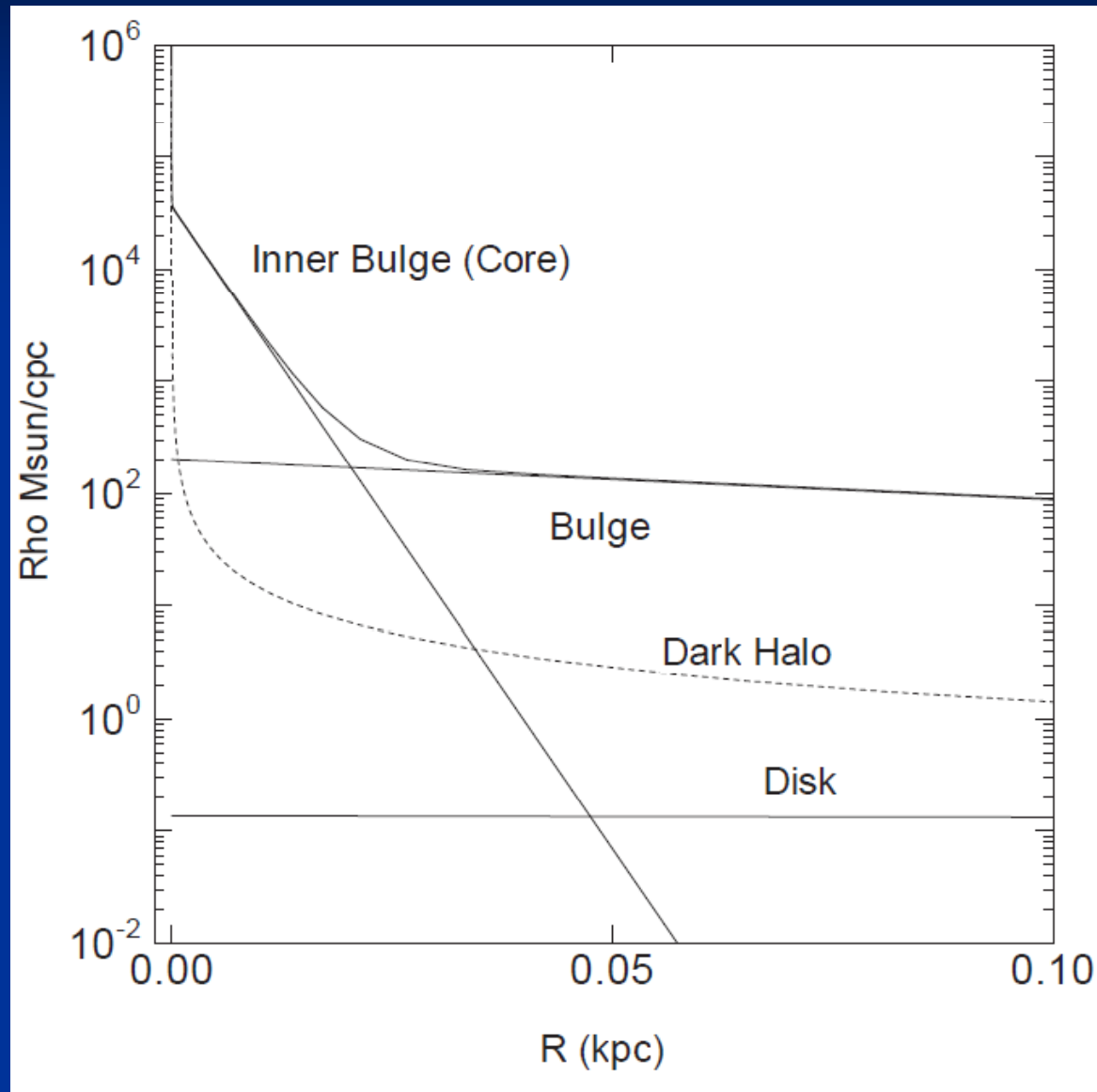




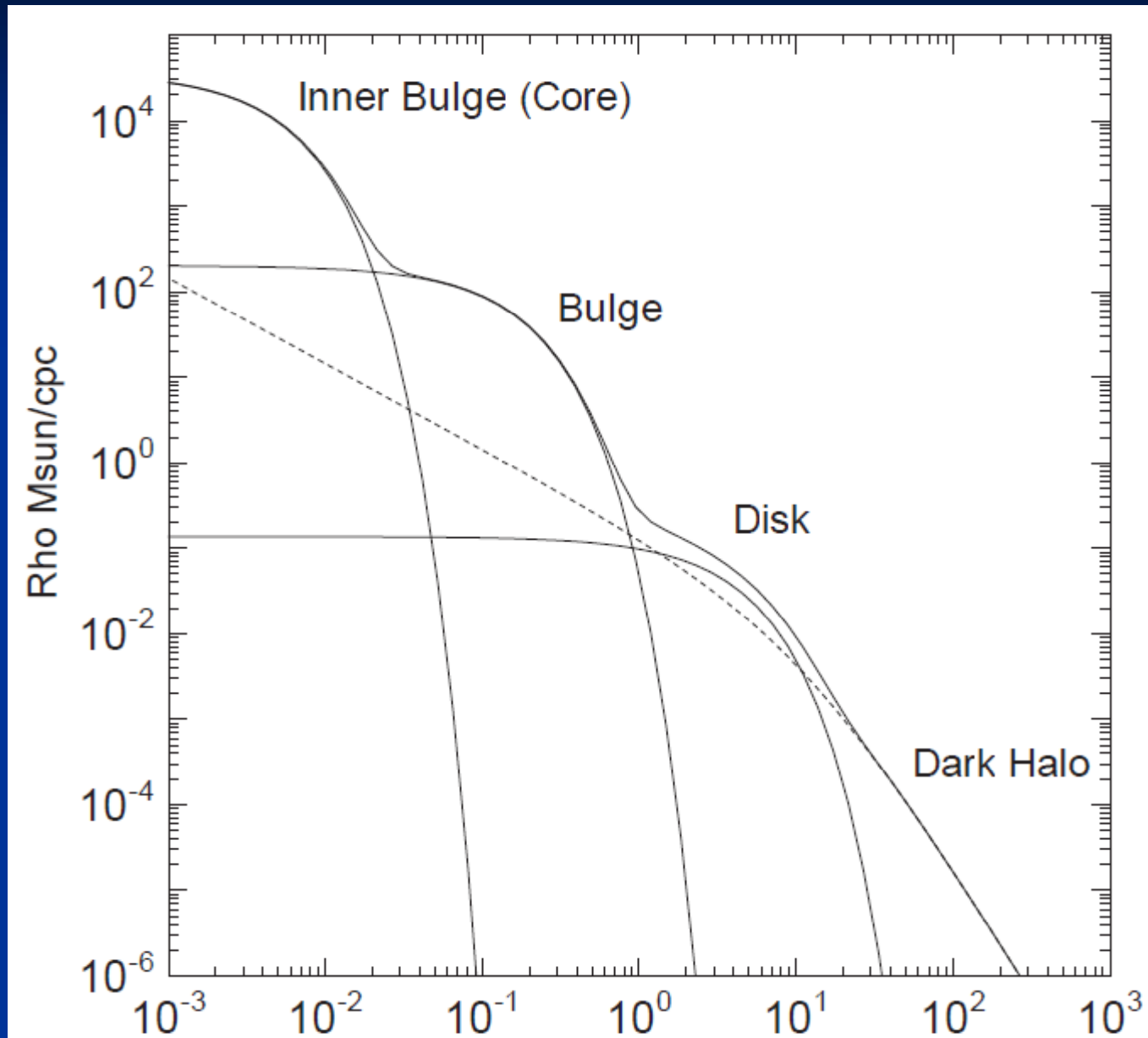
# Vaucouleurs vs Exponential



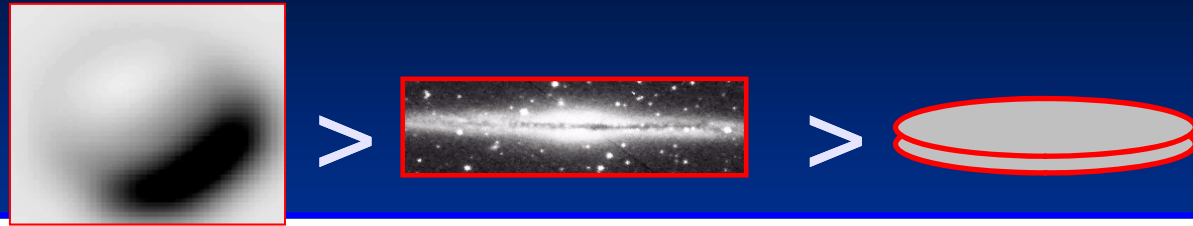
# Density (Semi Log)



# Density (Log Log)



# 質量分布一直接導出



(a) Spherical Mass Distribution:

$$M(r) = \frac{rV(r)^2}{G},$$

$$\rho(r) = \frac{1}{4\pi r^2} \frac{dM(r)}{dr}.$$

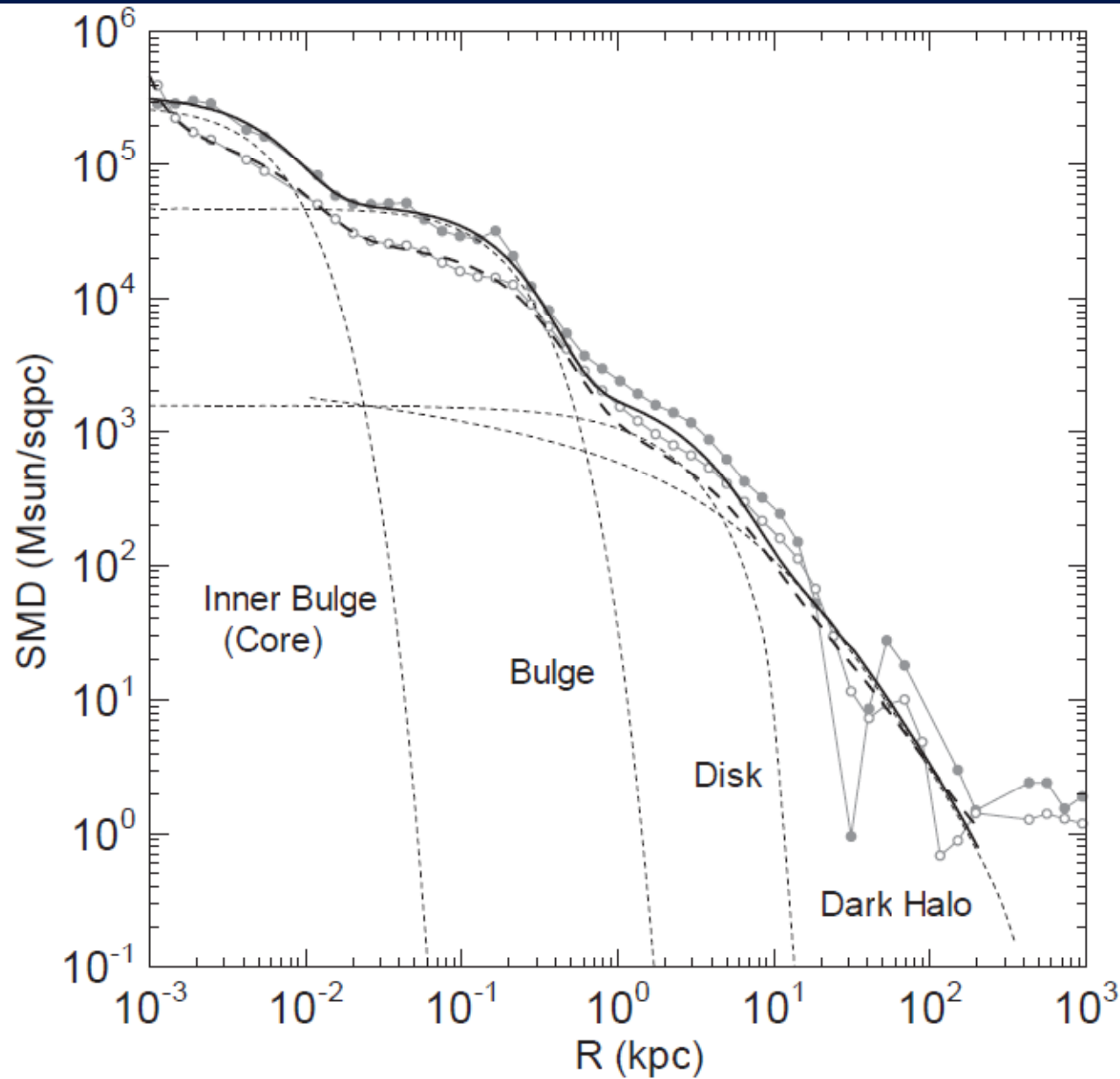
$$\sigma(R)_s = 2 \int_0^\infty \rho(r) dz = \frac{1}{2\pi} \int_R^\infty \frac{\left(\frac{dM(r)}{dr}\right)_x}{x\sqrt{x^2 - R^2}} dx,$$

(b) Flat-Disk Mass Distribution: Laplace's equation  $\Delta\Phi = 0$ :

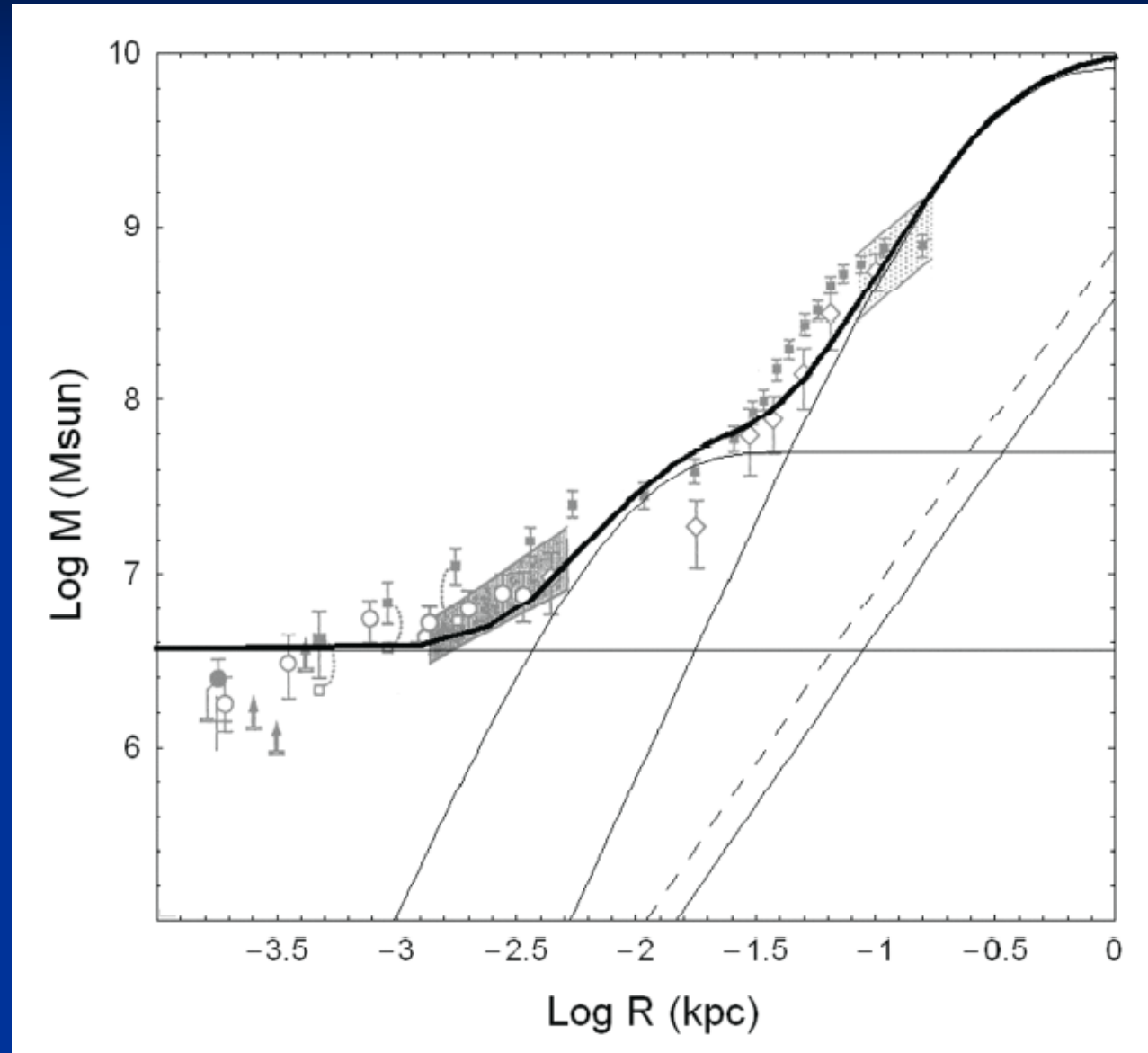
$$\sigma(R)_f = \frac{1}{\pi^2 G} \left[ \frac{1}{R} \int_0^R \left(\frac{dV^2}{dr}\right)_x K\left(\frac{x}{R}\right) dx + \int_R^\infty \left(\frac{dV^2}{dr}\right)_x K\left(\frac{R}{x}\right) \frac{dx}{x} \right],$$

where  $K(x)$  is the complete elliptic integral (Binney & Tremaine 1987).

# SMD : Obs vs Model



# Comparison with Genzel et al. 94



# RC Fitting Result:

(1) BH

(2) Bulge 1 : Exp. Sphere

(3) Bulge 2: Exp. Sphere

(4) Exp. Flat Disk

(5) NFW Dark Halo

# PASJ submitted 2013

PASJ: Publ. Astron. Soc. Japan , 1-??,  
© 2013. Astronomical Society of Japan.

## Rotation Curve and Mass Distribution in the Galactic Center and Entire Galaxy

Yoshiaki SOFUE<sup>1,2</sup>

1. *Department of Physics, Meisei University, Hinoshi-shi, 191-8506 Tokyo*
2. *Institute of Astronomy, University of Tokyo, Mitaka, 181-0015 Tokyo,*  
*Email:sofue@ioa.s.u-tokyo.ac.jp*

(Received 2013 0; accepted 2013 0)

PASJ: Publ. Astron. Soc. Japan , 1-??,  
© 2013. Astronomical Society of Japan.

## Logarithmic Rotation Curve and Multiple Bulges around the Galactic Center

Yoshiaki SOFUE<sup>1,2</sup>

1. *Department of Physics, Meisei University, Hinoshi-shi, 191-8506 Tokyo*
2. *Institute of Astronomy, University of Tokyo, Mitaka, 181-0015 Tokyo,*  
*Email:sofue@ioa.s.u-tokyo.ac.jp*

(Received ; accepted )



# Further Analysis of Activity in known Gravity Environment

